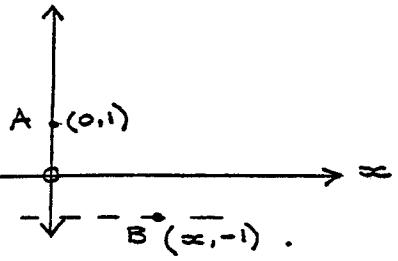


2 Unit Mathematics

LOCUS and the PARABOLA.

1. Find the equation of the point that moves so it is equidistant from the point $(0, 1)$ and the line $y = -1$.
2. Find the equation of the parabola that has focus $(1, 4)$ and directrix $x = 3$.
3. For the parabola $x^2 = 20y$, find:
 - a) the coordinates of the focus
 - b) the equation of its axis of symmetry
 - c) the equation of the directrix
 - d) its focal length
4. Find the co ordinates of the focus and the equation of the directrix of the parabola $y^2 = 10x$. Sketch the parabola, showing these two features.
5. Find the equation of the locus of the point moving so that it is equidistant from the point $(3, 5)$ and the line $y = -1$.
6. Find the coordinates of the vertex and the focus, and the equation of the directrix of the parabola with equation
$$x^2 - 10x - 16y - 7 = 0$$
.
7. Find the equation of the parabola with focus $(-2, 1)$ and vertex $(-2, -4)$.
8. Find the coordinates of the vertex and focus and the equation of the directrix for the parabola
$$y^2 + 6y - 4x - 11 = 0$$
Sketch the parabola, showing these features.

Solutions to Parabola and Locus Sheet.



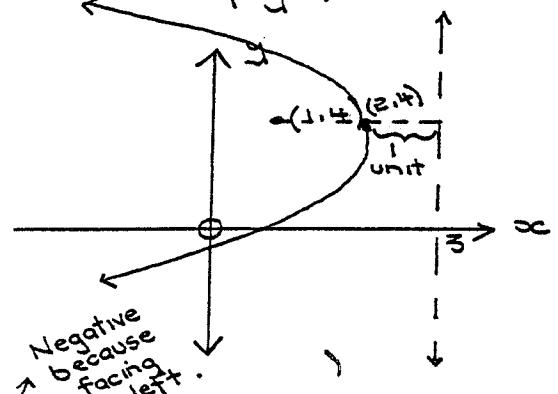
Let $P(x, y)$ be a point equidistant from $A(0, 1)$ and $B(x, -1)$ a point on the line $y = -1$.

$$AP = PB$$

$$\sqrt{x^2 + (y-1)^2} = \sqrt{(x-x)^2 + (y+1)^2}$$

$$x^2 + y^2 - 2y + 1 = y^2 + 2y + 1$$

$$\therefore x^2 = 4y$$



$$a = -1. \quad \text{Vertex } (2, 4)$$

$$(y - k)^2 = 4a(x - h)$$

$$(y - 4)^2 = -4(x - 2)$$

a) $4a = 20$
 $a = 5.$

$$(0, 5)$$

) $x = 0$

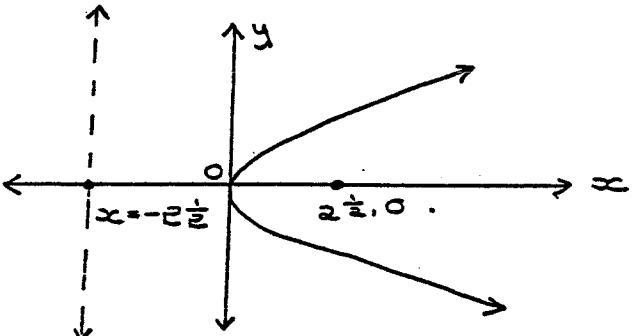
$$y = -5$$

) Focal length = 5

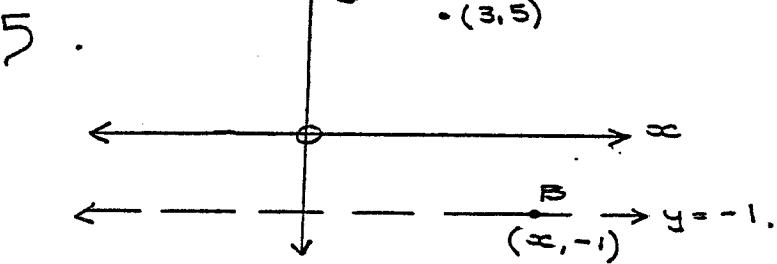
$$4. \quad 4a = 10$$

$$a = \frac{10}{4}$$

$$a = 2\frac{1}{2}.$$



$$\text{Directrix } x = -2\frac{1}{2}$$



Let $P(x, y)$ be a point equidistant from $A(3, 5)$ and $B(x, -1)$. Then $AP = BP$.

$$\sqrt{(x-3)^2 + (y-5)^2} = \sqrt{(x-x)^2 + (y+1)^2}$$

$$x^2 - 6x + 9 + y^2 - 10y + 25$$

$$= y^2 + 2y + 1.$$

$$x^2 - 6x + 9 = 12y - 24$$

$$(x-3)^2 = 12(y-2)$$

6. $x^2 - 10x - 16y - 7 = 0$.

$$x^2 - 10x = 16y + 7$$

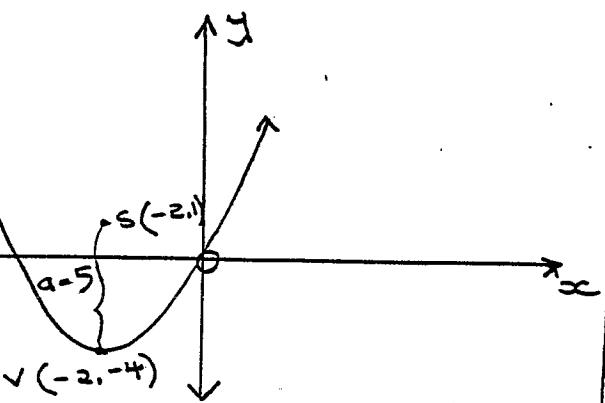
$$x^2 - 10x + 25 = 16y + 32$$

$$(x-5)^2 = 16(y+2)$$

Vertex = $(5, -2)$. Focal length = $\frac{16}{4} = 4$.

Focus $(5, 2)$ Directrix $y = -6$.

7.

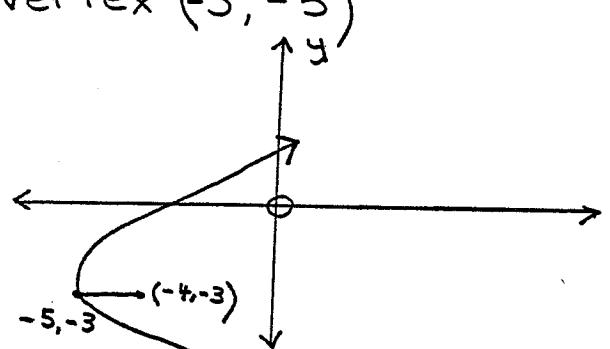


$$(x + 2)^2 = 20(y + 4)$$

$$\begin{aligned} y^2 + 6y &= 4x + 11 \\ y^2 + 6y + 9 &= 4x + 20 \\ (y + 3)^2 &= 4(x - 5) \end{aligned}$$

$$a = 1.$$

Vertex $(-5, -3)$



Focus $(-4, -3)$

Directrix $x = -6$