

1996

# MATHEMATICS

3/4 UNIT

*Time allowed - two hours  
(Plus 5 minutes reading time)*

## DIRECTIONS TO CANDIDATES

- \* Student Number to be clearly written on the top of your front page.
- \* All questions may be attempted.
- \* Show all necessary working.
- \* Staple ALL questions together.

### QUESTION 1:

i) Solve  $\frac{2x+1}{x-2} \geq 1$  for  $x$  and graph the solution.

ii) Evaluate  $\int_0^{\frac{\pi}{2}} \frac{\sin x \, dx}{\sqrt{4 - \cos^2 x}}$  using  $u = \cos x$

iii) Solve for  $x$   

$$\left(x + \frac{1}{x}\right)^2 - 10\left(x + \frac{1}{x}\right) + 24 = 0$$

iv) Differentiate  $\tan^{-1}(\log_e x)$

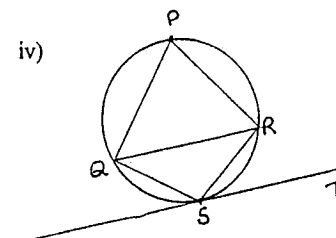
v) Write down the 3rd term in  
 $(3a - 2b)^4$

### QUESTION 2: (Start a new page)

i) Sketch  $y = 2 \cos^{-1} \frac{x}{3}$

ii) Solve for  $\theta$   $3 \sin \theta + 4 \cos \theta = 3$   $0 \leq \theta \leq 2\pi$  (Correct to 2dp.)

iii) The point  $P(6, 9)$  divides the interval  $AB$  in the ratio  $-3 : 2$ . Find the point  $B$  given that  $A$  is  $(1, 4)$



ST is a tangent to the circle, and  
 $QR \parallel ST$ . Copy the diagram and prove that

- $\alpha$ )  $SQ = SR$
- $\beta$ )  $SP$  bisects  $\widehat{QPR}$

QUESTION 3: (Start a new page)

- i) If the probability of a hit in a single run is 0.1. Calculate the probability of a jet fighter getting exactly 2 hits on a target in 20 runs at the target.
- ii) a) Show that the equation  

$$2x^3 - 3x^2 + 0.99 = 0$$
 has a root near  $x = 1$ .
- b) Attempt to find an improved value of this root by using Newton's Method once, starting with  $x_0 = 1$ .
- c) Explain why this attempt fails.
- iii) The polynomial  $2x^3 + 3x^2 + ax - 6$  has  $(x + 3)$  and  $(2x + b)$  as factors.  
 Find 'a' and 'b'

QUESTION 4: (Start a new page)

- i) By using the principle of mathematical induction prove

$$\sum_{k=1}^n s^k = s \left( \frac{s^n - 1}{s - 1} \right)$$

- ii) a) What is a primitive function of  $e^{f(x)} \cdot f'(x)$ ?

- b) Using part (a) evaluate  $\int_0^1 \frac{e^{\cos^{-1}x} dx}{\sqrt{1-x^2}}$  (leave answer in irrational form)

- iii) Two points  $P(2ap, ap^2)$  and  $Q(2aq, aq^2)$  lie on the parabola  $x^2 = 4ay$

- (a) Find the equation of the tangent  $l$  to the parabola at  $Q$ .
- (b) Derive the equation of the chord  $PQ$  and show that  $pq = -1$  when  $PQ$  is focal chord.
- (c) Find the acute angle between the tangent  $l$  and the chord  $PQ$   
 If  $p = 3$  and  $q = -0.2$ .

QUESTION 5 (Start a new page)

- i) The velocity of a particle moving in S.H.M. in a straight line is given by

$$v^2 = 4x - x^2 \text{ ms}^{-1} \text{ where } x \text{ is displacement in } m$$

- a) Find the two points between which the particle is oscillating.
- b) Find the centre of the motion.
- c) Find the maximum speed of the particle.
- d) Find the acceleration of the particle in terms of  $x$ .

- ii) Prove the identity  $\frac{2 \cos A}{\operatorname{cosec} A - 2 \sin A} = \tan 2A$

- iii) A person walking along a straight road observes a tower bearing  $045^\circ T$ , the angle of elevation being  $5^\circ$ . After travelling a distance of 5000m, the tower bears  $315^\circ T$  and the angle of elevation is  $8^\circ$ .

- a) Find the height of the tower (to 0.1m).

- b) Determine the angle which the road makes with a line bearing  $090^\circ T$ .

QUESTION 6: (Start a new page)

i) a) Sketch the curves  $y^2 = x$  and  $x^2 = 8y$

b) Show that the area formed between these curves is given by

$$\int_0^4 \left( x^{\frac{1}{2}} - \frac{x^2}{8} \right) dx$$

c) The area is rotated about the  $x$  axis, find the volume of the solid of revolution so formed.

ii) Let  $f(x) = \sin^{-1} x + \cos^{-1} x$  ( $0 \leq x \leq 1$ )

Find a)  $f'(x)$

$$\int_0^1 f(x) dx$$

iii) Newton's Law of cooling states that the rate at which a body cools is proportional to the excess of its temperature above that of its surroundings.

A sphere at a temperature of  $70^\circ\text{C}$  is placed in a container at a temperature of  $20^\circ\text{C}$ .

a) Show that  $T = 20 + 50 e^{-kt}$  is a solution of the differential equation

$$\frac{dT}{dt} = -K(T - 20) \text{ where } K \text{ is a positive constant.}$$

b) If, after 2 minutes, the temperature of the sphere is  $60^\circ\text{C}$  approx.. show that

$$T = 20 + 50 e^{-0.11t}$$

c) Find the temperature of the sphere after 4 minutes (to the nearest degree).

QUESTION 7 (Start a new page)

i) A ball is thrown from a height 1 metre from the ground and is caught, without bouncing, 2 seconds later at a distance of 50m, also at a height of 1m. Assuming no air resistance and that gravity is approx.  $10\text{ms}^{-2}$  you may assume  $x = Vt \cos \theta$  and  $y = -\frac{1}{2}gt^2 + Vt \sin \theta$

Find a) The velocity and angle of projection of the ball.

b) The maximum height of the ball above the ground during its flight.

ii) For the expansion of  $(a + bx)^n$  in ascending powers of  $x$

a) Show that the expression for the ratio of the  $r^{\text{th}}$  and  $(r + 1)^{\text{th}}$  terms

is  $\frac{T_{r+1}}{T_r} = \frac{(n - r + 1)}{r} \cdot \frac{bx}{a}$

b) Two consecutive coefficients in the expansion  $(3 + x)^{15}$  are equal. Find which terms these are.

Q1.

(a)  $\frac{2x+1}{x-2} \geq 1$

$\frac{2x+1}{x-2} - 1 \geq 0$

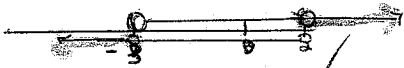
$2x+1 - x + 2 \geq 0$

$x \neq 2$

$\frac{x+3}{x-2} \geq 0$

$x+3 \geq 0 \cap x-2 \geq 0$   
 $x \geq -3 \cap x \geq 2$   
 $x \geq 2$

$x+3 \leq 0 \cap x-2 < 0$   
 $x \leq -3 \cap x < 2$   
 $x \leq -3$



$x \geq 2 \cup x \leq -3$

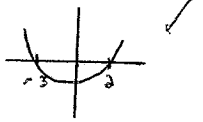
DP

$(2x+1)(x-2) \geq (x-2)^2$

$2x^2 - 3x - 2 \geq x^2 - 4x + 4$

$x^2 + x - 6 \geq 0$

$(x+3)(x-2) \geq 0$



$x \geq 2 \cup x \leq -3$

(ii)  $\int_0^{\pi/2} \frac{\sin x \cos x}{\sqrt{4-\cos^2 x}}$

Let  $u = \cos x$

$\frac{du}{dx} = -\sin x$

when  $x = \pi/2$ ,  $u = 0$   
 when  $x = 0$ ,  $u = 1$

$I = \int_1^0 \frac{-du}{\sqrt{4-u^2}}$   
 $= \int_0^1 \frac{du}{\sqrt{4-u^2}}$   
 $= [\sin^{-1}(\frac{u}{2})]_0^1$   
 $= \sin^{-1}(\frac{1}{2})$   
 $= \frac{\pi}{6}$

(iii)  $(x + \frac{1}{x})^2 - 10(x + \frac{1}{x}) + 24 = 0$

Let  $u = (x + \frac{1}{x})$

$(u-4)(u-6) = 0$

$u = 4$  or  $u = 6$

$x^2 + 4x + 1 = 0$

$x = \frac{-4 \pm \sqrt{16-4}}{2}$   
 $= \frac{-4 \pm \sqrt{12}}{2}$   
 $= -2 \pm \sqrt{3}$

$x^2 - 6x + 1 = 0$

$x = \frac{6 \pm \sqrt{36-4}}{2}$   
 $= \frac{6 \pm \sqrt{32}}{2}$   
 $= 3 \pm 2\sqrt{2}$

(iv)  $\tan^{-1}(\ln x)$

$f(u) = \ln x$

$f'(u) = \frac{1}{x}$

$\frac{d}{dx} (\tan^{-1}(\ln x)) = \frac{1}{x(1+(\ln x)^2)}$

Q1 (cont)

(v)  $(3a-2b)^4$

$T_3 = T_2 + 1$

$= \binom{4}{2} (3a)^2 \cdot (2b)^2$

$= 6 \times 9a^2 \times 4b^2$

$= 216a^2b^2$

Question 2.

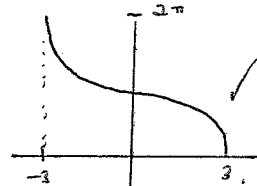
(i)  $y = 2 \cos^{-1}(x/3)$

$\theta: -1 \leq x/3 \leq 1$

$-3 \leq x \leq 3$

$\theta: 0 \leq y/2 \leq \pi$

$0 \leq y \leq 2\pi$



(ii)  $3 \sin \theta + 4 \cos \theta = 5$

$5 \sin(\theta + 53^\circ) = 5$

$\sin(\theta + 53^\circ) = 1$

$\theta + 53^\circ = 90^\circ$

$\theta = 37^\circ$

Note:  $0 \leq \theta < 2\pi$

$\theta +$

(iii) P(6,9)

A(1,4) B(x,y)

$x = 6 = \frac{m \cdot x_2 + n \cdot x_1}{m+n}$

$6 = \frac{-3x + 2}{-1}$

$-6 = -3x + 2$

$-8 = -3x$

$x = 8/3$

$y = 9 = \frac{m \cdot y_2 + n \cdot y_1}{m+n}$

$9 = \frac{-3y + 8}{-1}$

$-9 = -3y + 8$

$-17 = -3y$

$y = 17/3$

(iv) (a) Let  $\angle RST = \alpha$

$\angle RQS = \alpha$  (Angles in the alternate segment)

$\angle QRS = \alpha$  (Angles in a circle)

$\therefore \angle SQR = \angle SRQ = \alpha$

$\therefore SQ = SR$  (Chords subtending equal angles)

(b)  $\angle RST = \angle SPR = \alpha$  (Angles in the alternate segment)

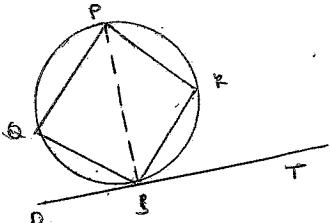
Since  $\angle RQS = \alpha$

then  $\angle QSO = \alpha$  (Angles in the alternate segment)

then  $\angle QPS = \angle QSO$  (Angles in a circle)

$\therefore \angle QPS = \angle SPR = \alpha$

$\therefore SP$  bisects  $\angle QPR$  (Angles are equal)



Question 3.

(i)  $P = \frac{1}{10}$ ,  $Q = \frac{9}{10}$   
 Hit  $N = \pi/4$

$(\frac{1}{10} + \frac{9}{10})^2$

$T_3 = \binom{20}{2} (\frac{1}{10})^2 (\frac{9}{10})^{18}$

(i) (a)  $2x^3 - 3x^2 + 0.99 = 0.$

$P(0) = 0.99$

$P(1) = -6.01$

∴ Change is sign, means root between 0 & 1. ie near 1.

(b).  $x_0 = 1$

$x_1 = 1 - \frac{P(1)}{P'(1)}$

$= 1 - \frac{0.99}{0}$

Cannot find  $x_1$ .

$P(x) = 6x^2 - 6x$

(c). Fails because of turning point at  $x=1$ , ie  $P'(x) = 0$ .

(iii).  $2x^2 + 3x^2 + ax - 6$

$P(-3) = 0.$

$2(-3)^2 + 3(-3)^2 + a(-3) - 6 = 0.$

$-33 - 3a = 0.$

$-3a = 33$

$a = -11$

~~Factors are  $(x+3)$  &  $(2x-3)$~~

~~$= 2x^2 + (6+3)x - 36$~~

~~$2x^2 + 9x - 36 = 0$~~

~~$2x^2 + 3x - 3x - 36 = 0$~~

~~$2x(x+3) - 3(x+12) = 0$~~

~~Let  $x = -3$~~

$\sum x = -3/2 = -3 + \frac{1}{2}$

$3/2 = 1/2$

$\therefore b = -3$

Let  $\beta = \frac{1}{2}$

Question 4.

(i).  $\sum_{k=1}^n 5^k = 5 \left( \frac{5^n - 1}{4} \right)$

Let  $n = 1$   
LHS = 5, RHS =  $5 \left( \frac{5-1}{4} \right) = 5$

∴ LHS = RHS

∴ True for  $n=1$

Assume true for  $n=k$

$5^1 + 5^2 + \dots + 5^k = 5 \left( \frac{5^k - 1}{4} \right)$

Prove true for  $n=k+1$

$5^1 + 5^2 + \dots + 5^k + 5^{k+1} = 5 \left( \frac{5^{k+1} - 1}{4} \right)$

LHS =  $5 \left( \frac{5^k - 1}{4} \right) + 5^{k+1}$

$= \frac{5(5^k - 1) + 5 \times 5^k}{4}$

$= \frac{5(5^k - 1) + 20 \times 5^k}{4}$

$= \frac{5(5^k + 4 \times 5^k - 1)}{4}$

$= \frac{5(5^k(4+1) - 1)}{4}$

-3-

∴ If true for  $n=k$ , and then true for  $n=k+1$ .  
By the principles of Mathematical Induction true for all  $n$  integers.

Q4 (cont)

(i) (a)  $\int e^{f(x)} \cdot f'(x)$

$= \frac{e^{f(x)} + c}{f'(x)}$

(b)  $\int_0^1 \frac{\cos^{-1} x}{\sqrt{1-x^2}} dx$

$= \int_0^1 \frac{-e^{\cos^{-1} x} \cdot dx}{\sqrt{1-x^2}}$

$= - \left[ e^{\cos^{-1} x} \right]_0^1$

$= \left[ e^{\cos^{-1} x} \right]_1^0$

$= e^{\pi/2} - e^0 = \frac{e^{\pi/2} - 1}{1}$

(ii) (a)  $P(2ap, ap^2)$  &  $(2aq, aq^2)$

$x^2 = 4ay$

$y = \frac{x^2}{4a}$

$\frac{dy}{dx} = \frac{2x}{4a}$

$= \frac{x}{2a}$

at  $x = 2ap$

$m = p$

∴ Eqn of 1 =  $y - ap^2 = p(x - 2ap)$

$y - ap^2 = px - 2ap^2$

$y - ap^2 = px - 2ap^2$

$y = px - ap^2$

(b). Eqn of PA =  $\frac{aq^2 - ap^2}{2aq - 2ap}$

$= \frac{a(q-p)(q+p)}{2a(q-p)}$

$= \frac{q+p}{2}$

$= \frac{p+q}{2}$

Eqn:  $y - ap^2 = \frac{p+q}{2} (x - 2ap)$

$2y - 2ap^2 = (p+q)x - 2ap(p+q)$

$2y - 2ap^2 = (p+q)x - 2ap^2 - 2apq$

$y = \frac{(p+q)x}{2} - apq$

If focal chord, then passes through  $(0, a)$

$a = -apq$

$\frac{-a}{apq} = 1$

$-1 = pq$

(c).  $\tan \theta = \frac{m_1 - m_2}{1 + m_1 m_2}$   
 $= \frac{p - \frac{p+q}{2}}{1 + \frac{p(p+q)}{2}}$   
 $= \frac{2p - p - q}{2 + p + pq}$   
 $= \frac{p - q}{2 + p + pq}$

$\theta = 17^\circ 6'$

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Question 5.

(i)  $v^2 = 4x - x^2$

(a). Let  $v=0$ .  
 $4x - x^2 = 0$ .  
 $x = 4 \neq 0$ .

$0 \leq x \leq 4$  ✓

(b). Centre  $x=2$  ✓

$\frac{d}{dt} v^2 = 2x - \frac{x^2}{t}$

$\frac{d}{dx} (\frac{1}{2} v^2) = 2 - x$

$\ddot{x} = -[x-2]$

when  $x=2=0$  ✓  
 $\therefore x=2$

(c). Max Speed when  $\ddot{x}=0$ .  
 $\Rightarrow x=2$

$v^2 = 8 - 4$

$v^2 = 4$  ✓

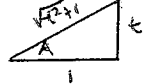
$v = 2$

Max Speed is 2 m/s

(d).  $\ddot{x} = -(x-2)$  ✓ (from above).

(ii).  $\frac{2 \cos A}{\operatorname{cosec} A - 2 \sin A} = \tan 2A$

Let  $\tan A = t$



$\sin A = \frac{t}{\sqrt{t^2+1}}$   
 $\cos A = \frac{1}{\sqrt{t^2+1}}$

$\therefore \text{LHS} = \frac{2 \cos A}{\operatorname{cosec} A - 2 \sin A}$

$= \frac{2}{\frac{1}{\frac{t}{\sqrt{t^2+1}}} - 2 \frac{t}{\sqrt{t^2+1}}}$

$= \frac{2}{\frac{1}{\sqrt{t^2+1}} - \frac{2t}{\sqrt{t^2+1}}}$

$= \frac{2}{\frac{1-2t}{\sqrt{t^2+1}}}$

$= \frac{2 \sqrt{t^2+1}}{1-2t}$

$= \frac{2}{1-t^2}$

$= \frac{1}{1-\tan^2 A}$

$= \tan 2A$   
 $= \text{RHS}$

RHS =  $\tan 2A$

$= \frac{2 \tan A}{1 - \tan^2 A}$

$= \frac{2t}{1-t^2}$

Question 5.

(ii).  $\frac{2 \cos A}{\operatorname{cosec} A - 2 \sin A} = \tan 2A$

Let  $t = \tan A$



$\sin A = \frac{t}{\sqrt{t^2+1}}$   
 $\cos A = \frac{1}{\sqrt{t^2+1}}$

LHS =  $\frac{2}{\frac{1}{\frac{t}{\sqrt{t^2+1}}} - 2 \frac{t}{\sqrt{t^2+1}}}$

$= \frac{2}{\frac{1}{\sqrt{t^2+1}} - \frac{2t}{\sqrt{t^2+1}}}$

$= \frac{2}{\frac{1-2t}{\sqrt{t^2+1}}}$

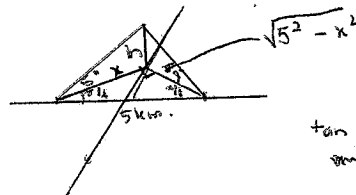
$= \frac{2 \sqrt{t^2+1}}{1-2t}$

$= \frac{2}{1-t^2}$

$= \frac{2 \tan A}{1 - \tan^2 A}$  ✓

$= \tan 2A$   
 $= \text{RHS}$

(ii). (c)



$\tan 5^\circ = \frac{h}{x}$   
 $\cot 5^\circ = \frac{x}{h}$   
 $h \cot 5^\circ = x$   
 $h^2 \cot^2 5^\circ = x^2$  ✓

$\tan 8^\circ = \frac{h}{\sqrt{5^2 - x^2}}$   
 $\cot 8^\circ = \frac{\sqrt{5^2 - x^2}}{h}$   
 $h \cot 8^\circ = \sqrt{5^2 - x^2}$   
 $h^2 \cot^2 8^\circ = 5^2 - x^2$   
 $5^2 - h^2 \cot^2 8^\circ = x^2$

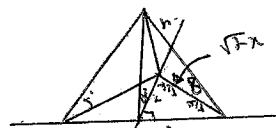
$h^2 \cot^2 5^\circ = 25 - h^2 \cot^2 8^\circ$   
 $h^2 \cot^2 5^\circ + h^2 \cot^2 8^\circ = 25$   
 $h^2 [\cot^2 5^\circ + \cot^2 8^\circ] = 25$

$h^2 = \frac{25}{\cot^2 5^\circ + \cot^2 8^\circ}$

$h = \frac{5}{\sqrt{130.646 + 50.628}}$

$= \frac{5}{13.46}$

$= 0.371 \text{ m}$

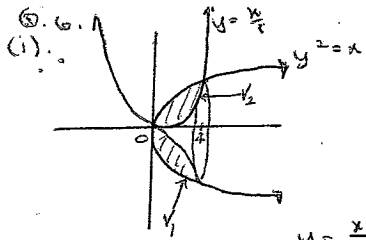


(b)  $\tan \alpha = \frac{h}{x}$   
 $\cot \alpha = \frac{x}{h}$   
 $\sqrt{2} h \cot \alpha = \sqrt{2} x$

$\tan 8^\circ = \frac{h}{\sqrt{2} x}$   
 $\cot 8^\circ = \frac{\sqrt{2} x}{h}$

$\sqrt{2} h \cot 8^\circ = \sqrt{2} x$

$\Rightarrow x = \tan^{-1} \left( \frac{\sqrt{2}}{7.115} \right)$



$$y = \frac{x^2}{8}, \quad y^2 = x \Rightarrow y = \sqrt{x}$$

$$\left(\frac{x^2}{8}\right)^2 = x$$

$$\frac{x^4}{64} = x$$

$$x^4 - 64x = 0$$

$$x(x^3 - 64) = 0$$

$$x = 0, \quad x = 4$$

$$\therefore \text{Area} = \int_0^4 \left(\sqrt{x} - \frac{x^2}{8}\right) dx$$

$$V_1 = \pi \int_0^4 (\sqrt{x})^2 dx$$

$$V_2 = \pi \int_0^4 \left(\frac{x^2}{8}\right)^2 dx$$

$$y^2 = \left(x^{1/2} - \frac{x^2}{8}\right)^2$$

$$= \left(x - \frac{x^{5/2}}{4} + \frac{x^4}{64}\right)$$

$$\therefore \text{Volume} = \pi \int_0^4 \left(x - \frac{x^{5/2}}{4} + \frac{x^4}{64}\right) dx$$

$$= \pi \left[ \frac{x^2}{2} - \frac{2x^{7/2}}{28} + \frac{x^5}{320} \right]_0^4$$

$$= \pi \left[ 8 - 9^{1/4} + 3^{1/5} \right]$$

$$= 2^{2/35} \pi$$

(i) (a)  $f(x) = \sin^{-1} x + \cos^{-1} x = \pi/2$   
 $f'(x) = \frac{d}{dx} (\pi/2) = 0$

(b)  $\int_0^1 \sin^{-1} x + \cos^{-1} x \cdot dx$   
 $= \int_0^1 \pi/2 \cdot dx$   
 $= \pi/2 [x]_0^1$   
 $= \pi/2$

(ii) (a)  $T = 20 + 50e^{-kt}$   
 $T - 20 = 50e^{-kt}$   
 $\frac{dT}{dt} = -50ke^{-kt}$   
 $= -k(T - 20)$

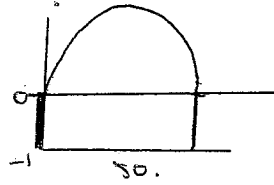
(c) when  $t = 4$ ,  
 $T = 20 + 50e^{-2 \ln 4/5}$   
 $= 48 \frac{1}{8} ^\circ \text{C}$

(b) when  $t = 2$ ,  $T = 60^\circ \text{C}$   
 $60 = 20 + 50e^{-2k}$   
 $40 = 50e^{-2k}$   
 $4/5 = e^{-2k}$   
 $\ln(4/5) = -2k$   
 $k = \frac{-\ln(4/5)}{2}$

$$\therefore T = 20 + 50e^{-\frac{\ln(4/5)}{2} t}$$

$$= 20 + 50e^{-0.11 t}$$

Question 7.



(a)  $x = v \cos \theta, \quad y = -\frac{gt^2}{2} + v \sin \theta$

$x = 50, t = 2, \quad y = 0, t = 2$   
 $50 = 2v \cos \theta, \quad 0 = -20 + 2v \sin \theta$   
 $\frac{50}{2} = v \cos \theta, \quad \frac{20}{2} = v \sin \theta$

$$50 = \left(\frac{20}{\sin \theta}\right) \cos \theta$$

$$50 = 20 \cot \theta$$

$$50 \tan \theta = 20$$

$$\tan \theta = 2/5$$

$$\theta = \tan^{-1}(2/5)$$

$$= 21^\circ 48'$$

$$\frac{20}{\sin 21^\circ 48'} = 2v$$

$$v = \frac{20}{\sin 21^\circ 48'}$$

$$= 26.93 \text{ m/s}$$

(b) Max Height when  $t = 1$

$$y = -\frac{gt^2}{2} + v \sin \theta$$

$$\text{sub } t = 1$$

$$y = -5 + 26.93 \sin 21^\circ 48'$$

$$= 5 \text{ m}$$

plus 1 metre from starting  
 $\therefore$  Max Height = 6m

(ii)  $(a+bx)^n$

$$\frac{T_{r+1}}{T_r} = \frac{\binom{n}{r} (a+bx)^{n-r} b^r}{\binom{n}{r-1} (a+bx)^{n-r+1} b^{r-1}}$$

$$= \frac{n!}{(n-r)! r!} \times a^{n-r} \times (bx)^r$$

$$\frac{n!}{(n-r+1)! (r-1)!} \times a^{n-r+1} \times (bx)^{r-1}$$

$$= \frac{n!}{(n-r)! r!} \times \frac{(n-r+1)(r-1)!}{(r-1)!} \times \frac{bx}{a}$$

$$= \frac{n-r+1}{r} \times \frac{bx}{a}$$

(b)  $\frac{T_{r+1}}{T_r} = 1 \Rightarrow \frac{(n-r+1)}{r} \times \frac{1}{3} = 1$

$$\frac{16-r}{3r} = 1$$

$$16-r = 3r$$

$$16 = 4r$$

$$r = 4$$

$$\therefore T_5 = T_4$$

$$\therefore T_5 = T_4$$