

**Topic 21: Exercises on Resisted Motion**

**Level 1**

1. A particle of mass  $m$  falls from rest under gravity and the resistance to its motion is  $mkv^2$ , where  $v$  is its speed and  $k$  is a positive constant. Show that  $v^2 = \frac{g}{k}(1 - e^{-2kx})$ , where  $x$  is the distance fallen.

2. A particle of mass  $m$  is projected vertically upward under gravity in a medium in which the resistance is  $mk$  times the square of the speed, where  $k$  is a positive constant. The speed of projection is  $V$ . Find the maximum height.

$$\frac{1}{2k} \ln \left| 1 + \frac{k}{g} V^2 \right|$$

3. A particle of mass  $0.5 \text{ kg}$  is released from rest and moves vertically downward under gravity in a medium which exerts a resistance to the motion of  $\frac{1}{10}v^2$ . At time  $t$  after release it has fallen a distance  $x$  and has velocity  $v$ . Taking  $g = 10 \text{ ms}^{-2}$ , show that  $v^2 = 50(1 - e^{-0.4x})$  and  $\ddot{x} = 10e^{-0.4x}$ .

4. A particle of mass  $1 \text{ kg}$  is projected vertically upward under gravity with speed  $2c$  in a medium in which the resistance to motion is  $\frac{g}{c^2}$  times the square of the speed, where  $c$  is a positive constant. Find the time of ascent of the particle and the maximum height.

$$\frac{c \cdot \tan^{-1} 2}{g}; \frac{c^2}{2g} \ln 5$$

5.