

# CHAPTER 1

## Geometrical applications of differentiation



### The sign of the derivative (1)

**QUESTION 1** Determine whether  $f'(2)$  is positive or negative:

**a**  $f(x) = x^2 - 7x$

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**b**  $f(x) = x^3 - 7x + 5$

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**c**  $f(x) = 9 - 3x - x^2$

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**QUESTION 2** Determine whether the curve is increasing or decreasing at the given point:

**a**  $y = x^4 - x^3$  at  $(1, 0)$

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**b**  $y = 8x^2 + 11x - 4$  at  $(-2, 6)$

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**c**  $y = -\frac{3}{x}$  at  $(3, -1)$

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**QUESTION 3** For what values of  $x$  is the curve  $y = f(x)$  increasing?

**a**  $y = 7x + 4$

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**b**  $y = x^2 + 8x - 5$

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**c**  $y = 4x^3 - 1$

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# Geometrical applications of differentiation

## The sign of the derivative (2)

QUESTION 1 For what value of  $x$  is the curve  $y = f(x)$  decreasing?

a  $y = x^2 - 6x + 1$

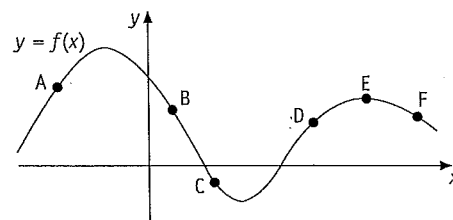
b  $y = x^3 - 12x + 5$

c  $y = 2x^3 + 3$

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QUESTION 2 For the curve  $y = f(x)$  indicate whether  $f'(x)$  will be positive, negative or zero at each of the points:

- a A \_\_\_\_\_
- b B \_\_\_\_\_
- c C \_\_\_\_\_
- d D \_\_\_\_\_
- e E \_\_\_\_\_
- f F \_\_\_\_\_



QUESTION 3 Show that the curve:

a  $y = 2x^3 + 6x - 2$  is always increasing

b  $y = x^5$  never decreases

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