MARCELLIN COLLEGE RANDWICK



YEAR 11 ACCELERATED MATHEMATICS

HSC ASSESSMENT TASK 2 2016

STUDENT NAME		MARK	/33
TEACHER:			
TIME ALLOWED: WEIGHTING:	45 minutes 20 %		

Directions:

- Answer multiple choice questions on the page provided.
- Use a new sheet for each question.
- Show all necessary working. Where more than one mark is allocated to a question, full marks may not be awarded for answers only.
- Marks may not be awarded for careless or badly arranged work.
- · Calculators may be used

Section I Start each question on a new sheet of paper

Question 1 (16 marks)

		Marks
a)	Differentiate	
	i $\sin(\ln x)$	2
	ii) $x^2 \ln x$	2
b)	Find $\int \frac{x}{x^2-3} dx$	2
c)	Find $\int_0^{\frac{\pi}{4}} \sin 2x dx$	2
d)	Solve $2\cos\theta=-\sqrt{3}$ for $0\leq\theta\leq2\pi$	2
e}	Find the limiting sum of the series $1 - \frac{1}{3} + \frac{1}{9} - \frac{1}{27} + \cdots$	2
f)	A plant has a probability of $\frac{2}{7}$ of producing white flowers. If 3 plants are chosen at random, find the probability that	
	i) 2 plants will produce white flowers	1
	ii) At least 1 plant will produce white flowers	. 1
g)	Find the equation of the tangent to the curve $y = 2e^{2x}$ at the point where $x = 0$	2

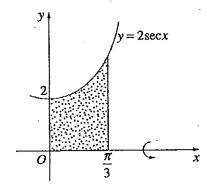
Question 2 (6 marks)

Start a new page

a) John is learning to drive. His first lesson is 30 minutes long. His second lesson is 35 minutes and each lesson thereafter is 5 minutes longer than the lesson before.

- i) How long with John's fifteenth lesson be?
- ii) How many hours will John have completed after his fifteenth lesson?
- b) In the diagram below, the shaded region is bound by the curve $y = 2 \sec x$, the x axis and the lines x = 0 and $x = \frac{\pi}{3}$.

The shaded region is rotated about the x – axis



Calculate the exact volume of the solid of revolution formed.

3

Marks

1

2

Question 3 (7 marks) Start a new page

		•	Marks
a)	A bag contains 10 marbles of which only two are black. Each trial involves drawing two marbles from the bag. The marbles are NOT replaced until the end of each trial.		3
		ny trials should one make so that the certainty of two black marbles in a trial at least once is greater %?	
bЭ	Frances	decides to set up a trust fund for her grandson Michael.	
D)	She inve	sts \$100 at the beginning of each month. The money is at 3% per annum, compounded monthly.	
	The trust fund matures at the end of the month of her final investment, 20 years after her first investment. This means the Betty makes 240 monthly investments.		·
	: i) ,	After 20 years, what will be the value of the first \$100 invested?	1 .
	ii)	By writing a geometric series for the value of all Frances' investments, calculate the final value of Michael's trust fund.	3
	•	•	

Section II – Multiple Choice (4 marks) Attempt all questions

Use the Multiple Choice Answer Sheet for Questions 4 to 7

- 4. Which of the following is the solution to $6^x = 5$?
- (A) $x = \frac{\ln x}{6}$

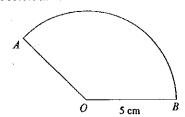
(B) $x = \frac{5}{\ln 6}$

(C) $x = \ln\left(\frac{5}{6}\right)$

- (D) $x = \frac{\ln s}{\ln 6}$
- 5. In a school the population of females is 45% and males 55%. If two students are chosen at random, what is the probability that they are both female
- (A) 0.2025
- (B) 0.2475
- C) 0.3025

 $c_{1}^{-1} \in \mathcal{C}_{1}$

- (D) 0.5555
- AOB is a sector of a circle, centre O and radius S cm. The sector has an area of 10π



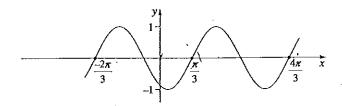
Not to scale

What is the arc length of the sector?

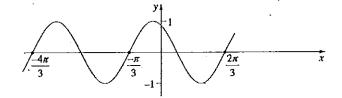
- (A) 2n
- B) 47
- C) 6π
- (D) 10π

7. Which diagram shows the graph $y = \sin\left(2x + \frac{\pi}{3}\right)$?

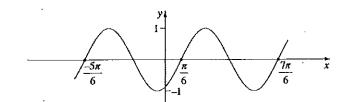
(A)



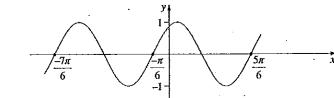
(B)



(C)



(D)



MARCELLIN YRII ACCELERATED MATHS 2016 ASSESSMENT ?

d). 21050=-13

b)
$$\int \frac{x}{x^2-3} dx$$

= $\frac{1}{2} \int \frac{2y}{x^2-3} dx$
= $\frac{1}{2} \ln (x^2-3.) + C$

y-2-4x=0

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3. lu mubles
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2 black

NO REPLACE

Chance of draing 2 black mortes = 10 x = 10

So to yourskie, we need 90x0.95-72 ie. 86 trials.

as tres to statistically governier that it will hoppen 100% In the certainly. but I right tike as in whe two bears the events are independent of each other.

6) [00x(140.03)260

1) 182.045

1: \\$ 32912.28 (2.d.p).

L let P= r= 1+ 0.03 = 1.0025

To = 100

T1 = 100+100 r

Tz= lost loor +loor?

In-larthout...tom.

where n= 240.

Sum of geometric series

a= 100 (1.002s)

n: 245.

= 100 1.0025 (141.002540)

1. 675 -1

=\$32912.28

Sedia I multiple choice.

4. 6×:5

In 16x)=1115)

X1a6 = 1a5

X=1,5=1,6 = D

6. Total circumference = 107.

Aren of South = 10TT.

Arm of Entire ande = 25.7

5, 10 = 2 x3600

- 1440.

Sure ratio for the circum ferene

So 10 TX X = 47 = 13.

7. Take ponts

>5- 21 X=0. 5 y= SN (3) = 53

So either Bor D.

-7. S.N D= S;N (2(-1/2)+1/3)

s. = 0.