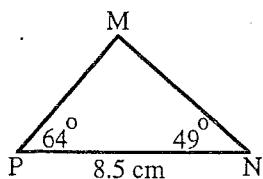
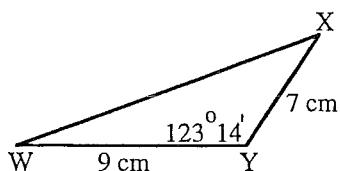


1.



Find the length of MP.
(correct to 3 significant figures)

2.



Find, correct to 1 decimal place:

- (a) the length of XW.
- (b) the area of triangle XYW.

3. In triangle RST, RS = 18 cm, ST = 20 cm and TR = 13 cm.

Find, to the nearest minute, the size of the largest angle of triangle RST.

4. In triangle PQR, QR = 15.3 cm, PQ = 7.8 cm and $\angle PRQ = 23^\circ 40'$.

Find, to the nearest minute, the size of $\angle RPQ$.

5. In parallelogram ABCD, AB = 19 cm, AD = 14 cm and $\angle BAD = 135^\circ$.

Find, in its simplest surd form, the exact value of the area of parallelogram ABCD.

6. The angle of elevation of the top of a tower D from a point A is 27° .

On walking 120 m towards the tower, the angle of elevation from a point B is 41° .

Given the points A and B are in line with the foot of the tower C:

- (a) draw a diagram to illustrate this information.
- (b) find, correct to 1 decimal place, the height of the tower.

7. A hiker starts from point P and walks 8 km on a bearing of $143^\circ T$ to point Q.

He then walks 12 km on a bearing of $292^\circ T$ to point R.

(a) Draw a diagram to illustrate this information.

(b) Find the distance of R from P.
(correct to 1 decimal place)

(c) Find the bearing of R from P.
(to the nearest degree)

*8. To find the height of an inaccessible tower, the elevation of its summit is observed from two points A and B which are on the same level as the foot of the tower.

From point A, due south of the tower, the angle of elevation is 26° and from point B, due east of the tower, the angle of elevation is 34° .

The distance between the points A and B is 200 metres.

- (a) Draw a diagram to illustrate this information.
- (b) Show that the height, h, of the tower is given by

$$h = \frac{200}{\sqrt{\cot^2 26^\circ + \cot^2 34^\circ}}.$$

(c) Hence find the height of the tower.
(to the nearest metre)

*9. A person walking along a straight horizontal road observes the summit of a tower on a bearing of $056^\circ T$, at an elevation of 13° .

After walking 1200 metres, the summit of the tower bears $312^\circ T$, at an elevation of 28° .

- (a) Draw a diagram to illustrate this information.
- (b) Show that the height, h, of the tower is given by

$$h = \frac{1200}{\sqrt{\cot^2 13^\circ + \cot^2 28^\circ - 2 \cot 13^\circ \cot 28^\circ \cos 104^\circ}}$$

(c) Hence find the height of the tower.
(to the nearest metre)

Solutions

Trigonometry Test 2.

11

$$\begin{aligned}\angle M &= 180^\circ - 64^\circ - 49^\circ \\ &= 67^\circ\end{aligned}$$

$$\frac{n}{\sin N} = \frac{m}{\sin M}$$

$$\frac{MP}{\sin 49^\circ} = \frac{8.5}{\sin 67^\circ}$$

$$MP = \frac{8.5}{\sin 67^\circ} \times \sin 49^\circ$$

$$MP = 6.97 \text{ cm } (\text{c.t. 3 sig figs})$$

$$\begin{aligned}y^2 &= x^2 + w^2 - 2xw \cos Y \\ xw^2 &= q^2 + t^2 - 2 \times q \times t \cos 123^\circ 14' \\ xw^2 &= 130 - 126 \cos 123^\circ 14' \\ w^2 &= 199.05 \quad (\text{c.t. 2 dec. pl.}) \\ xw &= \sqrt{199.05} \\ xw &= 14.1 \text{ cm } (\text{c.t. 1 dec. pl.})\end{aligned}$$

$$\begin{aligned}\text{area of } \triangle XYZ &= \frac{1}{2} \times w \times h \sin Y \\ &= \frac{1}{2} \times 9 \times 7 \times \sin 123^\circ 14' \\ &= 31.5 \sin 123^\circ 14' \\ &= 26.3 \text{ cm}^2 \quad (\text{c.t. 1 dec. pl.})\end{aligned}$$

largest angle is opposite the longest side

Largest angle is $\angle R$.

$$\cos R = \frac{s^2 + t^2 - r^2}{2st}$$

$$\begin{aligned}\cos R &= \frac{13^2 + 18^2 - 20^2}{2 \times 13 \times 18} \\ &= \frac{93}{468}\end{aligned}$$

$$\angle R = 78^\circ 32'$$

$$\frac{\sin P}{P} = \frac{\sin R}{r}$$

$$\frac{\sin P}{15.3} = \frac{\sin 23^\circ 40'}{7.8}$$

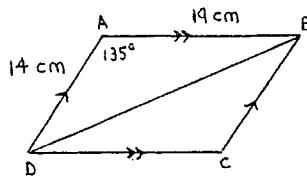
$$\sin P = 15.3 \times \frac{\sin 23^\circ 40'}{7.8}$$

$$\sin P = 0.787 \quad (\text{c.t. 3 dec. pl.})$$

$$\angle P = 51^\circ 57' \quad (180^\circ - 51^\circ 57')$$

$$\angle P = 51^\circ 57' \quad 128^\circ 3'$$

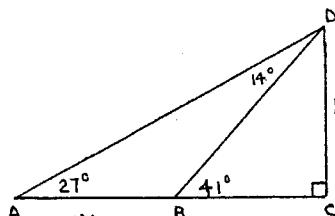
5/



$$\begin{aligned}\text{area of parallelogram ABCD} &= 2 \times \text{area of } \triangle BAD \\ &= 2 \times \frac{1}{2} bd \sin A \\ &= 2 \times \frac{1}{2} \times 14 \times 19 \times \sin 135^\circ \\ &= 266 \times \sin 45^\circ \\ &= 266 \times \frac{1}{\sqrt{2}} \\ &= \frac{266}{\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} \\ &= \frac{266\sqrt{2}}{2} \\ &= 133\sqrt{2} \text{ cm}^2\end{aligned}$$

6/

4/



$$\begin{aligned}\angle ADB &= 41^\circ - 27^\circ \\ &= 14^\circ\end{aligned}$$

b)

in $\triangle ADB$

$$\begin{aligned}\frac{a}{\sin A} &= \frac{d}{\sin D} \\ \frac{DB}{\sin 27^\circ} &= \frac{120}{\sin 14^\circ} \\ DB &= \frac{120 \sin 27^\circ}{\sin 14^\circ} \quad \text{--- ①}\end{aligned}$$

in $\triangle BDC$

$$\begin{aligned}\sin B &= \frac{DC}{DB} \\ \sin 41^\circ &= \frac{DC}{DB} \\ DC &= DB \sin 41^\circ \quad \text{--- ②}\end{aligned}$$

sub ① into ②

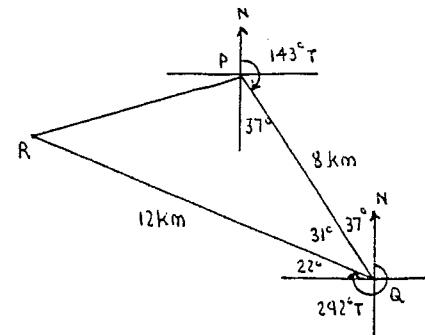
$$DC = \frac{120 \sin 27^\circ}{\sin 14^\circ} \times \sin 41^\circ$$

$$DC = 147.7 \quad (\text{c.t. 1 dec. pl.})$$

\therefore the height of the tower is 147.7 m.

7/

4/



$$\begin{aligned}\angle PQR &= 90^\circ - [(180^\circ - 143^\circ) + (292^\circ - 270^\circ)] \\ &= 90^\circ - [37^\circ + 22^\circ] \\ &= 90^\circ - 59^\circ \\ &= 31^\circ\end{aligned}$$

b)

$$\begin{aligned}q^2 &= p^2 + r^2 - 2pr \cos Q \\ PR^2 &= 12^2 + 8^2 - 2 \times 12 \times 8 \times \cos 31^\circ \\ PR^2 &= 208 - 192 \cos 31^\circ \\ PR^2 &= 43.42 \quad (\text{c.t. 2 dec. pl.}) \\ PR &= \sqrt{43.42} \\ PR &= 6.6 \text{ km } (\text{c.t. 1 dec. pl.})\end{aligned}$$

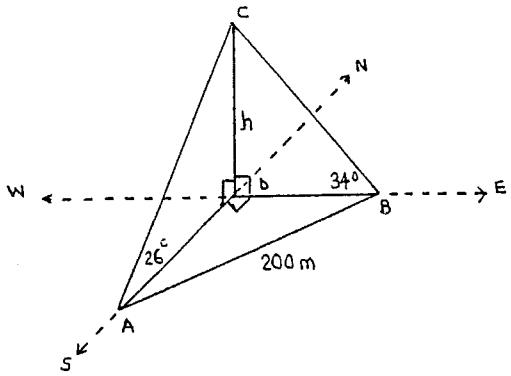
c)

$$\cos P = \frac{q^2 + r^2 - p^2}{2qr}$$

$$\begin{aligned}\cos P &= \frac{6.6^2 + 8^2 - 12^2}{2 \times 6.6 \times 8} \\ &= \frac{-36.44}{105.6}\end{aligned}$$

$$\angle P = 110^\circ \quad (\text{to nearest degree})$$

\therefore the bearing of R from P is $(143 + 110)^\circ T = 253^\circ T$



in $\triangle ACD$

$$\tan A = \frac{CD}{AD}$$

$$\tan 26^\circ = \frac{h}{AD}$$

$$AD = \frac{h}{\tan 26^\circ}$$

$$AD = h \cot 26^\circ$$

in $\triangle BCD$

$$\tan B = \frac{CD}{BD}$$

$$\tan 34^\circ = \frac{h}{BD}$$

$$BD = \frac{h}{\tan 34^\circ}$$

$$BD = h \cot 34^\circ$$

in $\triangle ADB$ (by Pythagoras)

$$AB^2 = AD^2 + BD^2$$

$$200^2 = (h \cot 26^\circ)^2 + (h \cot 34^\circ)^2$$

$$200^2 = h^2 (\cot^2 26^\circ + \cot^2 34^\circ)$$

$$h^2 = \frac{200^2}{\cot^2 26^\circ + \cot^2 34^\circ}$$

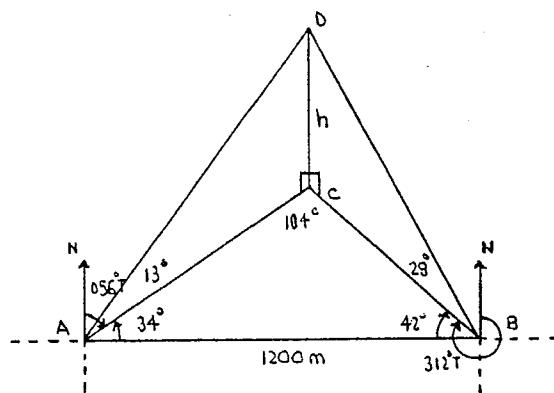
$$h = \sqrt{\cot^2 26^\circ + \cot^2 34^\circ}$$

$$h = 79 \text{ m} \quad (\text{to nearest metre})$$

\therefore tower is 79 m high

q)

a)



$$\angle ACB = 180^\circ - [(90^\circ - 56^\circ) + (312^\circ - 270^\circ)]$$

$$= 180^\circ - (34^\circ + 42^\circ)$$

$$= 104^\circ$$

b)

in $\triangle ADC$

$$\tan A = \frac{DC}{AC}$$

$$\tan 13^\circ = \frac{h}{AC}$$

$$AC = \frac{h}{\tan 13^\circ}$$

$$AC = h \cot 13^\circ$$

in $\triangle BDC$

$$\tan B = \frac{DC}{BC}$$

$$\tan 28^\circ = \frac{h}{BC}$$

$$BC = \frac{h}{\tan 28^\circ}$$

$$BC = h \cot 28^\circ$$

in $\triangle ACB$ (by the Cos Rule)

$$AB^2 = AC^2 + BC^2 - 2 \times AC \times BC \times \cos \angle ACB$$

$$1200^2 = (h \cot 13^\circ)^2 + (h \cot 28^\circ)^2 - 2 \times h \cot 13^\circ \times h \cot 28^\circ \times \cos 104^\circ$$

$$1200^2 = h^2 (\cot^2 13^\circ + \cot^2 28^\circ - 2 \cot 13^\circ \cot 28^\circ \cos 104^\circ)$$

$$h^2 = \frac{1200^2}{\cot^2 13^\circ + \cot^2 28^\circ - 2 \cot 13^\circ \cot 28^\circ \cos 104^\circ}$$

$$h = \sqrt{\frac{1200^2}{\cot^2 13^\circ + \cot^2 28^\circ - 2 \cot 13^\circ \cot 28^\circ \cos 104^\circ}}$$

c)

$$h = 234 \text{ m} \quad (\text{to nearest metre})$$

\therefore tower is 234 m high