

**Topic 7: Exercises on Graphing**  
**Level 3, Part 2**

1. Sketch the graph of  $y = \frac{\cos x - \sin x}{\cos x + \sin x}$ .

2. Use the graph of  $y = x^2 - 1$  to sketch the graph of  $y = (x^2 - 1)^2$ .

3. Use the graph of  $y = \cos x$  to sketch the graph of  $y = (\cos x)^2$ .

4. Use the graph of  $y = 3x - \frac{x^3}{4}$  to sketch the graph of  $y = \left(3x - \frac{x^3}{4}\right)^3$

5. For the function  $f(x) = 3x - \frac{x^3}{4}$  use the graph of  $y = f(x)$  to sketch the graphs of  
a)  $y = \sqrt{f(x)}$ , b)  $y^2 = f(x)$ .

6. For the function  $f(x) = 4 \sin x$  use the graph  $y = f(x)$  to sketch the graphs of  
a)  $y = \sqrt{f(x)}$ , b)  $y^2 = f(x)$ .

7. Use the graphs of  $y = \ln u$  and  $u = \sin x$  ( $0 \leq x \leq 2\pi$ ) to sketch the graph of  $y = \ln(\sin x)$  ( $0 \leq x \leq 2\pi$ ).

8. Sketch (showing critical points and stationary points) the graph of  $x^3 + y^3 = 1$ .

9. Sketch (showing critical points and stationary points) the graph of  $x^2 + y^2 + xy = 3$ .

10. Find the equation of the tangent to the curve  $xy(x + y) + 16 = 0$  at the point on the curve where the gradient is  $-1$ .

$$y + x + 4 = 0$$

11. Sketch the graph of  $y = \frac{x^2 + 1}{x^2 - 1}$ . Use this graph to solve the inequality  $\frac{x^2 + 1}{x^2 - 1} < 1$ .

$$-1 < x < 1$$