

Student \_\_\_\_\_



**BRIGIDINE COLLEGE  
RANDWICK**

**HALF YEARLY**

**MATHEMATICS  
EXTENSION 1**

**- 2013 -**

**(TIME - 2 HOURS)**

*DIRECTIONS TO CANDIDATES*

- \* *Put your name at the top of this paper and on each of the 5 sections to be collected.*
- \* *All questions are to be attempted.*
- \* *All questions are to be answered on separate pages and will be collected in 5 separate bundles at the end of this exam.*
- \* *All necessary working should be shown in every question in PEN.*
- \* *Full marks may not be awarded for careless or badly arranged work*

**MULTIPLE CHOICE (PLACE ANSWERS ON THE ANSWER SHEET PROVIDED)**

1 What is the solution to the equation  $|2x-5|=x+2$ ?

- (A)  $x=1$
- (B)  $x=7$
- (C)  $x=1$  or  $x=7$
- (D)  $x=1$  and  $x=7$

2 What is the exact value of  $\tan(\theta-180)$ , if  $4\cos\theta=-3$  and  $\tan\theta>0$ ?

- (A)  $\frac{\sqrt{7}}{3}$
- (B)  $\frac{\sqrt{7}}{3}$
- (C)  $-\frac{3}{\sqrt{7}}$
- (D)  $\frac{3}{\sqrt{7}}$

3 Which of the following is equivalent to the expression  $\frac{\sin 2\theta + \sin \theta}{\cos 2\theta + \cos \theta + 1}$ ?

- (A)  $\cot \theta$
- (B)  $\sec \theta$
- (C)  $\sin \theta$
- (D)  $\tan \theta$

4 What is the acute angle to the nearest degree between the lines  $y=2x-1$  and  $x-3y+6=0$ ?

- (A)  $45^\circ$
- (B)  $54^\circ$
- (C)  $79^\circ$
- (D)  $82^\circ$

5 A parabola has the parametric equations  $x=12t$  and  $y=-6t^2$ .  
What are the coordinates of the focus?

- (A) (-6,0)
- (B) (0,-6)
- (C) (6,0)
- (D) (0,6)

6 How many arrangements of all of the letters of the word ~~TRIGONOMETRY~~ are possible?

- (A) 59 875 200
- (B) 119 750 400
- (C) 239 500 800
- (D) 479 001 600

7 It is known that two of the roots of the equation  $3x^3 + x^2 - kx + 6 = 0$  are reciprocals of each other. What is the value of  $k$ ?

- (A) -2
- (B) 6
- (C) 7
- (D) 17

8 Which of the following is an expression for  $\int \frac{e^{-2x}}{e^{-x}+1} dx$ ?

Use the substitution  $u = e^{-x} + 1$ .

- (A)  $\frac{(e^{-x}+1)^2}{2} - e^{-x} + c$
- (B)  $\frac{(e^{-x}+1)^2}{2} + e^{-x} + c$
- (C)  $\log_e(e^{-x}+1) - e^{-x} + c$
- (D)  $\log_e(e^{-x}+1) + e^{-x} + c$

9 Which of the following is an expression for  $\int \sin^2 6x dx$ ?

- (A)  $\frac{x}{2} - \frac{1}{24} \sin 6x + c$
- (B)  $\frac{x}{2} + \frac{1}{24} \sin 6x + c$
- (C)  $\frac{x}{2} - \frac{1}{24} \sin 12x + c$
- (D)  $\frac{x}{2} + \frac{1}{24} \sin 12x + c$

10 What is the derivative of  $y = \cos^{-1}\left(\frac{1}{x}\right)$  with respect to  $x$ ?

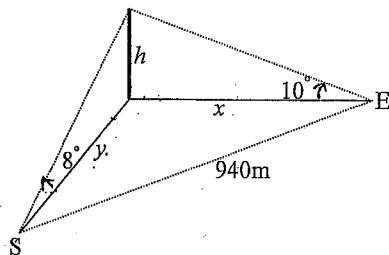
- (A)  $\frac{-1}{\sqrt{x^2-1}}$
- (B)  $\frac{-1}{x\sqrt{x^2-1}}$
- (C)  $\frac{1}{\sqrt{x^2-1}}$
- (D)  $\frac{1}{x\sqrt{x^2-1}}$

**End of Multiple Choice**

Question 11 (15 Marks) (Start a New Page)

Marks

- (a) Evaluate  $\int_0^3 \frac{1}{16+x^2} dx$  3
- (b) Differentiate  $2x^3 \tan x$  with respect to  $x$  2
- (c) The point  $(-6t, 9t^2)$ , where  $t$  is a variable, lies on a curve. Find the Cartesian equation of the curve. 2
- (d) Use the substitution  $u = x - 2$  to evaluate  $\int_3^4 \left( \frac{x}{\sqrt{x-2}} \right) dx$ . 3
- (e) A surveyor who is  $y$  metres south of a tower sees the top of it with an angle of elevation  $8^\circ$ . A second surveyor is  $x$  metres east of the tower. From his position the angle of elevation is  $10^\circ$  to the top of the tower. The two surveyors are 940m apart. 1
- (i) Show that  $y = h \cot 8^\circ$  1
- (ii) Find the height of the tower to the nearest metre. 4



Question 12 (15 Marks) (Start a New Page)

Marks

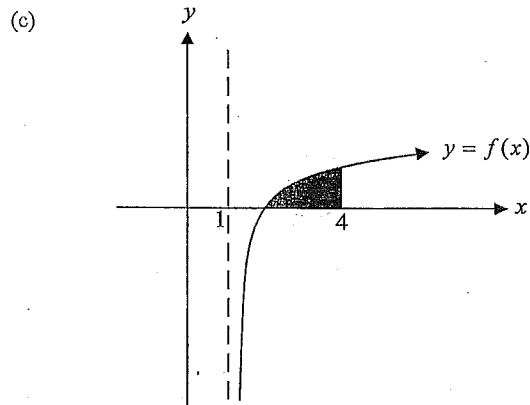
- (a) Evaluate  $\lim_{x \rightarrow 0} \frac{\sin 4x}{5x}$  1
- (b) The chord joining  $P(2ap, ap^2)$  and  $Q(2aq, aq^2)$  on the parabola  $x^2 = 4ay$  subtends a right angle at the vertex of the parabola. 2
- (i) Show that  $pq = -4$  2
- (ii) Show that the locus of the point  $M$ , the midpoint of  $PQ$ , is also a parabola and give its vertex. 2
- (c) (i) Prove the identity  $\frac{\sin 2\theta}{2 \sin \theta} - \cos \theta \cos 2\theta = 2 \cos \theta \sin^2 \theta$  2
- (ii) Hence solve the equation  $\frac{\sin 2\theta}{2 \sin \theta} - \cos \theta \cos 2\theta = \cos \theta$  for  $0 \leq \theta \leq 2\pi$ . 3
- (d) A particle moves in a straight line starting at the origin. At  $t$  seconds, the velocity of the particle is given by  $v = 2 \sin t - \sqrt{3}$ ,  $0 \leq t \leq 2\pi$ , where  $v$  is in metres per second. 1
- (i) When is the particle at rest? 2
- (ii) Find an expression for the acceleration  $a$ , of the particle a time  $t$ . 1
- (iii) Find the displacement of the particle  $x$ , in metres, when the particle is first at rest. 2

Question 13 (15 Marks) (Start a New Page)

Marks

(a) Use mathematical induction to prove that  $n^2 + 2n$  is divisible by 8 for even  $n \geq 2$ . 3

(b) Find the general solution to  $2\sqrt{3} \cos^2 \theta = \sin 2\theta$  4



The sketch shows the graph of the curve  $y = f(x)$  where  $f(x) = \ln(x-1)$ ,  $x > 1$ .

Copy or trace this diagram onto your page.

(i) Sketch the graph of the inverse function  $y = f^{-1}(x)$  on the same diagram. 2

(ii) Show that the inverse function is given by  $f^{-1}(x) = e^x + 1$ . 2

(iii) Hence find the area of the shaded region. 2

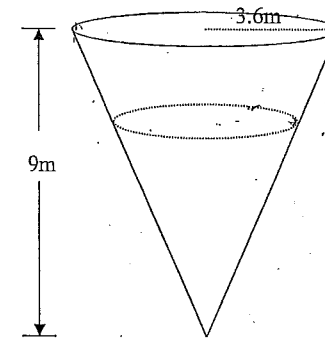
(d) The polynomial  $P(x) = x^3 + 5x^2 - cx + 2$  is exactly divisible by  $x - 2$ . Find the value of  $c$ . 2

Question 14 (15 Marks) (Start a New Page)

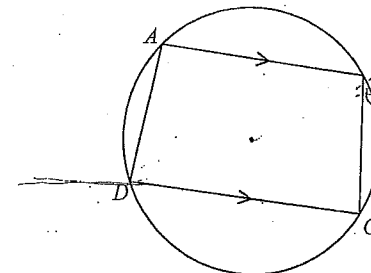
Marks

(a) The diagram shows a milk storage unit in the shape of an inverted cone with radius 3.6m and height 9m. 3

When the gate at the bottom is open, milk pours out at a rate equal to  $\frac{\sqrt{h}}{10} m^3 s^{-1}$ . At what rate is the height changing when  $h = 7.2m$ .



(b)



ABCD is a cyclic quadrilateral with  $AB \parallel DC$ .

(i) Prove  $\angle ADC = \angle BCD$  2

(ii) Hence, use congruent triangles to prove that any trapezium inscribed in a circle must be isosceles. (i.e. has its non-parallel sides equal in length) 3

**Question 14 continued**

**Marks**

(c) Let  $f(x) = \tan^{-1}\left(\frac{2}{x}\right) - \tan^{-1}(-2x)$  where  $x > 0$ .

(i) Find  $f'(x)$ . 2

(ii) Hence explain why the inverse function  $f^{-1}(x)$  does not exist. 3

(iii) Find the largest possible continuous domain for  $f(x)$  so that its inverse function  $f^{-1}(x)$  exists. 2

**End of Exam**

MULTIPLE CHOICE  
ANSWERS AT THE BACK

Question 7/1

$12+1=13$   
15

a)  $\int_0^3 \frac{1}{16+x^2} dx$

$= \left[ \frac{1}{4} \tan^{-1}\left(\frac{x}{4}\right) \right]_0^3$

$= \frac{1}{4} \tan^{-1}\left(\frac{3}{4}\right) - \frac{1}{4} \tan^{-1}\left(\frac{0}{4}\right)$

$= 0.16$  (to 2 d.p.)

Exact given

b)  $2x^3 \tan x$

$u = 2x^3 \quad v = \tan x$

$u' = 6x^2 \quad v' = \sec^2 x$

$\frac{dy}{dx} = 6x^2 \tan x + 2x^3 \sec^2 x$   
 $= 2x^2 (3 \tan x + x \sec^2 x)$

c)  $(-6t, 9t^2)$

$x = -6t \quad y = 9t^2$

$t = \frac{x}{-6}$

~~$y^2 = -49x$~~

$x = 2at \quad y = 9t^2$

$y = 9x \left(\frac{x}{-6}\right)^2$

$y = 9x \frac{x^2}{36 \cdot 4}$

$x^2 = 4y$

d)  $\int_3^4 \left( \frac{x}{\sqrt{x-2}} \right) dx$

let  $u = x-2$   
 $\frac{du}{dx} = 1$

$x = u+2$

when  $x=4$   $u=2$

$x=3$   $u=1$

good.

$\int_1^2 \frac{u+2}{\sqrt{u}} du$

$= \int_1^2 \frac{u}{\sqrt{u}} + \frac{2}{\sqrt{u}} du$

$= \int_1^2 \sqrt{u} + \frac{2}{\sqrt{u}} du = \left[ \frac{2}{3} \sqrt{u} + \frac{2 \cdot 2}{3/2} \sqrt{u} \right]_1^2 = \left[ \frac{2}{3} \sqrt{u} + 4\sqrt{u} \right]_1^2$   
 $= \left[ \left( \frac{2}{3} \sqrt{2} + 4\sqrt{2} \right) - \left( \frac{2}{3} + 4 \right) \right] = \frac{16}{3} \sqrt{2} - \frac{14}{3}$

Why?

$= -\frac{1}{2} \left[ \frac{u^{3/2}}{3/2} \right]_1^2 - \int_1^2 \frac{1}{\sqrt{u}} du$

$= -\frac{1}{2} \left[ \frac{2 \times 2^{3/2}}{3} - \frac{2 \times 1^{3/2}}{3} \right] - \left[ \frac{u^{1/2}}{1/2} \right]_1^2$  ✓ for subst

$= -\frac{1}{2} \left[ \frac{2}{3} \times 2\sqrt{2} - \frac{2}{3} \right] - \left[ \frac{2 \times 2^{1/2}}{1} - 2 \times 1 \right]$

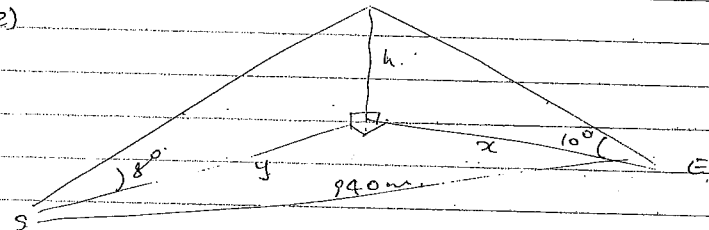
$= -\frac{1}{2} \left[ \frac{4\sqrt{2}}{3} - \frac{2}{3} \right] - 2\sqrt{2} + 2$

$= -\frac{2\sqrt{2}}{3} + \frac{1}{6} - 2\sqrt{2} + 2$

$= -\frac{8\sqrt{2}}{3} + \frac{13}{6}$

$= \frac{1}{6} \left( \frac{13}{2} - 8\sqrt{2} \right)$

e)



a)  $\tan 8^\circ = \frac{y}{940}$

$y = 940 \tan 8^\circ$

$y = h \cot 8^\circ$

b)  $\tan 10^\circ = \frac{h}{x}$

$x = h \cot 10^\circ$

$940^2 = x^2 + y^2$

$940^2 = h^2 \cot^2 10^\circ + h^2 \cot^2 8^\circ$

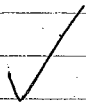
$h^2 = \frac{940^2}{\cot^2 10^\circ + \cot^2 8^\circ}$

$h = 103 \text{ m}$

14/15

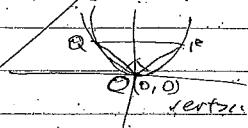
Question 12

a)  $\lim_{x \rightarrow 0} \frac{\sin 4x}{5x}$   
 $= \frac{4}{5} \lim_{x \rightarrow 0} \frac{\sin 4x}{4x}$   
 $= \frac{4}{5}$



b)  $P(2ap, ap^2)$   $Q(2aq, aq^2)$   $x^2 = 4ay$  right vertex

$x^2 = 4ay$   
 $y = \frac{x^2}{4a}$



$y' = \frac{x}{2a}$

at  $P(2ap, ap^2)$

similarly at  $Q$   $y' = q$

$y' = \frac{2ap}{2a}$

$= p$

eqn P to vertex

similarly at  $Q$  eqn

$y - ap^2 = p(x - 2ap)$

$y = qx - aq^2$

$y - aq^2 = px - 2ap^2$

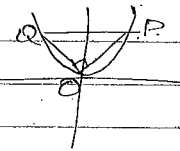
$y = px - ap^2$

$mp \times mq = -1$

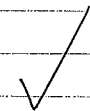
$pq = -1$

b)  $P(2ap, ap^2)$   $Q(2aq, aq^2)$   $x^2 = 4ay$

$x^2 = 4ay$   
 $y = \frac{x^2}{4a}$   
 $y' = \frac{x}{2a}$



i)  $M_{PQ} = \frac{aq^2 - ap^2}{2aq - 2ap} = \frac{q - p}{2}$



$M_{OP} = \frac{ap^2 - 0}{2ap - 0} = \frac{p}{2}$

$m_{PQ} \times m_{OP} = -1$  ← great 😊

$\frac{q-p}{2} \times \frac{p}{2} = -1$

$pq = -4$



ii)  $M \Rightarrow$  mid point of  $PQ$  vertex?

$M$  of  $PQ = \frac{2ap + 2aq}{2}, \frac{ap^2 + aq^2}{2}$

$= ap + aq, \frac{ap^2 + aq^2}{2}$

$= a(p+q), \frac{a}{2}(p^2 + q^2)$

$x = a(p+q) \quad y = \frac{a}{2}(p^2 + q^2)$

$\frac{x}{a} = p+q \quad y = \frac{a}{2}[(p+q)^2 - 2pq]$

$y = \frac{a}{2} \left[ \frac{x^2}{a^2} - 2(-4) \right]$

$y = \frac{a}{2} \left[ \frac{x^2}{a^2} + 8 \right]$

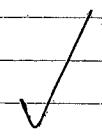
$y = \frac{x^2}{2a} + \frac{8a}{2}$

$y = \frac{x^2}{2a} + \frac{8a^2}{2a}$

$2ay = x^2 + 8a^2$

$x^2 = 2ay - 8a^2$

$x^2 = 2a(y - 4a)$  vertex  $(0, 4a)$



$$c) \text{ i. } \frac{\sin 2\theta}{2 \sin \theta} - \cos \theta \cos 2\theta = 2 \sin^2 \theta \cos \theta$$

$$\text{LHS: } \frac{\sin 2\theta}{2 \sin \theta} - \cos \theta \cos 2\theta$$

$$= \frac{2 \sin \theta \cos \theta}{2 \sin \theta} - \cos \theta (1 - 2 \sin^2 \theta)$$

$$= \cancel{\cos \theta} - \cancel{\cos \theta} + 2 \sin^2 \theta \cos \theta$$

$$\therefore = 2 \sin^2 \theta \cos \theta$$

$$= \text{RHS}$$

$$\text{ii. solve } 0 \leq \theta < 2\pi$$

$$\cancel{2 \sin^2 \theta \cos \theta} = \cos \theta$$

$$\ast \frac{\sin 2\theta}{2 \sin \theta} - \cos \theta \cos 2\theta = \cos \theta$$

$$2 \sin^2 \theta \cos \theta = \cos \theta$$

take out

$$\cos \theta (2 \sin^2 \theta - 1) = 0 \rightarrow \begin{matrix} 2 \sin^2 \theta = 1 & \times \\ \sin^2 \theta = \frac{1}{2} & 45^\circ \frac{\pi}{4} \\ \sin \theta = \pm \frac{1}{\sqrt{2}} \end{matrix}$$

$$\theta = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$$

$$d) v = 2 \sin t - \sqrt{3} \quad 0 \leq t \leq 2\pi \quad v = \text{m/s}$$

$$\text{i. } v = 0?$$

$$0 = 2 \sin t - \sqrt{3}$$

$$\frac{\sqrt{3}}{2} = \sin t$$

$$t = \frac{\pi}{3}, \frac{2\pi}{3}$$

$$\text{ii. } a = \int 2 \sin t - \sqrt{3} \, dt$$

=

$$\text{ii. } v = 2 \sin t - \sqrt{3}$$

$$v' = a$$

$$v' = 2 \cos t$$

$$a = 2 \cos t$$

$$\text{iii. displacement} = \int v$$

$$= \int 2 \sin t - \sqrt{3} \, dt$$

$$= -2 \cos t - \sqrt{3} t + c$$

$$t = 0 \quad s = 0$$

$$0 = -2 \cos(0) - 0 + c$$

$$0 = -2 + c$$

$$c = 2$$

$$s = -2 \cos t - \sqrt{3} t + 2$$

$$\text{when } t = \frac{\pi}{3}, \frac{2\pi}{3}$$

$$s = -2 \cos \frac{\pi}{3} - \sqrt{3} \frac{\pi}{3} + 2$$

$$= -1 - \frac{\pi}{3} \sqrt{3} + 2$$

$$= (1 - \frac{\pi}{3} \sqrt{3}) \text{ m}$$

$$s = -2 \cos \frac{2\pi}{3} - \sqrt{3} \times \frac{2\pi}{3} + 2$$

$$= 1 - 2\sqrt{3} \frac{\pi}{3} + 2$$

$$= 3 - \frac{2\sqrt{3}\pi}{3}$$

$$= 3 - \frac{2\sqrt{3}\pi}{3} \text{ m}$$



(13)(a) To prove  $n^2 + 2n$  is divisible by 8 for  $n \geq 2$  (for even 'n')

Step 1: Prove true for  $n=2$

$$2^2 + 2(2) = 8 \text{ which is divisible by } 8$$

$\therefore$  true for  $n=2$

Step 2:

Assume true for  $n=k$

i.e.  $k^2 + 2k = 8M$  (where  $M$  is an integer)

R.T.P. true for  $n=k+2$

i.e.  $(k+2)^2 + 2(k+2) = 8N$  (where  $N$  is another integer)

Proof

$$\text{LHS} = k^2 + 4k + 4 + 2k + 4$$

$$= (k^2 + 2k) + 4k + 8$$

$$= 8M + 8 + 4k$$

$$= 8(M+1) + 4(2L) \text{ since } k \text{ is even}$$

$$= 8(M+1+L)$$

$$= 8N \text{ which is divisible by } 8.$$

b)  $2\sqrt{3} \cos^2 \theta = \sin 2\theta$

$$2\sqrt{3} \cos^2 \theta = 2 \sin \theta \cos \theta$$

$$\frac{2\sqrt{3} \cos^2 \theta}{2} = \frac{2 \sin \theta \cos \theta}{2} \Rightarrow \sqrt{3} \cos \theta = \sin \theta$$

$$\frac{a}{\sqrt{a^2+b^2}} = \frac{2\sqrt{3}}{\sqrt{12+4}} = \frac{2\sqrt{3}}{\sqrt{16}} = \frac{2\sqrt{3}}{4} = \frac{\sqrt{3}}{2} = r$$

$$\frac{2\sqrt{3}}{4} = \frac{\sqrt{3}}{2} = r$$

$\therefore$  solution:

$$\frac{\sqrt{3}}{2} \sin\left(\frac{\pi}{6} - \theta\right)$$

$$2 \cos \theta = 0$$

$$\theta = \frac{\pi}{2} + 2n\pi$$

$$r = 2$$

$$\sqrt{3} \cos \theta = \sin \theta \Rightarrow \tan \theta = \frac{1}{\sqrt{3}}$$

$$\theta = \frac{\pi}{6} + 2n\pi$$

$$r \sin(\theta - \theta) = 2 \cos\left(\theta + \frac{\pi}{6}\right)$$

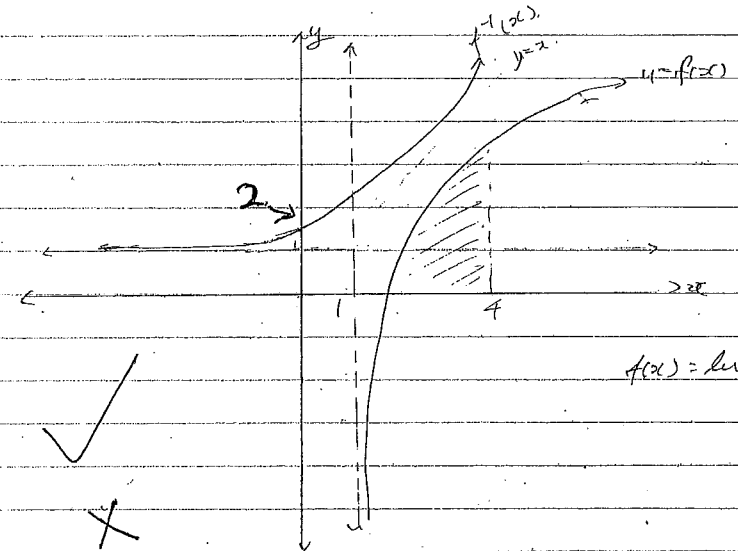
$$r \sin x \cos z - r \cos x \sin z = \sqrt{3} \cos \theta - \sin \theta$$

$$\tan \theta = \frac{1}{\sqrt{3}}$$

$$\tan \theta = \frac{1}{\sqrt{3}}$$

$$\theta = \frac{\pi}{6}$$

c)



$$\text{ii). } f^{-1}(0) = \ln(x-1) \quad x > 1$$

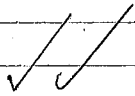
$$y = \ln(x-1)$$

$$x = \ln(y+1)$$

$$e^x = y+1$$

$$y = e^x - 1$$

$$\therefore f^{-1}(x) = e^x - 1$$



$$\text{iii). } y = \ln(x-1)$$

when  $x=0$ :

$$y = \ln(-1)$$

when  $y=0$ :  $x=2$

$$\int_2^4 \ln(x-1) \cdot dx$$

$$u = \ln(x-1) \quad v' = 1$$

$$u' = \frac{1}{x-1} \quad v = x$$

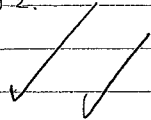
$$y = \left[ x \ln(x-1) \right]_2^4 - \int_2^4 \frac{x}{x-1} dx$$

$$= 4 \ln 3 - 2 \ln 1 - \int_2^4 \frac{x-1}{x-1} dx - \int_2^4 \frac{1}{x-1} dx$$

$$= 4 \ln 3 - [x-2] - [\ln(x-1)]_2^4$$

$$= 4 \ln 3 - 2 - [\ln 3 - \ln 1]$$

$$= 3 \ln 3 - 2 \quad u^2$$



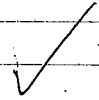
$$\text{d) } P(x) = x^3 + 5x^2 - cx + 2 \quad (x-2)$$

$$P(2) = 8 + 20 - 2c + 2$$

$$0 = 8 + 20 - 2c + 2$$

$$-30 = -2c$$

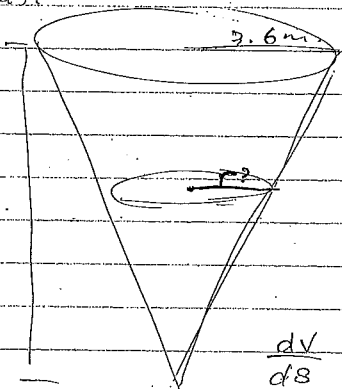
$$c = 15$$



Q14

7/15

a)



$$\frac{\sqrt{h}}{10} \text{ m}^3 \text{ s}^{-1} = \frac{dV}{ds}$$

$$h = 7.2 \text{ m}$$

?? rate h changing

$$V_{\text{cone}} = \frac{1}{3} \pi r^2 h$$

$$V = \frac{1}{3} \pi r^2 h$$

$$\frac{dV}{dh} = \frac{1}{3} \pi r^2$$

$$\frac{dV}{ds} = \frac{dV}{dh} \times \frac{dh}{ds}$$

$$\frac{\sqrt{h}}{10} = \frac{1}{3} \pi r^2 \times \frac{dh}{ds}$$

$$h = 7.2$$

$$r = 3.6$$

$$\frac{\sqrt{7.2}}{10} = \frac{1}{3} \pi (3.6)^2 \times \frac{dh}{ds}$$

$$\frac{r}{h} = \frac{3.6}{7.2} = \frac{2}{5}$$

$$r = \frac{2h}{5}$$

$$V = \frac{1}{3} \pi \frac{4h^3}{25}$$

$$\frac{dV}{ds} = \frac{dV}{dh} \times \frac{dh}{ds}$$

$$\frac{\sqrt{7.2}}{10} = \frac{1}{3} \pi \times \frac{4(7.2)^3}{25} \times \frac{dh}{ds}$$

$$\frac{dh}{ds} = \dots$$

b) i)  $\angle ADC = \angle BCD$

$$\angle ADB = \angle BCA$$

( $\angle$  subtended by same arc are equal)

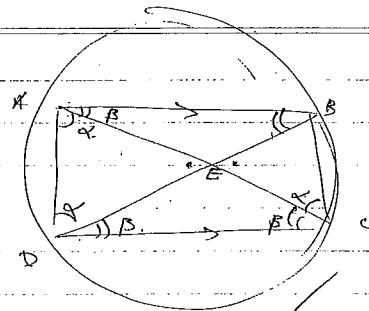
$$\angle ABD = \angle ACD$$

( $\angle$  subtended by same arc)

$$\angle ABD = \angle BDC$$

(alternate  $\angle$  in  $\parallel$  lines are equal)

$$\therefore \angle ADC = \angle BCD$$



ii)  $\angle ABC + \angle ACD = \angle BAC + \angle CAD$

(Opp.  $\angle$ s of cyclic quad are equal)

$$\therefore \text{let } \angle BCA = \alpha \quad \angle ACD = \beta$$

$$\angle BAC = \beta \quad \angle CAD = \alpha$$

$$\angle ADB = \angle BCA \text{ proven above (pt. i.)}$$

$$= \alpha$$

$$\angle CAD = \angle BCA = \alpha$$

$\therefore \triangle AED$  is an isosceles  $\triangle$

$$\angle AED = \angle BEC \text{ (vert opp. } \angle \text{ are equal)}$$

$$\angle BCA = \alpha = \angle ADE$$

(proven pt. i)

$$\therefore \triangle AED \cong \triangle BEC \text{ by AAA}$$

$$\therefore AD = BC$$

(chords subtending the same  $\angle$  are equal in length)

or matching sides of ~~isos~~ <sup>cong</sup>  $\triangle$  are equal

$\therefore$  any trapezium inscribed in a circle must be isosceles

Congruency !! equiangular !! NOT AAA !!

v)  $f(x) = \tan^{-1}\left(\frac{2}{x}\right) - \tan^{-1}(-2x) \quad x > 0.$

i)  $f'(x) = ?$

$$f'(x) = \frac{-\frac{2}{x^2}}{1 + \frac{4}{x^2}} - \left( \frac{-2}{1+4x^2} \right)$$

$$= \frac{-\frac{2}{x^2}}{\frac{x^2+4}{x^2}} + \frac{2}{1+4x^2}$$

$$= \frac{-2}{x^2+4} + \frac{2}{1+4x^2}$$

ii) since the denominator of both fractions are even functions. therefore  $f'(-x) = f'(x)$  and the domain of  $f(x)$  is only restricted for any values  $x > 0$ .  $\therefore$  graph  $(f(x))$  will not satisfy the horizontal line test.

iii)  $x \geq 1$

max. turning point. Does not pass horizontal test.

Multiple Choice Answer Sheet

Name: \_\_\_\_\_

Teacher: \_\_\_\_\_

Select Your Answers

1.	A	B	C	<input checked="" type="checkbox"/> D
2.	A	<input checked="" type="checkbox"/> B	C	D
3.	A	B	C	<input checked="" type="checkbox"/> D
4.	<input checked="" type="checkbox"/> A	B	C	D
5.	<input checked="" type="checkbox"/> A	<input checked="" type="checkbox"/> B	C	D
6.	<input checked="" type="checkbox"/> A	B	C	D
7.	A	<input checked="" type="checkbox"/> B	<input checked="" type="checkbox"/> C	D
8.	A	B	<input checked="" type="checkbox"/> C	D
9.	A	B	<input checked="" type="checkbox"/> C	D
10.	A	<input checked="" type="checkbox"/> B	C	<input checked="" type="checkbox"/> D

8/10