

# 13:02A | The Substitution Method

Name: \_\_\_\_\_ Class: \_\_\_\_\_

**Examples**Substitute one equation into the other, then solve for  $x$ , then for  $y$ .

1  $y = x - 1$  (A)

$x + 2y = 4$  (B)

Put (A) into (B).

$x + 2(x - 1) = 4$

$x + 2x - 2 = 4$

$3x = 6$

$\therefore x = 2$

Put  $x = 2$  in (A).

$y = 2 - 1$

$\therefore y = 1$

$\therefore x = 2, y = 1$

2  $y = 3x$  (A)

$2x - y = 2$  (B)

Put (A) into (B).

$2x - (3x) = 2$

$-x = 2$

$\therefore x = -2$

Put  $x = -2$  in (A).

$y = 3 \times -2$

$\therefore y = -6$

$\therefore x = -2, y = -6$

3  $y = 2x + 1$  (A)

$x + y = -2$  (B)

Put (A) into (B).

$x + (2x + 1) = -2$

$3x + 1 = -2$

$3x = -3$

$\therefore x = -1$

Put  $x = -1$  in (A).

$y = 2 \times -1 + 1$

$\therefore y = -1$

$\therefore x = -1, y = -1$

**Exercise**

1 Solve these equations.

a  $x + (x + 4) = 6$

b  $2x - (x + 3) = 5$

c  $4x + 2(x - 3) = 6$

d  $x - (2x - 1) = 4$

e  $3x - 2(x + 1) = 4$

f  $2x + (3x - 4) = 6$

g  $2x - 3(2x + 5) = -10$

h  $-x + 2(4x + 3) = -8$

2 a Substitute  $y = x + 2$  for  $y$  in the equation  $x + y = 10$ , and solve.b Substitute  $y = 2x$  for  $y$  in the equation  $x - y = 3$ , and solve.c Substitute  $y = 1 - x$  for  $y$  in the equation  $x - y = 3$ , and solve.d Substitute  $y = x + 2$  for  $y$  in the equation  $x - 2y = -1$ , and solve.e Substitute  $y = x - 1$  for  $y$  in the equation  $2x + y = 14$ , and solve.f Substitute  $y = -x$  for  $y$  in the equation  $x + 5y = 8$ , and solve.g Substitute  $y = 3 - x$  for  $y$  in the equation  $5x - 2y = 1$ , and solve.h Substitute  $y = 3x - 7$  for  $y$  in the equation  $4x + 3y = 5$ , and solve.i Substitute  $y = 2x + 8$  for  $y$  in the equation  $3x + 2y = 2$ , and solve.j Substitute  $y = 3x + 2$  for  $y$  in the equation  $2x - 3y = 8$ , and solve.3 Complete the solutions for Question 2 by solving for  $y$  also.

### 13:02A The Substitution Method

- |                                |            |            |            |                                |           |                      |            |
|--------------------------------|------------|------------|------------|--------------------------------|-----------|----------------------|------------|
| 1 a $x = 1$                    | b $x = 8$  | c $x = 2$  | d $x = -3$ | e $x = 6$                      | f $x = 2$ | g $x = -\frac{5}{4}$ | h $x = -2$ |
| 2 a $x + (x + 2) = 10, x = 4$  |            |            |            | b $x - 2x = 3, x = -3$         |           |                      |            |
| c $x - (1 - x) = 3, x = 2$     |            |            |            | d $x - 2(x + 2) = -1, x = -3$  |           |                      |            |
| e $2x + (x - 1) = 14, x = 5$   |            |            |            | f $x + 5(-x) = 8, x = -2$      |           |                      |            |
| g $5x - 2(3 - x) = 1, x = 1$   |            |            |            | h $4x + 3(3x - 7) = 5, x = 2$  |           |                      |            |
| i $3x + 2(2x + 8) = 2, x = -2$ |            |            |            | j $2x - 3(3x + 2) = 8, x = -2$ |           |                      |            |
| 3 a $y = 6$                    | b $y = -6$ | c $y = -1$ |            | d $y = -1$                     | e $y = 4$ | f $y = 2$            |            |
| g $y = 2$                      | h $y = -1$ | i $y = 4$  |            | j $y = -4$                     |           |                      |            |