

# Exercise 1D

# ALGEBRAIC FRACTIONS EXERCISES :

1. Simplify:

(a)  $\frac{x}{2x}$

(c)  $\frac{3x^2}{9xy}$

(e)  $\frac{12xy^2z}{15x^2yz^2}$

(b)  $\frac{a}{a^2}$

(d)  $\frac{12ab}{4a^2b}$

(f)  $\frac{uvw^2}{u^3v^2w}$

2. Simplify:

(a)  $\frac{x}{3} \times \frac{3}{x}$

(d)  $\frac{a^2}{2b} \times \frac{b^2}{a^2}$

(g)  $\frac{5}{a} \div 10$

(j)  $\frac{2a}{3b} \times \frac{5c^2}{2a^2b} \times \frac{3b^2}{2c}$

(b)  $\frac{a}{4} \div \frac{a}{2}$

(e)  $\frac{3x^2}{4y^2} \times \frac{2y}{x}$

(h)  $\frac{2ab}{3c} \times \frac{c^2}{ab^2}$

(k)  $\frac{12x^2yz}{8xy^3} \times \frac{24xy^2}{36yz^2}$

(c)  $x \times \frac{3}{x^2}$

(f)  $\frac{x^2}{3ay^3} \div \frac{x^2}{3ay^3}$

(i)  $\frac{8a^3b}{5} \div \frac{4ab}{15}$

(l)  $\frac{3a^2b}{4b^3c} \times \frac{2c^2}{8a^3} \div \frac{6ac}{16b^2}$

3. Write as a single fraction:

(a)  $\frac{x}{2} + \frac{x}{5}$

(d)  $\frac{2a}{3} + \frac{3a}{2}$

(g)  $\frac{1}{x} + \frac{1}{2x}$

(j)  $x + \frac{1}{x}$

(b)  $\frac{a}{3} - \frac{a}{6}$

(e)  $\frac{7b}{10} - \frac{19b}{30}$

(h)  $\frac{3}{4x} + \frac{4}{3x}$

(k)  $a + \frac{b}{a}$

(c)  $\frac{x}{8} - \frac{y}{12}$

(f)  $\frac{xy}{30} - \frac{xy}{18}$

(i)  $\frac{1}{a} - \frac{1}{b}$

(l)  $\frac{1}{2x} - \frac{1}{x^2}$

4. Simplify:

(a)  $\frac{x+1}{2} + \frac{x+2}{3}$

(e)  $\frac{x-5}{3x} - \frac{x-3}{5x}$

(i)  $\frac{2}{x+3} - \frac{2}{x-2}$

(b)  $\frac{2x-1}{5} - \frac{x+3}{2}$

(f)  $\frac{1}{x} - \frac{1}{x+1}$

(j)  $\frac{x}{x+y} + \frac{y}{x-y}$

(c)  $\frac{2x+1}{3} - \frac{x-5}{6} + \frac{x+4}{4}$

(g)  $\frac{1}{x+1} - \frac{1}{x+1}$

(k)  $\frac{a}{x+a} - \frac{b}{x+b}$

(d)  $\frac{3x-7}{5} + \frac{4x+3}{2} - \frac{2x-5}{10}$

(h)  $\frac{2}{x-3} + \frac{3}{x-2}$

(l)  $\frac{x}{x-1} - \frac{x}{x+1}$

5. Factor where possible and then simplify:

(a)  $\frac{a}{ax+ay}$

(d)  $\frac{a^2-9}{a^2+a-12}$

(g)  $\frac{ac+ad+bc+bd}{a^2+ab}$

(b)  $\frac{3a^2-6ab}{2a^2b-4ab^2}$

(e)  $\frac{x^2+2xy+y^2}{x^2-y^2}$

(h)  $\frac{y^2-8y+15}{2y^2-5y-3}$

(c)  $\frac{x^2+2x}{x^2-4}$

(f)  $\frac{x^2+10x+25}{x^2+9x+20}$

(i)  $\frac{9ax+6bx-6ay-4by}{9x^2-4y^2}$

6. Simplify:

(a)  $\frac{3x+3}{2x} \times \frac{x^2}{x^2-1}$

(d)  $\frac{x^2-x-20}{x^2-25} \times \frac{x^2-x-2}{x^2+2x-8} \div \frac{x+1}{x^2+5x}$

(b)  $\frac{a^2+a-2}{a+2} \times \frac{a^2-3a}{a^2-4a+3}$

(e)  $\frac{ax+bx-2a-2b}{3x^2-5x-2} \times \frac{9x^2-1}{a^2+2ab+b^2}$

(c)  $\frac{c^2+5c+6}{c^2-16} \div \frac{c+3}{c-4}$

(f)  $\frac{2x^2+x-15}{x^2+3x-28} \div \frac{x^2+6x+9}{x^2-4x} \div \frac{6x^2-15x}{x^2-49}$

7. Simplify:

(a)  $\frac{1}{x^2+x} + \frac{1}{x^2-x}$

(d)  $\frac{3}{x^2+2x-8} - \frac{2}{x^2+x-6}$

(b)  $\frac{1}{x^2-4} + \frac{1}{x^2-4x+4}$

(e)  $\frac{x}{a^2-b^2} - \frac{x}{a^2+ab}$

(c)  $\frac{1}{x-y} + \frac{2x-y}{x^2-y^2}$

(f)  $\frac{1}{x^2-4x+3} + \frac{1}{x^2-5x+6} - \frac{1}{x^2-3x+2}$

8. Simplify:

(a)  $\frac{b-a}{a-b}$

(c)  $\frac{x^2 - 5x + 6}{2-x}$

(e)  $\frac{m}{m-n} + \frac{n}{n-m}$

(b)  $\frac{v^2 - u^2}{u-v}$

(d)  $\frac{1}{a-b} - \frac{1}{b-a}$

(f)  $\frac{x-y}{y^2 + xy - 2x^2}$

DEVELOPMENT

9. Study the worked exercise on compound fractions and then simplify:

(a)  $\frac{1 - \frac{1}{2}}{1 + \frac{1}{2}}$

(c)  $\frac{\frac{1}{2} - \frac{1}{5}}{1 + \frac{1}{10}}$

(e)  $\frac{\frac{1}{x}}{1 + \frac{2}{x}}$

(g)  $\frac{1}{\frac{1}{b} + \frac{1}{a}}$

(i)  $\frac{1 - \frac{1}{x+1}}{\frac{1}{x} + \frac{1}{x+1}}$

(b)  $\frac{2 + \frac{1}{3}}{5 - \frac{2}{3}}$

(d)  $\frac{\frac{17}{20} - \frac{3}{4}}{\frac{4}{5} - \frac{3}{10}}$

(f)  $\frac{t - \frac{1}{t}}{t + \frac{1}{t}}$

(h)  $\frac{\frac{x}{y} + \frac{y}{x}}{\frac{x}{y} - \frac{y}{x}}$

(j)  $\frac{\frac{3}{x+2} - \frac{2}{x+1}}{\frac{5}{x+2} - \frac{4}{x+1}}$

10. If  $x = \frac{1}{\lambda}$  and  $y = \frac{1}{1-x}$  and  $z = \frac{y}{y-1}$ , show that  $z = \lambda$ .

11. Simplify:

(a)  $\frac{x^4 - y^4}{x^2 - 2xy + y^2} \div \frac{x^2 + y^2}{x-y}$

(b)  $\frac{8x^2 + 14x + 3}{8x^2 - 10x + 3} \times \frac{12x^2 - 6x}{4x^2 + 5x + 1} \div \frac{18x^2 - 6x}{4x^2 + x - 3}$

(c)  $\frac{(a-b)^2 - c^2}{ab - b^2 - bc} \times \frac{c}{a^2 + ab - ac} \div \frac{ac - bc + c^2}{a^2 - (b-c)^2}$

(d)  $\frac{x-y}{x} + \frac{x^3 + y^3}{xy^2} - \frac{x^2 + y^2}{x^2}$

(e)  $\frac{x+4}{x-4} - \frac{x-4}{x+4}$

(f)  $\frac{4y}{x^2 + 2xy} - \frac{3x}{xy + 2y^2} + \frac{3x-2y}{xy}$

(g)  $\frac{8x}{x^2 + 5x + 6} - \frac{5x}{x^2 + 3x + 2} - \frac{3x}{x^2 + 4x + 3}$

(h)  $\frac{1}{x-1} + \frac{2}{x+1} - \frac{3x-2}{x^2-1} - \frac{1}{x^2+2x+1}$

12. (a) Expand  $\left(x + \frac{1}{x}\right)^2$ .

(b) Suppose that  $x + \frac{1}{x} = 3$ . Use part (a) to evaluate  $x^2 + \frac{1}{x^2}$  without attempting to find the value of  $x$ .

(ANSWERS)

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1(a)  $\frac{1}{2}$  (b)  $\frac{1}{a}$  (c)  $\frac{x}{3y}$  (d)  $\frac{3}{a}$  (e)  $\frac{4y}{5xz}$  (f)  $\frac{w}{u^2v}$

2(a) 1 (b)  $\frac{1}{2}$  (c)  $\frac{3}{x}$  (d)  $\frac{b}{2}$  (e)  $\frac{3x}{2y}$  (f) 1 (g)  $\frac{1}{2a}$

(h)  $\frac{2c}{3b}$  (i)  $6a^2$  (j)  $\frac{5c}{2a}$  (k)  $\frac{x^2}{yz}$  (l)  $\frac{1}{2a^2}$

3(a)  $\frac{7x}{10}$  (b)  $\frac{a}{6}$  (c)  $\frac{3x-2y}{24}$  (d)  $\frac{13a}{6}$  (e)  $\frac{b}{15}$  (f)  $-\frac{xy}{45}$

(g)  $\frac{3}{2x}$  (h)  $\frac{25}{12x}$  (i)  $\frac{b-a}{ab}$  (j)  $\frac{x^2+1}{x}$  (k)  $\frac{a^2+b}{a}$  (l)  $\frac{x-2}{2x^2}$

4(a)  $\frac{5x+7}{6}$  (b)  $\frac{-x-17}{10}$  (c)  $\frac{9x+26}{12}$  (d)  $\frac{12x+3}{5}$

(e)  $\frac{2x-16}{15x}$  (f)  $\frac{1}{x(x+1)}$  (g)  $\frac{2x}{x^2-1}$  (h)  $\frac{5x-13}{(x-2)(x-3)}$

(i)  $\frac{-10}{(x+3)(x-2)}$  (j)  $\frac{x^2+y^2}{x^2-y^2}$  (k)  $\frac{ax-bx}{(x+a)(x+b)}$  (l)  $\frac{2x}{x^2-1}$

5(a)  $\frac{1}{x+y}$  (b)  $\frac{3}{2b}$  (c)  $\frac{x}{x-2}$  (d)  $\frac{a+3}{a+4}$  (e)  $\frac{x+y}{x-y}$

(f)  $\frac{x+5}{x+4}$  (g)  $\frac{c+d}{a}$  (h)  $\frac{y-5}{2y+1}$  (i)  $\frac{3a+2b}{3a+2y}$

6(a)  $\frac{3x}{2(x-1)}$  (b)  $a$  (c)  $\frac{c+2}{c+4}$  (d)  $x$  (e)  $\frac{3x-1}{a+b}$  (f)  $\frac{x-7}{3(x+3)}$

7(a)  $\frac{2}{x^2-1}$  (b)  $\frac{2x}{(x-2)^2(x+2)}$  (c)  $\frac{3x}{x^2-y^2}$

(d)  $\frac{x+1}{(x-2)(x+3)(x+4)}$  (e)  $\frac{bx}{a(a-b)(a+b)}$

(f)  $\frac{x}{(x-1)(x-2)(x-3)}$

8(a) -1 (b)  $-u-v$  (c)  $3-x$  (d)  $\frac{2}{a-b}$  (e) 1

(f)  $\frac{-1}{2x+y}$

9(a)  $\frac{1}{3}$  (b)  $\frac{7}{13}$  (c)  $\frac{3}{11}$  (d)  $\frac{1}{5}$  (e)  $\frac{1}{x+2}$  (f)  $\frac{t^2-1}{t^2+1}$

(g)  $\frac{ab}{a+b}$  (h)  $\frac{x^2+y^2}{x^2-y^2}$  (i)  $\frac{x^2}{2x+1}$  (j)  $\frac{x-1}{x-3}$

11(a)  $x+y$  (b)  $\frac{2x+3}{3x-1}$  (c)  $\frac{a-b+c}{ab}$  (d)  $\frac{x^4-y^4}{x^2y^2}$  (e)  $\frac{16x}{x^2-16}$

(f)  $\frac{4}{x+2y}$  (g)  $\frac{-13x}{(x+1)(x+2)(x+3)}$  (h)  $\frac{2}{(x+1)^2(x-1)}$

12(a)  $x^2 + 2 + \frac{1}{x^2}$  (b) 7