

Topic 7: Exercises on Graphing
Level 2, Part 1

1. For $n \geq 2$, an even positive integer, sketch the graphs of: a) $y = x^n$; b) $y = x^{-n}$.

- a) The minimum turning point is $(0, 0)$.
- b) $x = 0$ is a vertical asymptote; $y=0$ is a horizontal asymptote.

2. For $n \geq 2$, an even positive integer, sketch the graphs of: a) $y = x^{1/n}$; b) $y = x^{-1/n}$.

b) $x = 0$ is a vertical asymptote; $y=0$ is a horizontal asymptote

3. For $n \geq 3$, an odd positive integer, sketch the graphs of: a) $y = x^n$; b) $y = x^{-n}$.

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| <p>a) Point of inflexion at $(0,0)$
b) $x=0$ is a vertical asymptote; $y=0$ is a horizontal asymptote</p> |
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4. For $n \geq 3$, an odd positive integer, sketch the graphs of: a) $y = x^{1/n}$; b) $y = x^{-1/n}$.

a) $(0, 0)$ is a critical point.
b) $x=0$ is a vertical asymptote; $y=0$ is a horizontal asymptote.

5. Sketch (showing critical points) the graph of $y = x(2 + \sqrt{x})$.

6. Sketch (showing critical points) the graph of $y = x + |x|$.

7. Sketch (showing critical points) the graph of $y = |x| - |x - 2|$.

8. Use the graph of $f(x) = 4 - x^2$ (an even function) to sketch (showing critical points) the graph of $y = |f(x)|$.

9. Use the graph $y = x(x + 2)$ to sketch showing critical points the graph of $y = |x(x + 2)|$.

10. Sketch the graph of $|x| + |y| = 1$.

11. Use the graph of $y = \cos x$ to sketch the graph of $y = \cos(x - \frac{\pi}{2})$.

12. Use the graph of $y = \sin^{-1} x$ to sketch the graph of: $y = \sin^{-1} x - \frac{\pi}{2}$.