

Present all necessary working in a neat and logical manner.

1. Evaluate the following:

(a)  $6 + 4 \div -2$

(b)  $-8 - (4 - 2 \times -1) - 3$

(c)  $-0.3 \times -0.2$

2. Simplify the following expressions.

(a)  $2\frac{7}{10} + 1\frac{4}{30} - 1\frac{3}{4}$

(b)  $1\frac{1}{5} \times 2\frac{7}{8}$

(c)  $\frac{7}{10} \div \frac{3}{5}$

3. Evaluate the following:

(a)  $34.65 - 2.006$

(b)  $1.4 \div 0.5$

(c)  $(0.6)^2 + 0.4 \times 0.025$

4. Convert the following to a percentages:

(a) 0.003

(b)  $1\frac{2}{9}$

5. Convert the following to fractions in their simplest form:

(a) 0.05%

(b) 15.5%

6. (a) If 15% of a class of 40 girls were absent, how many girls were absent?

(b) On a monorail journey that lasts one hour Joshua sleeps for 12% of the time. How long does he sleep? (Answer to the nearest second.)

7. Harry invested \$1200 for 3 years earning 9.6% simple interest per annum.

Calculate:

(i) The simple interest earned.

(ii) His total savings at the end of 3 years.

8. The students below gained the following marks in a Maths paper which was marked out of a total of 48. Express each mark as a percentage.

(a) Eli: 42

(b) Sean : 30.

9. (a) Decrease 340 ml by 15%.

(b) Hanson buys a computer game for \$84 then sells it to Arjun for \$105. Calculate his percentage profit on the cost price.

10. Find 100% given that:

(a)  $16\% = \$128$

(b)  $124\% = 806 \text{ km}$

11. An amount  $x$  is decreased by 12%. This amount is then increased by 6% to obtain \$400. Find  $x$ .

12. Guang pays 40% deposit on the purchase of a Harley Davidson Motor Cycle with a cost price of \$10 000. His monthly repayments for five years are \$140. Calculate the simple interest rate p.a. charged on the loan.

13. Evaluate

(a)  ~~$\frac{3}{4} + \frac{2}{3} + \frac{1}{2}$~~   
 ~~$\frac{3}{8} + \frac{1}{3} - \frac{1}{4}$~~

(b)  $\frac{1}{a} + \frac{1}{b}$  given  $a = \frac{3}{4}$  and  $b = \frac{2}{3}$ .

(c)  $2 - (1 - (2 - (1 - (2 - (1 - (2))))))$

14. If each edge of a cube is increased by 60%, find the percentage increase in surface area.

15. A motor car manufacturer makes  $m$  cars per week. If the production is increased by  $n\%$  write down an expression that gives the number  $N$  of cars made each week.

2B - RATIONALS AND PERCENTAGES

1. (a)  $6 + 4 \div -2 = 6 + -2$   
 $= 4$  ✓

(b)  $-8 - (4 - 2 \times -1) - 3 = -8 - (4 + 2) - 3$   
 $= -8 - 6 - 3$   
 $= -14 - 3$  ✓  
 $= -17$

(c)  $-0.3 \times -0.2 = 0.06$  ✓

2. (a)  $2 \frac{7}{10} + 1 \frac{4}{30} - 1 \frac{3}{4} = 2 \frac{42 + 8 - 45}{60}$  ✓  
 $= 2 \frac{5}{60}$   
 $= 2 \frac{1}{12}$  ✓

(b)  $1 \frac{1}{5} \times 2 \frac{7}{8} = \overset{3}{\cancel{6}} \frac{1}{5} \times \frac{23}{\cancel{8} 4}$   
 $= \frac{69}{20}$  ✓  
 $= 3 \frac{9}{20}$

(c)  $\frac{7}{10} \div \frac{3}{5} = \frac{7}{\cancel{10} 2} \times \frac{5}{3}$   
 $= \frac{7}{6}$  ✓  
 $= 1 \frac{1}{6}$

3. (a)  $34.65 - 2.006 = 32.644$

$$\begin{array}{r} 34.650 \\ - 2.006 \\ \hline 32.644 \end{array}$$

(b)  $1.4 \div 0.5 = 14 \div 5$   
 $= 2 \frac{4}{5}$  ✓

(c)  $(0.6)^2 + 0.4 \times 0.025 = 0.36 + 0.01$   
 $= 0.37$  ✓

4. (a)  $0.003 = 0.3\%$  ✓

(b)  $1\frac{2}{9} = 1.222\dots$   
 $= 122.2\%$  ✓

OR  $\frac{11}{9} \times \frac{100}{1}\% = \frac{1100}{9}\%$  ✓

5. (a)  $0.05\% = \frac{0.05}{100}$

$= \frac{5}{10000}$

$= \frac{1}{2000}$  ✓

(b)  $15.5\% = \frac{15.5}{100}$

$= \frac{31}{200}$  ✓

6. Girls absent =  $15\% \times 40$   
 $= \frac{3}{20} \times 40$   
 $= 6$  ✓

6(b)  
 later

432 seconds  
 OR 7min 12 seconds ✓

so 6 girls were absent from class.

7. (i)  $I = PRN$

Interest =  $\$1200 \times \frac{9.6}{100} \times 3$  ✓

$= \$36 \times 9.6$

$= \$345.60$  ✓

(ii) Total savings =  $\$1200 + \$345.60$   
 $= \$1545.60$  ✓

8. (a) Eli's mark =  $\frac{42}{48} \times \frac{100}{1}\%$

$= \frac{7}{8} \times \frac{100}{1}\%$

$= 87\frac{1}{2}\%$  ✓

(b) Sean's mark =  $\frac{30}{48} \times \frac{100}{1}\%$

$= \frac{5}{8} \times \frac{100}{1}\%$

$= 62\frac{1}{2}\%$  ✓

$$\begin{aligned}
 9. \quad (a) \quad 340 \text{ ml} \times 85\% &= 340 \text{ ml} \times \frac{17}{20} \\
 &= 17 \times 17 \text{ ml} \\
 &= 289 \text{ ml} \quad \checkmark
 \end{aligned}$$

$$\begin{aligned}
 (b) \quad \text{Profit} &= \$105 - \$84 \\
 &= \$21 \quad \checkmark
 \end{aligned}$$

$$\begin{aligned}
 \text{Percentage Profit} &= \frac{21}{84} \times \frac{100}{1} \% \\
 &= 25\% \quad \checkmark
 \end{aligned}$$

$$\begin{aligned}
 10. \quad (a) \quad 16\% \text{ of amount} &= \$128 \\
 4\% \text{ of amount} &= \$32 \\
 100\% \text{ of amount} &= \$32 \times 25 \\
 &= \$800 \quad \checkmark
 \end{aligned}$$

$$\begin{aligned}
 (b) \quad 124\% \text{ of distance} &= 806 \text{ km} \\
 2\% \text{ of distance} &= \frac{806}{62} \text{ km} \\
 &= 13 \text{ km}
 \end{aligned}$$

$$\begin{aligned}
 100\% \text{ of distance} &= 13 \times 50 \\
 &= 650 \text{ km} \quad \checkmark
 \end{aligned}$$

$$11. \quad 106\% \times 88\% \times x = \$400 \quad \checkmark$$

$$x = \frac{\$400}{1.06 \times 0.88} \quad \checkmark$$

$$x = \$428.82 \quad (\text{nearest c}) \quad \checkmark$$

NASTY NUMBERS !!

$$\begin{aligned}
 6. \quad (b) \quad \text{length of sleep} &= 12\% \times 60 \times 60 \\
 &= \frac{12}{100} \times 3600 \\
 &= 12 \times 36 \\
 &= 432 \text{ seconds} \quad \checkmark
 \end{aligned}$$

$$12. \text{ Deposit} = 40\% \times \$10000 \\ = \$4000$$

$$\text{Repayments} = 5 \times 12 \times \$140 \\ = \$8400$$

$$\therefore \text{Loan} = \$6000 \quad \checkmark$$

$$I = PRN$$

$$2400 = 6000 \times R \times 5$$

$$R = \frac{2400}{5 \times 6000} \quad \checkmark$$

$$R = \frac{2}{25} \quad \checkmark$$

so the simple interest rate on the loan is 8% p.a.

$$13. (a) \quad \frac{\frac{3}{4} + \frac{2}{3} + \frac{1}{2}}{\frac{3}{8} + \frac{1}{3} - \frac{1}{4}} = \frac{\frac{9+8+6}{12}}{\frac{9+8-6}{24}}$$

$$= \frac{23}{12} \times \frac{24}{11}^2$$

$$= \frac{46}{11}$$

$$= 4 \frac{2}{11}$$

$$(b) \quad \frac{1}{a} + \frac{1}{b} = \frac{1}{\frac{3}{4}} + \frac{1}{\frac{2}{3}}$$

$$= \frac{4}{3} + \frac{3}{2} \quad \checkmark$$

$$= \frac{8+9}{6} \quad \checkmark$$

$$= 2 \frac{5}{6}$$

$$(c) \quad 2 - (1 - (2 - (1 - (2 - (1 - (2)))))) = 2 - (1 - (2 - (1 - (2 - (-1)))))$$

$$= 2 - (1 - (2 - (1 - 3)))$$

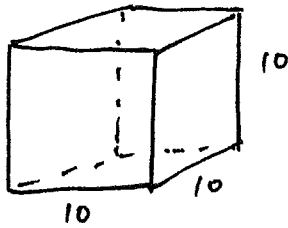
$$= 2 - (1 - (2 + 2))$$

$$= 2 - (-3)$$

$$= 5 \quad \checkmark$$

6

14. Let the side length of the cube be 10 units



$$\text{Surface area} = 6 \times 100 \text{ units}^2$$

$$\begin{aligned} \text{New side length} &= 160\% \times 10 \\ &= 16 \text{ units} \end{aligned} \quad \checkmark$$

$$\begin{aligned} \text{New surface area} &= 6 \times 16 \times 16 \\ &= 6 \times 256 \text{ units}^2 \end{aligned} \quad \checkmark$$

$$\begin{aligned} \text{Increase in S.A.} &= 6 \times 256 - 6 \times 100 \\ &= 6 \times 156 \text{ units}^2 \end{aligned}$$

$$\begin{aligned} \text{Percentage increase} &= \frac{6 \times 156}{6 \times 100} \times 100\% \\ \text{in surface area} &= 156\% \end{aligned} \quad \checkmark$$

3

15.  $N = m \left(1 + \frac{n}{100}\right)$

TOTAL

*Mad.*

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