

Year 10

Yearly Examination 2009

Mathematics

General Instructions

- Working time 120 minutes
- Write using black or blue pen.
- Approved calculators may be used.
- All necessary working should be shown in every question if full marks are to be awarded.
- Marks may not be awarded for messy or badly arranged work.
- If more space is required, clearly write the number and the SECTION on the back page and answer it there. Indicate that you have done so
- Write all answers in simplest exact form unless specified otherwise
- Clearly indicate your class by placing an X, next to your class

NAME:

Examiner: E. Choy

Class	Teacher	Ī
10 A	Mr McQuillan	
10B	Ms Roessler	×
10 C	Ms Nesbitt .	
$10\mathrm{D}^{-2}$	Mr Fuller	
10 E	Mr Hespe	<u> </u>
10 F	Mr Gainford	
10 G.	Ms Evans	ļ

L	Section	Mark	Ì.
	1	~ /20	1
,	2		16
	3	/40	14
	4	/20	
	5	/20	
	6	- /20	
	7	/20	
	Total	./130	,

Ques	tion One (20 marks)	Answers	Marks
A	Write down the gradient of the line $y = 2x - 3$.		1
В	Simplify $(2m^3)^2$,	1
С	Expand and simplify $(\sqrt{3}-1)(\sqrt{3}+1)$		1
D	Write down the exact value of sin 60°.		1
Е	Simplify 8 ³		1
F	Given that $\tan\alpha=0.42$ and α is acute, use your calculator to find the angle α , correct to the nearest minute.		1
G	If $P(x)=1-8x^2+14x^3-5x^4$, write down the degree of the polynomial $P(x)$.		1
Н	Using the remainder theorem, find the remainder when the polynomial $P(x) = 2x^3 - x^2 + 3x - 1$ is divided by $(x-1)$.		1
I	Simplify $\frac{1}{a} + \frac{2}{a}$		1
1	Factorise $x^2 - 16$		1
K	Expand $(x-5)^2(\chi-1)$		1
L	Write $\frac{1}{x}$ as a power of x .		1
М	Subtract 1-x from 1+x.		1
N	Two similar statues have volumes in the ratio 1:64. What is the ratio of their heights?		1

	Sketch the graph of the line with equation $y = 5$.	
0		
-	Solve for $x: 2x-7=5-x$.	
P		
	M-1-1-1-111105000	
-	To what amount will \$5000 grow over 6 years if it is invested at 8% p.a. compound interest compounded yearly. (Give your answer to the nearest cent.)	
		1
	If $a = 2b\sqrt{\frac{c}{d}}$ express c in terms of a, b and d.	1
(Express $\sqrt[3]{2.5 \times 10^6}$ in standard (scientific) notation.	1
	Simplify $\sqrt{4-4x^2} - \sqrt{1-x^2}$	1
Ĺ		<u> </u>

Ques	stion Two (20 marks)	Answers	. Marks
Α.	Factorise $a^2 + 2ab + b^2$		- 1
••			1
			-
		je je sa	
	·,		
~			-
(B)			1
\cup			
	\bigvee		
		, '	1
	What test can be used to show that these two		1
	triangles are similar?	<u> </u>	
	Ron was asked to write down the value of		 -
	$\sqrt{16}$. He remembered that every positive		
C	number has two square roots, so that he		
_	wrote $\sqrt{16} = \pm 4$. Is Ron's answer correct?	Į.	1
	Give a reason for your answer.		1
	What is the value of $-x^2$ when $x = 5$?		
ъ	What is the value of is when x = 5.		1.
D	_		1
			<u> </u> -
	Find the centre and exact radius of the circle		,
	with the equation $x^2 + y^2 + 2y - 10 = 0$, by	. •	
E	first completing the square in y.	146	1
	ļ	<u> </u>	
	The midwide Service of the Company o	<u> </u>	<i>!</i>
	The midpoint of an interval is (2, 8). Find two distinct points that could be the end		1
F	points of this interval.		1
	points of this interval.	, ,	<u> </u> .
	The surface area of a closed hemisphere is		+-
	$12\pi \mathrm{cm}^2$. Find its radius.		
G	-		1
Ì			
		•	<u> </u>
	(i) Write down the minimum value of		1 /
-	$(x-1)^2+4$.		1
1			
H	CONTROL OF THE CONTRO		2
]	(ii) Without doing any further working,	•	· ~
	write down the number of solutions of		1
	$(x-1)^2 + 4 = 1 \div 3$	•	}
l	1		1

		Solve the equation $2^x \times 4 = 32$ for x.		
	1	boive the equation 2 x4=32 for x.		
	I		·	1
		•		ĺ
-	-1		<u> </u>	
1	1	12		٠
	1	Γ α	, i	
ļ		5.		
ر ا	_	13		/
1/	ľ	15		2
1	ノ		· 1	
	- 1	YY7 ' 1	. 1	
ĺ		Write down the exact value of:	}	
	İ	(i) $\tan \alpha$) , , , , , , , , , , , , , , , , , , ,	.
L.		(ii) $\tan(180^{\circ} - \alpha)$		
		Given the formula F = 9 C + 200 E-14-		
١,	ĸ	Given the formula $F = \frac{9}{5}C + 32^{\circ}$, find the		, [
-	*~	value of C if $F = 320^{\circ}$.	· ·	1
ĺ	į		i.	
		A new car costs \$35 690. If it depreciates at		
		a compound interest rate of 20% p.a., find its		
ļ.	.	value, to the nearest dollar, at the end of four		
} :	L	years.	: '	1
		3		
	Į		,	,
		Solve (algebraically) the pair of equations	· · · · · · · · · · · · · · · · · · ·	
		simultaneously.	ļ	
1		y=4x-1		
		y=x+2	' '	,
l١	м	y=x+ ⁵		. 1
1	.,,	•		1
1				
			. }	
			. }	
\vdash		On connected the second	1	-
		On separate diagrams sketch the graphs of		
		(i) $y = -x^3$,	
		•		
1			·	
			, 1	
	N			3
		:	·	1
		·		
	•			
. [-	
: ·			·	

	(ii) $y = 2x^2$		
	•		
ļ		, i	:
	•		
	,		
			`
	(iii) $y = -\sqrt{25 - x^2}$,	
			1
		-	
	(i) Find the exact value of cos150°.		
	•		
	1	r	_
	(ii) Solve the equation $\sin \theta = \frac{1}{\sqrt{2}}$ for		
0	$0^{\circ} \le \theta \le 180^{\circ}$.		2
			-
	· ·		
<u> </u>			1

Que	stion Three (10 marks)	Answers	Marks
A	A A B 16 B R C In the diagram above DE is parallel to BC, AE=16, CE=8 and DE=12. Let BC=x. (i) Show that $\triangle ABC$ is similar to $\triangle ADE$. (ii) Find x.		3
В	A house has a hemispherical roof of diameter 15 metres. The roof is to be painted (on the outside only) with a special reflective coating that costs \$120 per litre. How much (correct to the nearest hundred dollars) will it cost to purchase enough of the coating to paint the roof if one litre of the coating will cover an area of 5m ² ?		3
С	 Two similar cones have volumes 27cm³ and 64cm³. (i) Write down the ratio of the surface area of the smaller cone to the larger cone. (ii) Find the radius of the smaller cone if its height is ⁹/_π cm. 		4

Question Fo	our (20 marks)	Answers	Marks
Let P	be the parabola with equation		
	² -10x.	1 1	
(i)	Find the x-intercepts of P.		ľ
			Į
(41)	T 1.1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	3	1
	Find the coordinates of the vertex of P.		·
	r. ,		1
		<u> </u>	1
(iii)	Sketch the graph of P.		
` `	0 1		'
Ì	ı		
-			
	•	Į.	
		•	
			1
]			İ
			}
1			
A			9
ļ			
			[,
4			ļ
,		(52)	
		· ·	
(iv)	For what value of x does $x^2 - 10x$		1.
	take on its minimum possible value?	,	` [
}		;	1
	•	·	Į
(9)	Show that the point A(2, -16) lies on	•	
	P and write down the coordinates of		-
	the point B on P that is the reflection		1
	of A in the axis of symmetry of P.		
ļ			1
} }			
	•	-	
•			
]]			- }
1			1

		•	
	 The line I with equation 4x + y = 7 intersects the parabola P from part (A) in two distinct points. (i) Use simultaneous equations to find the two points of intersection. 		
	, , ·	3	l.
-	÷		
В			6
	(ii) Go back to your sketch on part (A)(iii) and include the line <i>I</i> , showing clearly its points of intersection with the parabola P.		
	B B C		
С	The diagram above shows a pyramid with square base ABCD. Point P is the apex of the pyramid. It is given that PD=PB=8 and $\angle PBD = 60^{\circ}$. The point P lies vertically above the centre X of the square.		5
	(i) Find length DB giving reasons.		
	(ii) Find the exact volume of the pyramid.	_	
			ļ

one de la destación de la des

Question Five (20 marks)	Answers	Marks
The diagram above shows the circle	Answers	Marks
$(x-1)^2 + y^2 = 25$ with centre A(1, 0) and radius 5. The point P(5, 3) lies on the circumference of the circle.		
(i) Find the gradient of AP.		
A (ii) Find, in general form, the equation of the tangent at P.		7

٠

	Consider the curve $y = ax^n$, where n is an		
	integer and a is a constant.	•	
	(i) If the curve passes through the point (-1, 2), find the possible values of a.		
	. (ii) It is known further that the graph has the form sketched below.		
	2 x		7
	(α) Write down three possible values for n .		
	(β) Given further that $\left(2, -\frac{1}{16}\right)$ lies on the curve, find the value of n .		
	There are 4 cards in a box. Each card has a letter on it. The letters on the cards are A, B, c and d. Two of the cards are chosen at random without replacement. (i) Draw a tree diagram to represent this experiment and list all the possible outcomes.		
c	(ii) Determine the probability that:	; 	. 6
	(α) the two capital letters are chosen.		
	(β) a capital letter and a lower case letter are chosen.		
39			

Question Six (20 marks)	Answers	Marks
A (i) In the diagram above, P has coordinates (-4, 2). Find length of OP. (ii) Write down the exact value of cos θ.		2
In the diagram above, QP is a tangent to the circle, while QRS is a secant. If QP = a units, QR = b units and RS = c units. Write down an equation (do not prove this equation) showing the relationship between a, b and c.		2

	•			
С	The diagram above shows a cyclic quadrilateral ABCD. The diagonal BD of the quadrilateral passes through the centre O of the circle and $\angle CAD = 42^{\circ}$. Find, giving reasons: (i) $\angle BAC$ (ii) $\angle BDC$		6	
	C_1 R C_2 In the diagram above, C1 and C2 are circles			-
D	in the diagram above, C1 and C2 are circles intersecting at A and B. The tangent to C1 at A meets C2 at P. Q is the point on C1 so that QB is parallel to AP. The chord QB intersects C2 at R. (i) Draw in the intervals AQ, AB and PR.	¢.	10	
	(ii) Give a reason why $\angle PAB = \angle AQB$. (iii) Give a reason why $\angle PAB = \angle PRB$			
	(iv) Explain why QA is parallel to RP. (v) Are QA and RP equal? Explain your answer.		,	
		·	'	l

.

•

Que	stion Seven (20 marks)	Answers	Marks
	(i) Find the size of each interior angle in a regular hexagon.		•
A	(ii) In the diagram above, the length of the straight line joining the midpoints of two adjacent sides of a regular hexagon is 12cm.		7
	(α) Calculate the exact length of one side of the regular hexagon.		
	(eta) Calculate the exact area of the regular hexagon.		

	In the diagram above, the vertices of $\triangle ABC$ and $\triangle ADC$ are on the circumference of a circle with centre O, and $\angle CAD = 90^{\circ}$.	
В	Let the diameter $CD = d$ and let $AC = b$.	4
	(i) Explain why $\angle ADC = \angle ABC$.	
and the state of t	(ii) Hence show that $\frac{b}{\sin B} = d$.	
-	The maximum daily temperatures (°C) recorded in a city over a period of 20 days are given below.	
С	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
	(ii) Find the interquartile range of the temperatures.	
	(iii) Find the standard deviation, correct to 1 decimal place.	
	(iv) What would be the two most appropriate measures of spread for these temperatures? Why?	

of mi

	(i) Prove that $ (a-b)^2 + (b-c)^2 + (c-a)^2 = 2(a^2 + b^2 + c^2 - ab - bc - ca) $	
	(ii) Use part (i) to prove that $a^2 + b^2 + c^2 \ge ab + bc + ca$.	
D.		3
	(iii) Use part (ii) to prove that $ (a+b+c)^2 \ge 3(ab+bc+ca). $	
i.	1,	
	(i) Without using a calculator, explain why $7^{\frac{1}{2}}$ is less than 3.	
E	(ii) Use methods similar to part (i) to explain why $7^{\frac{1}{2}} + 7^{\frac{1}{3}} + 7^{\frac{1}{4}} < 7$. (Once again do not use a calculator.)	2
	This is the and	

This is the end of the exam.

Ques	tion One (20 marks)	Answers	Marks
	Write down the gradient of the line		
А	y=2x-3.	2	1
	Simplify $(2m^3)^2$	6	
В		4m6	1
		<u> </u>	
	Expand and simplify $(\sqrt{3}-1)(\sqrt{3}+1)$	(J3) -(1) = 3-1=2	1
C		(03)	1
<u> </u>			
	Write down the exact value of sin 60°.	5/2	
D		2	1
-	1		
_	Simplify 8 ^{1/3}		
E		2	1
		·	
	Given that $\tan \alpha = 0.42$ and α is acute, use		
F	your calculator to find the angle α , correct	22° 47	1
	to the nearest minute.		<u> </u>
	If $P(x) = 1 - 8x^2 + 14x^3 - 5x^4$, write down	1	1
G	the degree of the polynomial $P(x)$.	4	
`	the degree of the polynomial 1 (x).	7	
	Using the remainder theorem, find the	P(1)=2(1)3-(1)2+3(1)-11)	+
	remainder when the polynomial	= 2 - 1 +3-1	
H	$P(x) = 2x^3 - x^2 + 3x - 1$ is divided by		1
1	(x-1).	- 3	1
		3	†
. I	Simplify $\frac{1}{a} + \frac{2}{a}$	$\frac{3}{a}$	1 1
	Factorise $x^2 - 16$		
J	.	(x+4) (x-4)	1
<u> </u>			<u> </u>
	Expand $(x-5)^2(x-1)$	7 - (- 171	
K		72-57-57 + 23	1
<u> </u>		カレーしつスナンら	
	Write $\frac{1}{x}$ as a power of x.		
L	x	x	1
-	Subtract $1-x$ from $1+x$.	-	1
м		1+x - (1-x) = 2x	-
INT			1 1
	Two similar statues have volumes in the		-
И	1	1:4	1
	heights?		{

Stower Con-

	Sketch the graph of the line with equation $y = 5$.	y=5.	
0			1
-	Solve for $x: 2x-7=5-x$.		
	Solve for $x: 2x-1=5-x$.	n=4	
P			1
Q	To what amount will \$5000 grow over 6 years if it is invested at 8% p.a. compound interest compounded yearly. (Give your answer to the nearest cent.)	5000x (1.08) 12	1
-			
R	If $a = 2b\sqrt{\frac{c}{d}}$ express c in terms of a, b and d.	$\frac{a}{2b} = \int_{-\frac{\pi}{d}}^{\frac{\pi}{d}} \left(\frac{a}{2b}\right)^{\frac{\pi}{d}} = \frac{a}{d}$	1
		c= \frac{a^2 d}{4b^2}	
8	Express $\sqrt[3]{2.5 \times 10^6}$ in standard (scientific) notation.	1357×102	1
Т	Simplify $\sqrt{4-4x^2} - \sqrt{1-x^2}$	JI-X2	_1

Oues	tion Two (20 marks)	Answers	Marks
A	Factorise $a^2 + 2ab + b^2$	(atb) ²	1
B	What test can be used to show that these two triangles are similar?	right L vent opp Ls : 3 L mother equal typpiblity there right angle and two equal again	1
С	Ron was asked to write down the value of $\sqrt{16}$. He remembered that every positive number has two square roots, so that he wrote $\sqrt{16} = \pm 4$. Is Ron's answer correct? Give a reason for your answer.	yes because (-4) and 42 both end le alto high solutions	1
D	What is the value of $-x^2$ when $x = 5$? $-(5)^{x}$	-25	1
Е	Find the centre and exact radius of the circle with the equation $x^2 + y^2 + 2y - 10 = 0$, by first completing the square in y.	x2+ y22y = 10 centre (6/19) y272y+(1) = 11 radius HT x2+(y+1)2 = 11	1
F	The midpoint of an interval is (2, 8). Find two distinct points that could be the end points of this interval.	$(\frac{1+3}{2})(\frac{7+9}{2})$	1
G	The surface area of a closed hemisphere is $12\pi \text{ cm}^2$. Find its radius.	3A: 2xx = 12x i = 6 C J6	1
н	 (i) Write down the minimum value of (x-1)² + 4. (ii) Without doing any further working, write down the number of solutions of (x-1)² + 4 = 1:3 	y= 4	2

1	Solve the equation $2^x \times 4 = 32$ for x.	χ=3
(Ī)	Write down the exact value of: (i) $\tan \alpha$ (ii) $\tan (180^{\circ} - \alpha)$	$\tan d = \frac{5}{12}$ $\tan(1\pi u - d) = -\frac{5}{12}$
K	Given the formula $F = \frac{9}{5}C + 32^{\circ}$, find the value of C if $F = 320^{\circ}$. 320^{-3}	學 (2160) 1
L	A new car costs \$35 690. If it depreciates at a compound interest rate of 20% p.a., find its value, to the nearest dollar, at the end of four years.	35690 ×(0·s) 9 -
М	Solve (algebraically) the pair of equations simultaneously. $y = 4x - 1 \cdots \bigcirc y = x + 2 $	$4x^{-1} = x + 1$ $3x = 3$ $x = 1$ $y = 3$
N	On separate diagrams sketch the graphs of (i) $y = -x^3$	(-1,1)

(x11:-3

		· · · · · · · · · · · · · · · · · · ·	
	(ii) $y = 2x^2$	(2,8)	
	(iii) $y = -\sqrt{25 - x^2}$	-S	
	(i) Find the exact value of cos150°.	- 55 2	
0	(ii) Solve the equation $\sin \theta = \frac{1}{\sqrt{2}}$ for $0^{\circ} \le \theta \le 180^{\circ}$.	45° ,135°	2

Ques	tion Three (10 marks)	Answers	Marks
	A	i) h DABC M DADE	(A)
	16	LADE = LABC (como Lo DELIBE)	
		LAEDE LACIS COMILIDELLO	Grd
	D 12 E	: ABC = AADE (cynegle)	
A	$\frac{1}{B}$ $\frac{1}{x}$ C		3
	In the diagram above DE is parallel to BC, AE=16, CE=8 and DE=12. Let BC=x. (i) Show that ΔABC is similar to ΔADE.	16 2 12 prefs 24	
	(ii) Find x.	x=18	
	A house has a hemispherical roof of diameter 15 metres. The roof is to be painted (on the outside only) with a special	2xr2= 2x5633	
В	reflective coating that costs \$120 per litre. How much (correct to the nearest hundred dollars) will it cost to purchase enough of the coating to paint the roof if one litre of the coating will cover an area of 5m ² ?	70.19 × 10	3
į.	· ·	~ \$8500	
	Two similar cones have volumes 27cm ³ and 64cm ³ .	81= 7×9 ×1	
	(i) Write down the ratio of the surface area of the smaller cone to the larger cone.	9:16	
С	(ii) Find the radius of the smaller cone if its	9=12	4
	height is $\frac{9}{\pi}$ cm.	V= 1/3 x = 1/2 h 27 = 1/3 x = 1/2 h	
		81= 712 A Rut	/

Question Four (20 marks)	Answers	Marks
Let P be the parabola with equation	/ac'	
$y = x^2 - 10x. \qquad \gamma(\chi - 1)$	1 / 5-0-25	
(i) Find the x-intercepts of P.	n 10/ 10/ 2	} }
	250,10/192,5	
(ii) Find the coordinates of the vertex of		
P.		
	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	4/1
(iii) Sketch the graph of P.		V
	, (
	1 1	
	(-1,11) 8	1, 1
	0 1	/ 1
	(21)	/ _ 1
	(5:25)	(10)
		(\mathcal{U})
	,	Ψ/
	ļ	1
		وا
A		
1		}
(iv) For what value of x does $x^2 - 10x$)
take on its minimum possible value?	V/I	<i>7</i>
		/
100		}
Show that the point A(2, -16) lies on P and write down the coordinates of		
P and write down the coordinates or the point B on P that is the reflection		
of A in the axis of symmetry of P.		
of 11 in the axis of symmetry of 1.	(8,-16)	ļ
Fuzz-102 DAMA	\\\'\'\ /	\
107		
-16 = 2 -01 W	1)
16=4-20 P		/
of A in the axis of symmetry of P. $y = x^{2} - y\rangle \qquad P p p A$ $- \phi = 2 - \phi \qquad \psi = 0$ $- \phi = \psi - \psi \qquad P$ $- \phi = \psi - \psi \qquad P$		

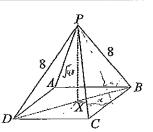
The line *l* with equation 4x + y = 7intersects the parabola P from part (A) in two distinct points.

(i) Use simultaneous equations to find the two points of intersection.

$$y=x^{2}-6x$$
...(0
 $4x+y=7$...(2)
 $y=x^{2}-10x$.. (1)
 $y=4x+7$...(2)

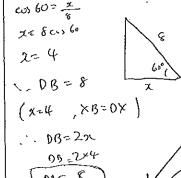
(ii) Go back to your sketch on part (A)(iii) and include the line *l*, showing clearly its points of intersection with the parabola P.

$$\chi^{2}-(0)\chi^{2}-(4)\chi^{2}-7$$
 $\chi^{2}-(0)\chi^{2}-7=0$
 $(\chi^{2}-7)(\chi^{2}+1)$
 $\chi^{2}-7,-1$
 $\chi^{2}-21$, 11
 $(\chi^{2}-21)$, $(\chi^{2}-1)$



The diagram above shows a pyramid with square base ABCD. Point P is the apex of the pyramid. It is given that PD=PB=8 and $\angle PBD = 60^{\circ}$. The point P lies vertically above the centre X of the square.

- (i) Find length DB giving reasons.
- (ii) Find the exact volume of the pyramid.



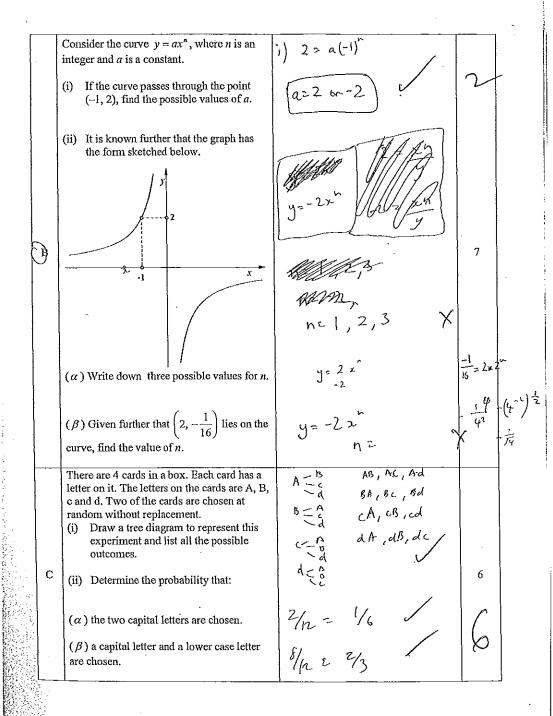
$$V^{2}\frac{1}{3}$$
 base $\times \sqrt{48}$
= $\frac{1}{3}(\sqrt{32})^{2} \times \sqrt{48}$
= $\frac{1}{3} 32 \times \sqrt{48}$

$$= \frac{1}{3} \times 32 \times 4\sqrt{3}$$

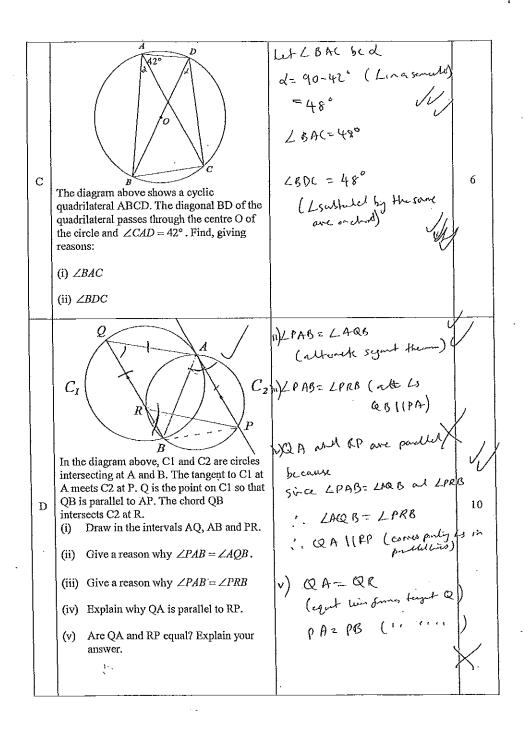
$$= \frac{1}{3} \times 32 \times 4\sqrt{3}$$

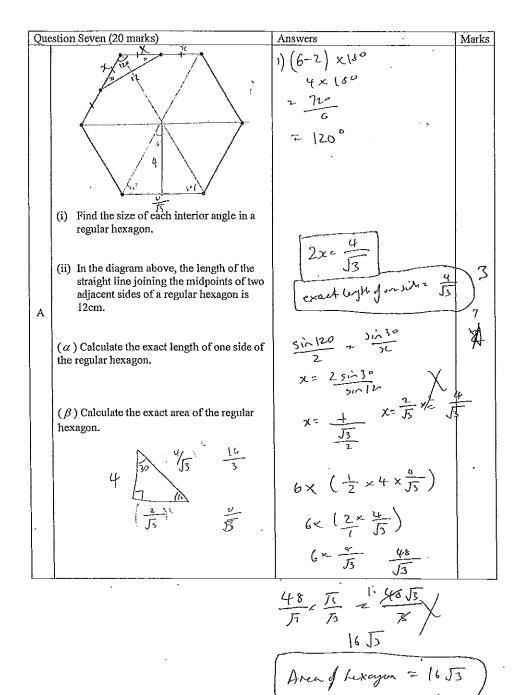
$$= \frac{1}{3} \times 32 \times 4\sqrt{3}$$

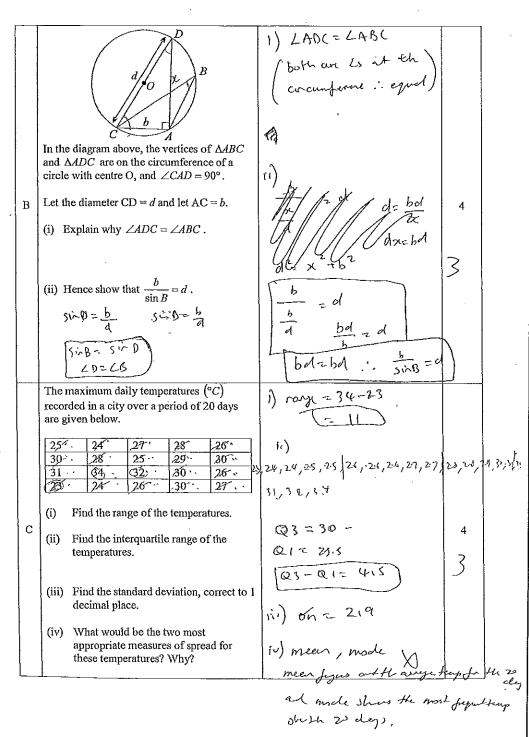
Question Five (20 marks)	Answers	Marks
The diagram above shows the circle $(x-1)^2 + y^2 = 25$ with centre A(1, 1 radius 5. The point P(5, 3) lies on the circumference of the circle. (i) Find the gradient of AP.	$\frac{3-6}{5-1} = \frac{3}{4}$ $m = \frac{3}{4}$ (i) $y - 3 = \frac{3}{4}(x-5)$ 0) and	7
(ii) Find, in general form, the equather tangent at P.	27 49 100	
[3-1-45-	4y=3x-3 [3x-4y-3=6) This is AP	2



Question Six (20 marks)	Answers	Marks
A (i) In the diagram above, P has coordinates (4, 2). Find length of OP. (3) $0 < 90 + d$ (ii) Write down the exact value of $\cos \theta$. (3) $0 < 5 $ $\sin \theta$	$D = \sqrt{(4-0)^2 + (2-0)^2}$ $= \sqrt{-4^2 + 2^2}$ $= \sqrt{20}$ $= \sqrt{15}$ $\cos 40 = 0$	2
B In the diagram above, QP is a tangent to the circle, while QRS is a secant. If QP = a units QR = b units and RS = c units. Write down an equation (do not prove this equation) showing the relationship between a, b and c.	$a^{2} = b (bec)$ $a^{2} = b^{2} + b c$ $a^{-1} \sqrt{b^{2} + b c}$	2







		<u> </u>	
	(i) Prove that $(a-b)^2 + (b-c)^2 + (c-a)^2 = 2(a^2+b^2+c^2-ab-bc-ca)$		
	(q2-2ab+b2) + (b2-2bc+c2)+(c2-2ca	2 (92 + 162 + 12 - 96 - 66 - (6))	
	(ii) Use part (i) to prove that $a^2 + b^2 + c^2 \ge ab + bc + ca$.	2 (42 +b2 +c2-45-bc-(4)	
		\ .	1
D			3
	(iii) Use part (ii) to prove that $(a+b+c)^2 \ge 3(ab+bc+ca).$		
	1, ,		
	(i) Without using a calculator, explain why $7^{\frac{1}{2}}$ is less than 3.	J7 ≈ < J9	
	, in less triates.	329 57=7	1
		[: 57 < 59	
Е	(ii) Use methods similar to part (i) to explain why $7^{\frac{1}{2}} + 7^{\frac{1}{3}} + 7^{\frac{1}{4}} < 7$. (Once again do not use a calculator.)	J7+57+57< J49	2
	$(3/7)^3 \times (3/43)$	7= >7= >7=	
	J343 < 343	J7 < 7 × (7) × (7) × (7) × (7)	1
	This is the end	7271	1

This is the end of the exam.