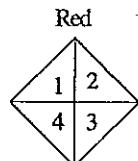
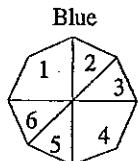


A Chance and data: Probability of multiple independent events

Skill 9.10

- 1 Each of these spinners is spun once. Find the probability of:
 - (a) Spinning each number on the blue spinner
 - (b) spinning each number on the red spinner
 - (c) spinning two 1's
 - (d) spinning two 2's
 - (e) spinning two 3's
 - (f) spinning two 4's
 - (g) spinning two even numbers
 - (h) spinning two odd numbers

- 2 A bag contains 3 red and 4 blue balls. A ball is selected and its colour noted and then it is replaced. This process occurs two more times. Find the probability that:
 - (a) All the balls are red
 - (b) all the balls are blue
 - (c) the balls are chosen in the order red, blue, red
 - (d) one ball is red and the other two are blue



B Chance and data: Probability of multiple dependent events

Skill 9.11

A bag contains 7 red balls, 5 blue balls and 3 white balls. A ball is selected at random and kept out of the bag. This process continues another two times.

Find the probability of selecting:

- | | |
|---|---|
| 1 Three red balls | 2 three blue balls |
| 3 three white balls | 4 red, blue and white in that order |
| 5 red, red then white in that order | 6 three different coloured balls in any order * |
| 7 two red and a white ball in any order * | (*List the orders to help work it out.) |

C Calculators: Scientific notation

Skill 10.6

Calculate:

- | | |
|---|---|
| 1 $3.07 \times 10^9 \times 6.03 \times 10^{12}$ | 2 $5.097 \times 10^{12} \times 3 \times 10^{-13}$ |
| 3 $9.07 \times 10^6 \div 5 \times 10^{-14}$ | 4 $1.02 \times 10^3 \times 6.03 \times 10^{12}$ |
| 5 $1.83 \times 10^{12} + 1.58 \times 10^{11}$ | 6 $8.04 \times 10^{13} - 6.04 \times 10^{12}$ |
| 7 $1.381 \times 10^{-11} + 4.9 \times 10^{-12}$ | 8 $1.581 \times 10^{14} - 3.81 \times 10^{12}$ |
| 9 $1.6 \times 10^{15} + 3.8 \times 10^{13}$ | 10 $1.48 \times 10^{17} - 3.81 \times 10^{15}$ |
| 11 $3.81 \times 10^{10} \times 3.9 \times 10^{-13}$ | 12 $7.07 \times 10^{11} \div 2 \times 10^{15}$ |

D Calculator: Reciprocals

Skill 10.7

- 1 Find the reciprocal of these numbers to 3 decimal places:
 - (a) 15
 - (b) -16.3
 - (c) 4.09
 - (d) 1.083
 - (e) -5.3

- 2 Use the reciprocal function to help calculate these to 3 decimal places:
 - (a) $\frac{5}{6+2\pi}$
 - (b) $\frac{\sqrt{2}}{5-2\sqrt{11}}$
 - (c) $\frac{5\pi}{7(2+\pi)}$
 - (d) $\frac{8}{\pi+\sqrt{8}}$
 - (e) $\frac{\sqrt{2}}{5+\pi+11.8}$
 - (f) $\frac{12}{3\pi+\sqrt{17}}$
 - (g) $\frac{2}{16(3\sqrt{2}+\pi)}$

E Calculators: Trigonometric functions

Skill 10.8

Find the angles expressed in degree/min form:

- | | | |
|---------------------------|---------------------------|---------------------------|
| 1 $\sin \alpha = 0.2138$ | 2 $\cos \alpha = 0.1238$ | 3 $\tan \alpha = 1.2148$ |
| 4 $\cos \alpha = 0.0314$ | 5 $\sin \alpha = 0.1318$ | 6 $\tan \alpha = 2.0314$ |
| 7 $\cos \alpha = 0.6214$ | 8 $\sin \alpha = 0.2643$ | 9 $\tan \alpha = 6.3142$ |
| 10 $\sin \alpha = 0.8142$ | 11 $\cos \alpha = 0.4104$ | 12 $\tan \alpha = 0.2314$ |

Worksheet 39

A 1 (a) Blue spinner

Number	1	2	3	4	5	6
Probability	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{8}$

(b) Red spinner

Number	1	2	3	4
Probability	$\frac{1}{4}$	$\frac{1}{4}$	$\frac{1}{4}$	$\frac{1}{4}$

(c) $\frac{1}{16}$ (d) $\frac{1}{32}$ (e) $\frac{1}{32}$ (f) $\frac{1}{16}$

(g) $\frac{1}{4}$ (h) $\frac{1}{4}$

2 (a) $\frac{27}{343}$ (b) $\frac{64}{343}$ (c) $\frac{36}{343}$ (d) $\frac{144}{343}$

B 1	$\frac{1}{13}$	$\frac{2}{91}$	$\frac{1}{455}$
5	$\frac{3}{65}$	$\frac{3}{13}$	$\frac{9}{65}$

C 1	1.85121×10^{22}
3	1.814×10^{20}
5	1.988×10^{12}
7	1.871×10^{-11}
9	1.638×10^{15}
11	0.014859
	2 1.5291
	4 6.1506×10^{15}
	6 7.436×10^{13}
	8 1.5429×10^{14}
	10 1.4419×10^{17}
	12 3.535×10^{-4}

D 1	(a) 0.067 (b) -0.061 (c) 0.244
	(d) 0.923 (d) -0.189
2	(a) 0.407 (b) -0.866 (c) 0.436
	(d) 1.340 (e) 0.071 (f) 0.886
	(g) 0.017

E 1	$12^{\circ}21'$	$82^{\circ}53'$
4	$88^{\circ}12'$	$5^{\circ}34'$
7	$51^{\circ}35'$	$15^{\circ}20'$
10	$54^{\circ}31'$	$65^{\circ}46'$
	3 $50^{\circ}32'$	6 $63^{\circ}47'$
	9 $81^{\circ}0'$	12 $13^{\circ}2'$
	11 $65^{\circ}46'$	