



## Mini Test 21: Fractions and Percentages

- 1 Which is halfway between  $2\frac{1}{5}$  and  $2\frac{1}{3}$ ?  
A 2    B  $2\frac{1}{4}$     C  $2\frac{4}{15}$     D  $2\frac{1}{2}$
- 2 A packet of mixed sweets is made up of jellies, butterscotch and mints.  $\frac{2}{5}$  of the sweets are jellies and  $\frac{1}{4}$  are mints. What fraction of the sweets is butterscotch?  
A  $\frac{1}{3}$     B  $\frac{7}{20}$     C  $\frac{2}{3}$     D  $\frac{3}{10}$
- 3 There are 240 pets at a pet motel. One-quarter of the pets are cats and the rest are dogs. 30% of the dogs are Labradors. How many Labradors are at the pet motel?  
A 18    B 36    C 54    D 72
- 4 Which set of fractions is arranged from lowest to highest?  
A  $\frac{2}{3}, \frac{3}{4}, \frac{4}{5}, \frac{5}{6}, \frac{7}{10}$     B  $\frac{2}{3}, \frac{7}{10}, \frac{3}{4}, \frac{4}{5}, \frac{5}{6}$   
C  $\frac{7}{10}, \frac{4}{5}, \frac{5}{6}, \frac{2}{3}, \frac{3}{4}$     D  $\frac{7}{10}, \frac{2}{3}, \frac{3}{4}, \frac{4}{5}, \frac{5}{6}$
- 5  $1\frac{2}{3} \times \frac{4}{5} = ?$   
A  $1\frac{8}{15}$     B  $2\frac{7}{15}$     C  $2\frac{1}{5}$     D  $1\frac{1}{3}$
- 6 Which fraction is not equal to  $\frac{2}{5}$ ?  
A  $\frac{4}{25}$     B  $\frac{12}{30}$     C  $\frac{16}{40}$     D  $\frac{28}{70}$
- 7 Leo asked 200 people which of four sports they preferred to watch on television. The table shows the results.
- | Sport  | Cricket | Swimming | Netball | Football |
|--------|---------|----------|---------|----------|
| Number | 39      | 51       | 42      |          |
- What percentage preferred football?  %
- 8 Which has the same value as  $\frac{13}{4}$ ?  
A  $3\frac{1}{4}$     B  $3\frac{3}{4}$     C  $4\frac{1}{4}$     D  $4\frac{3}{4}$
- 9 15% of all students received top marks in an exam.  $\frac{2}{3}$  of all students who achieved top marks were girls. If 180 students sat for the exam, how many girls got top marks?
- 10 Last week Dave's cows produced 25 000 litres of milk. This week they produced 25 500 litres. What percentage increase is this?  
A 2%    B 5%    C 12.5%    D 20%
- 11 A club has 320 members. 50 of the members are in the club today. The fraction of members who are in the club today is closest to  
A  $\frac{1}{3}$     B  $\frac{1}{4}$     C  $\frac{1}{5}$     D  $\frac{1}{6}$
- 12  $\frac{2}{3}$  of a number is 24. What is  $\frac{3}{4}$  of the number?
- 13 In 1983, Cameron celebrated his twenty-first birthday. On the same day, his niece Amy was also celebrating her birthday. Amy was  $\frac{1}{3}$  of Cameron's age. On their birthday in 2011, what fraction of Cameron's age is Amy?  
A  $\frac{1}{3}$     B  $\frac{4}{5}$     C  $\frac{2}{3}$     D  $\frac{5}{7}$
- 14 Which number is the largest?  
A  $\frac{1}{3}$     B  $\frac{3}{8}$     C  $\frac{5}{12}$     D  $\frac{7}{24}$
- 15  $15 \div \frac{1}{3} = ?$   
A 5    B 10    C 30    D 45
- 16 A recipe for Anzac biscuits uses  $\frac{3}{4}$  cup of coconut. This recipe makes three dozen biscuits. Georgia wants to make four dozen biscuits. How many cups of coconut should she use?  
A 1    B  $1\frac{1}{4}$     C  $1\frac{3}{4}$     D 3

# Mini Test 21: Fractions and

## Percentages

1 C 2 B 3 C 4 B 5 D 6 A 7 34% 8 A 9 18  
10 A 11 D 12 27 13 D 14 C 15 D 16 A

- 1 [Write both fractions with a common denominator (15).]

$$2\frac{1}{5} = 2\frac{3}{15}$$

$$2\frac{1}{3} = 2\frac{5}{15}$$

Now the number halfway between  $2\frac{3}{15}$  and

$$2\frac{5}{15} \text{ is } 2\frac{4}{15}.$$

So the number halfway between  $2\frac{1}{5}$  and  $2\frac{1}{3}$  is

$$2\frac{4}{15}.$$

- 2  $\frac{2}{5}$  are jellies and  $\frac{1}{4}$  are mints.

$$\begin{aligned} \text{Fraction of jellies and mints} &= \frac{2}{5} + \frac{1}{4} \\ &= \frac{8}{20} + \frac{5}{20} \\ &= \frac{13}{20} \end{aligned}$$

$$\begin{aligned} \text{Remainder} &= 1 - \frac{13}{20} \\ &= \frac{7}{20} \end{aligned}$$

The fraction of the sweets that are butterscotch is  $\frac{7}{20}$ .

- 3  $\frac{1}{4}$  of the pets are cats.

$$\begin{aligned} \text{Number of cats} &= 240 \div 4 \\ &= 60 \end{aligned}$$

$$\begin{aligned} \text{Number of dogs} &= 240 - 60 \\ &= 180 \end{aligned}$$

$$\begin{aligned} \text{Number of Labradors} &= 30\% \text{ of } 180 \\ &= \frac{3}{10} \text{ of } 180 \\ &= 54 \end{aligned}$$

- 4 Each set of fractions has denominators 3, 4, 5, 6 and 10.

The common denominator is 60.

$$\frac{2}{3} = \frac{40}{60}$$

$$\frac{3}{4} = \frac{45}{60}$$

$$\frac{4}{5} = \frac{48}{60}$$

$$\frac{5}{6} = \frac{50}{60}$$

$$\frac{7}{10} = \frac{42}{60}$$

$$\frac{10}{10} = \frac{60}{60}$$

So, in order, from lowest to highest, the

fractions are  $\frac{40}{60}, \frac{42}{60}, \frac{45}{60}, \frac{48}{60}, \frac{50}{60}$ .

The set of fractions that is in order is

$$\frac{2}{3}, \frac{7}{10}, \frac{3}{4}, \frac{4}{5}, \frac{5}{6}.$$

$$5 \quad 1\frac{2}{3} \times \frac{4}{5} = \frac{5}{3} \times \frac{4}{5}$$

$$= \frac{4}{3} \quad \left[ \frac{1\cancel{8}}{3} \times \frac{4}{\cancel{5}1} \right]$$

$$= 1\frac{1}{3}$$

- 6 Consider each option:

$\frac{4}{25}$  cannot be simplified.

$$\frac{12}{30} = \frac{2}{5} \quad (\text{after dividing both numerator and denominator by } 6)$$

$$\frac{16}{40} = \frac{2}{5} \quad (\text{after dividing both numerator and denominator by } 8)$$

$$\frac{28}{70} = \frac{2}{5} \quad (\text{after dividing both numerator and denominator by } 14)$$

The fraction that is not equal to  $\frac{2}{5}$  is  $\frac{4}{25}$ .

- 7 Total people = 200

Sport	Cricket	Swimming	Netball	Football
Number	39	51	42	

$$\begin{aligned} \text{Number in table} &= 39 + 51 + 42 \\ &= 132 \end{aligned}$$

$$\begin{aligned} \text{Number who preferred football} &= 200 - 132 \\ &= 68 \end{aligned}$$

$$\begin{aligned} \text{Fraction who preferred football} &= \frac{68}{200} \\ &= \frac{34}{100} \end{aligned}$$

So 34% of the people preferred to watch football.

$$8 \quad \frac{13}{4} = 3\frac{1}{4}$$

[4 divides into 13 three times with remainder one.]

- 9 Number who received top marks is 15% of 180.

$$\text{Now } 10\% \text{ of } 180 = 18$$

$$\text{So } 5\% \text{ of } 180 = 9$$

$$\begin{aligned} \text{and } 15\% \text{ of } 180 &= 18 + 9 \\ &= 27 \end{aligned}$$

$$\begin{aligned} \text{Number of girls} &= \frac{2}{3} \text{ of } 27 \\ &= 18 \end{aligned}$$

[Or  $\frac{2}{3}$  of 15% are girls who received top marks.

Now  $\frac{2}{3}$  of 15 is 10, so the number of girls who received top marks is 10% of 180 or 18.]

- 10 Increase = 25 500 - 25 000  
= 500

$$\% \text{ increase} = \frac{500}{25000} \times 100\%$$

$$= \frac{5}{250} \times 100\%$$

$$= \frac{1}{50} \times 100\%$$

$$= 2\%$$

$$11 \text{ Fraction} = \frac{50}{320}$$

$$= \frac{5}{32}$$

Now  $\frac{1}{3}$  is  $\frac{5}{15}$ ,  $\frac{1}{4}$  is  $\frac{5}{20}$ ,  $\frac{1}{5}$  is  $\frac{5}{25}$  and  $\frac{1}{6}$  is  $\frac{5}{30}$ .

So, of the options, the fraction is closest to  $\frac{1}{6}$ .

[Or, for each option, find the fraction of 320.

$\frac{1}{3}$  of 320 is more than 100.

$\frac{1}{4}$  of 320 is 80.

$\frac{1}{5}$  of 320 is 64.

$\frac{1}{6}$  of 320 is about 53.]

$$12 \frac{2}{3} \text{ of a number is 24.}$$

$\frac{1}{3}$  of the number is  $24 \div 2$  or 12.

The number is  $12 \times 3$  or 36.

Now  $\frac{3}{4}$  of 36 is 27.

So  $\frac{3}{4}$  of the number is 27.

13 In 1983, Cameron was 21.

Amy's age in 1983 =  $\frac{1}{3}$  of 21 = 7

Years later =  $2011 - 1983 = 28$

Cameron's age in 2011 =  $21 + 28$   
= 49

Amy's age in 2011 =  $7 + 28$   
= 35

Fraction of Cameron's age =  $\frac{35}{49}$   
=  $\frac{5}{7}$

14 [Change each fraction to an equivalent fraction with a common denominator (24).]

$$\frac{1}{3} = \frac{8}{24}$$

$$\frac{3}{8} = \frac{9}{24}$$

$$\frac{5}{12} = \frac{10}{24}$$

$$\frac{7}{24}$$

The largest fraction is  $\frac{10}{24}$  or  $\frac{5}{12}$ .

$$15 \ 15 \div \frac{1}{3} = 15 \times 3$$

$$= 45$$

$$16 \text{ Cups of coconut for 3 dozen} = \frac{3}{4}$$

$$\text{Cups of coconut for 1 dozen} = \frac{3}{4} \div 3$$

$$= \frac{1}{4}$$

$$\text{Cups of coconut for 4 dozen} = \frac{1}{4} \times 4$$

$$= 1$$

Georgia should use 1 cup of coconut.