

C.E.M. TUITION

Student Name : _____

Review Topic : Linear Functions

(Preliminary Course - Paper 1)

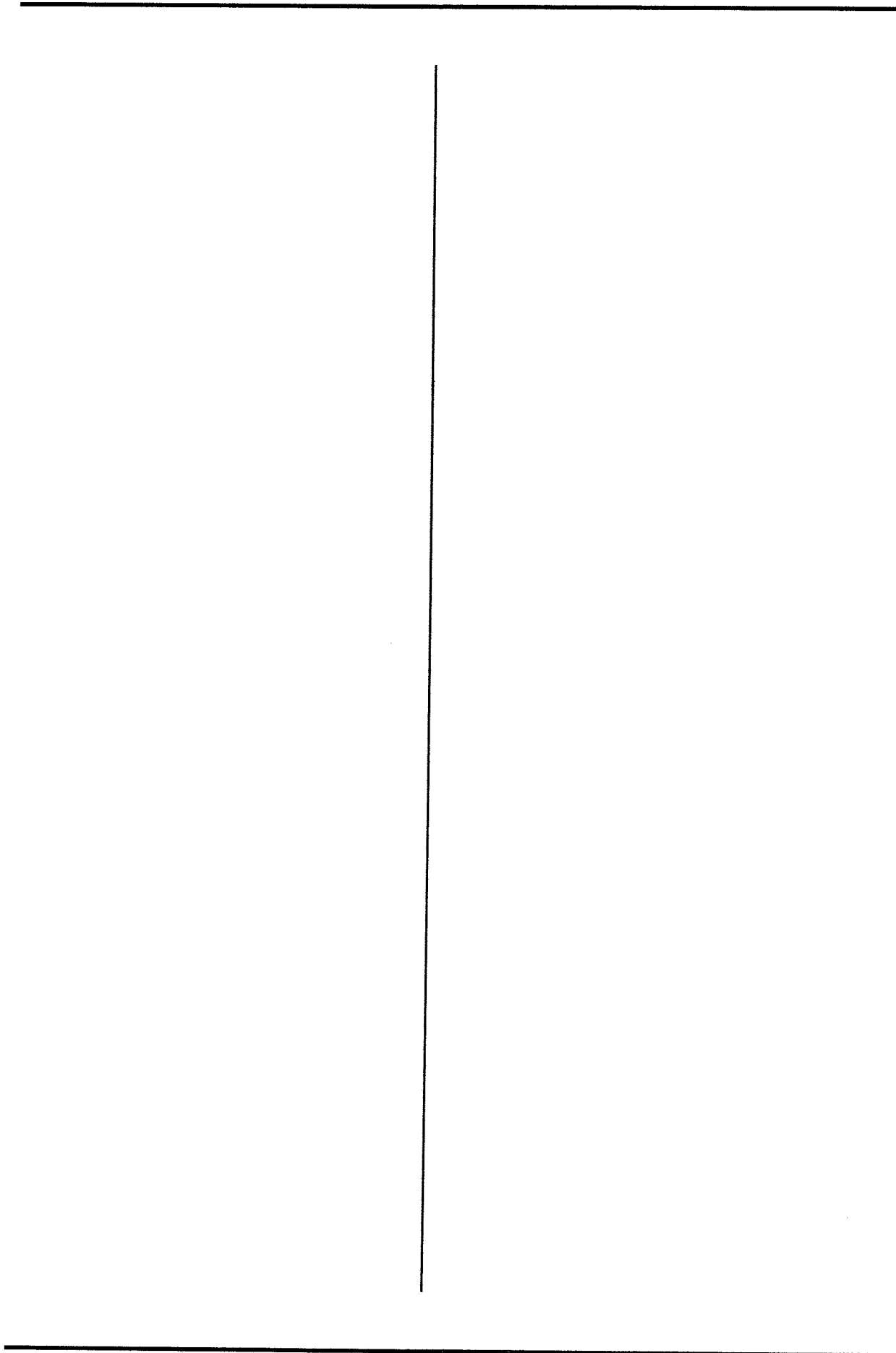
Year 11 - 2 Unit

Question 1

Without using square paper, plot on the Cartesian plane the three points A, B, C , whose coordinates are $(-5, 3)$, $(1, -5)$, $(2, 2)$, respectively.

- (a) Calculate the length AB . (b) Find the equation of the line AB .
- (c) The line through C , perpendicular to AB , meets AB at N . Find the coordinates of N .
- (d) Hence, or otherwise, find the area of $\triangle ABC$.

(a) 10 units (b) $4x + 3y + 11 = 0$ (c) $(-2, -1)$ (d) 25 units^2



Question 2 :

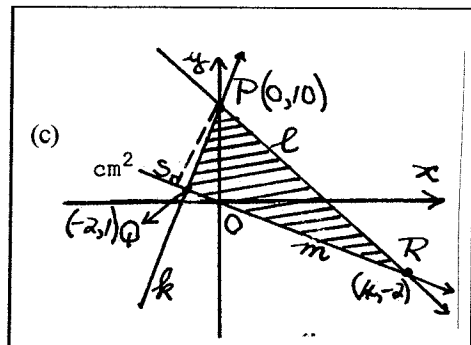
The point $Q(-2, 1)$ lies on the line k whose equation is $9x - 2y + 20 = 0$.

The point $R(4, -2)$ lies on the line l whose equation is $3x + y - 10 = 0$.

- (a) Show that k and l intersect at a point P on the y -axis.
- (b) Find the equation of the line m which joins Q and R .
- (c) Show, by shading on a sketch (not on graph paper), the region defined by the three inequalities
 $9x - 2y + 20 \geq 0$, $3x + y - 10 \leq 0$, $x + 2y \geq 0$.
- (d) Find, as a surd, the perpendicular distance from P to m .
- (e) Hence, or otherwise, find the exact value of the area of the triangle bounded by the three lines k , l and m .



(a) intersect at $(0, 10)$ (b) $x + 2y = 0$ (d) $4\sqrt{5}$ (e) 30 units^2



Question 3 :

(a) $A(1, 8)$, $B(3, 7)$ and $C(-2, 5)$ are three vertices of a parallelogram $ABCD$.
Find the coordinates of D .

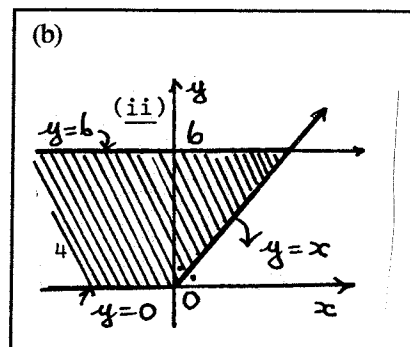
(b) Show that the points $A(3, -1)$, $B(7, 2)$ and $C(1, 10)$ are the vertices of a right-angled triangle.
Also find the area of $\triangle ABC$.

(a) $(-4, 6)$ (b) 25 units^2

Question 4 :

- (a) Find the equation of the line passing through the point (2, 7) and parallel to the line $2x - 3y = 8$.
- (b) On a sketch indicate, by suitable shading and labelling, the region $\{(x, y) : y \geq x\} \cap \{(x, y) : 0 \leq y \leq 6\}$.

(a) $2x - 3y + 17 = 0$



Question 5:

- (a) The three lines $3x - y = 6$, $2x + y = 14$ and $y = 0$ enclose a triangle. Find its area.
- (b) The two perpendicular lines $3x + 2y = 12$, $2x + ay = b$ intersect at the point $(2, 3)$. Find the values of a and b .
- (c) Show that the points $(2, 7)$, $(5, 13)$, $(-4, -5)$ are collinear.

(a) 15 units² (b) $a = -3, b = -5$

Question 6 :

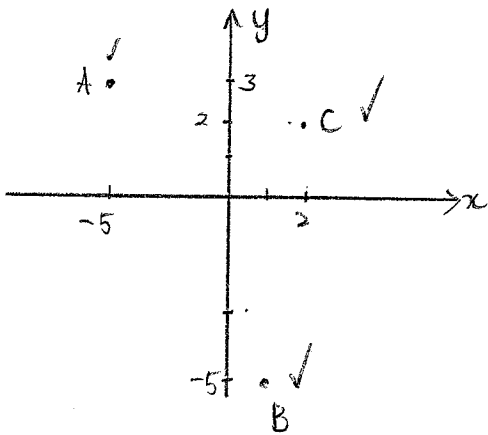
- (a) Give three inequalities satisfied by every point in the interior of the triangle with vertices $(0, 0)$, $(1, 0)$, $(0, 1)$ and such that no point outside the triangle satisfies all three inequalities.
- (b) R is the foot of the perpendicular from the point $P(-5, 10)$ to the line $4x - 3y = 0$. Find the coordinates of R .

(a) $x > 0, y > 0, x + y < 1$ (b) $R(3, 4)$

Question 1

Without using square paper, plot on the Cartesian plane the three points A, B, C , whose coordinates are $(-5, 3), (1, -5), (2, 2)$, respectively.

- (a) Calculate the length AB .
- (b) Find the equation of the line AB .
- (c) The line through C , perpendicular to AB , meets AB at N . Find the coordinates of N .
- (d) Hence, or otherwise, find the area of $\triangle ABC$.



$$(a) d_{AB} = \sqrt{6^2 + 8^2}$$

$$= \sqrt{100} = 10 \text{ units} \checkmark$$

(distance is positive)

$$(b) m_{AB} = \frac{-8}{6} = -\frac{4}{3}$$

$$\therefore y + 5 = \frac{-4}{3}(x - 1)$$

$$3y + 15 = -4x + 4$$

$$4x + 3y + 11 = 0 \checkmark$$

$$(c) m_{\perp} = \frac{3}{4} \quad y - 2 = \frac{3}{4}(x - 2)$$

$$4y - 8 = 3x - 6$$

$$3x - 4y = -2 \quad \text{--- (1)}$$

$$4x + 3y = -11 \quad \text{--- (2)}$$

$$\textcircled{1} \times 3: 9x - 12y = -6 \quad \text{--- (3)}$$

$$\textcircled{2} \times 4: 16x + 12y = -44 \quad \text{--- (4)}$$

$$\textcircled{3} + \textcircled{4}: 25x = -50$$

$$x = -2 \text{ sub in (1)}$$

$$-6 - 4y = -2$$

$$4y = -4$$

$$y = -1$$

$\therefore (-2, -1)$ is N

$$(d) d_{CN} = \sqrt{16 + 9}$$

$$= 5 \text{ units} \checkmark$$

$$\therefore A \text{ of } \triangle ABC = \frac{1}{2} \cdot 5 \cdot 10$$

$$= 25 \text{ units}^2$$

(a) 10 units (b) $4x + 3y + 11 = 0$ (c) $(-2, -1)$ (d) 25 units^2

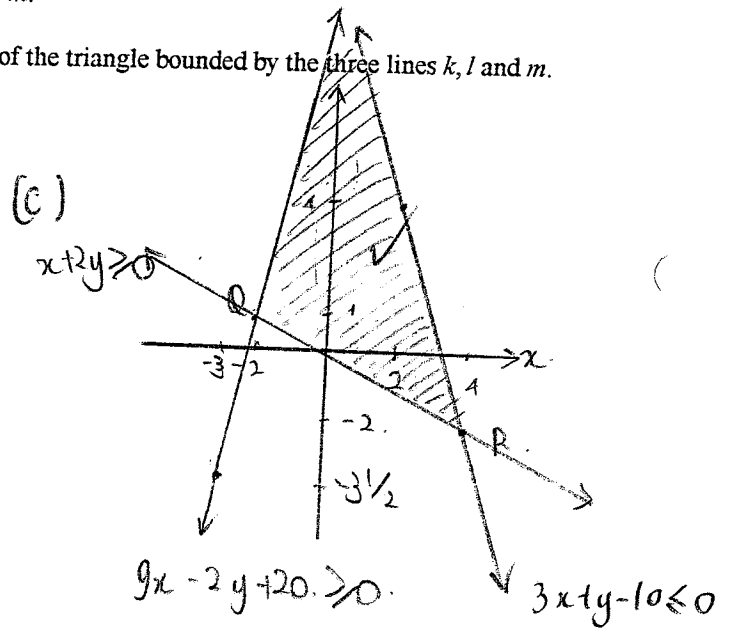
Question 2:

The point $Q(-2, 1)$ lies on the line k whose equation is $9x - 2y + 20 = 0$.
 The point $R(4, -2)$ lies on the line l whose equation is $3x + y - 10 = 0$.

- (a) Show that k and l intersect at a point P on the y -axis.
- (b) Find the equation of the line m which joins Q and R .
- (c) Show, by shading on a sketch (not on graph paper), the region defined by the three inequalities

$$9x - 2y + 20 \geq 0, \quad 3x + y - 10 \leq 0, \quad x + 2y \geq 0.$$

- (d) Find, as a surd, the perpendicular distance from P to m .
- (e) Hence, or otherwise, find the exact value of the area of the triangle bounded by the three lines k, l and m .



(a) $9x - 2y = -20$ — (1)
 $3x + y = 10$ — (2)
 (2) $\times 2 = 6x + 2y = 20$ — (3)
 (3) + (1) : $15x = 0$
 $x = 0$ ✓
 $y = 10 \therefore (0, 10)$

$\therefore k$ and l intersect at a point $P(0, 10)$ on the y -axis

(b) $m \text{ QR} = \frac{13}{6} = \frac{1}{2}$
 $y - 1 = -\frac{1}{2}(x + 2)$ ✓
 $2y - 2 = -x - 2$
 $\therefore x + 2y = 0$ ✓

(c) $x + 2y \geq 0$
 $9x - 2y + 20 \geq 0$
 $3x + y - 10 \leq 0$

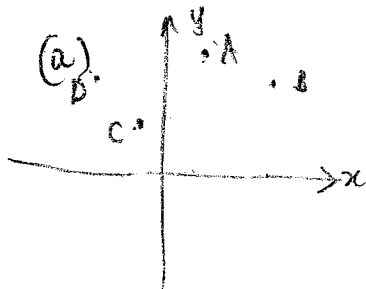
(d) $P(0, 10)$ $m: x + 2y = 0$
 $\therefore d = \frac{|20|}{\sqrt{1+4}} = \frac{20}{\sqrt{5}} = \frac{20\sqrt{5}}{5} = 4\sqrt{5}$ units

(e) $d_{QR} = \sqrt{36 + 9} = \sqrt{45} = 3\sqrt{5}$ units
 $\therefore A = \frac{1}{2} \times 3\sqrt{5} \times 4\sqrt{5} = 30$ units²

Question 3:

(a) $A(1, 8)$, $B(3, 7)$ and $C(-2, 5)$ are three vertices of a parallelogram $ABCD$.
Find the coordinates of D .

(b) Show that the points $A(3, -1)$, $B(7, 2)$ and $C(1, 10)$ are the vertices of a right-angled triangle.
Also find the area of $\triangle ABC$.



$D(-4, 6)$

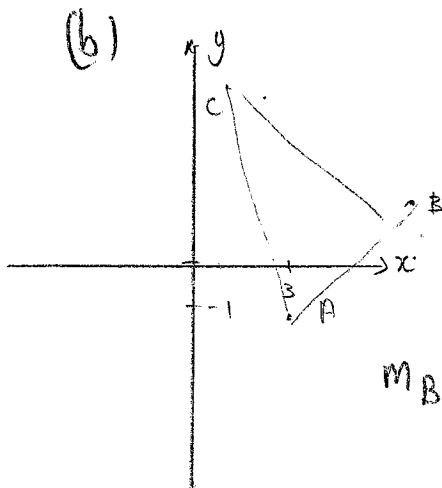
$$d_{BC} = \sqrt{36 + 64}$$

$$= \sqrt{100} = 10 \text{ units}$$

$$d_{AB} = \sqrt{16 + 9}$$

$$= \sqrt{25} = 5 \text{ units}$$

$$\therefore A \text{ is } 25 \text{ units}^2$$



$$m_{BC} = \frac{8}{-6}$$

$$= -\frac{4}{3}$$

$$m_{AB} = \frac{3}{4}$$

$$\text{since } m_{BC} \times m_{AB} = -\frac{4}{3} \times \frac{3}{4}$$

$$= -1$$

$AB \perp BC$

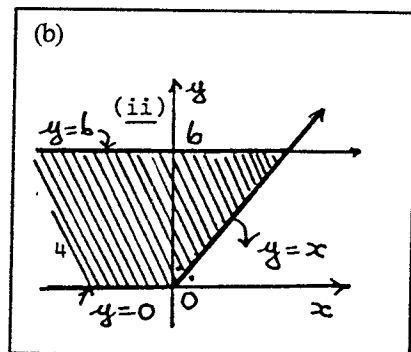
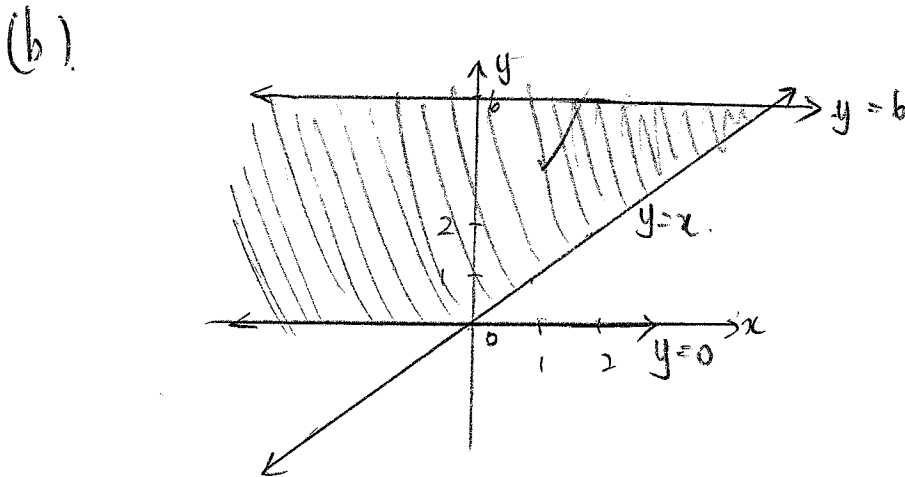
$\therefore A, B, C$ are the vertices of a right-angled \triangle

(a) $(-4, 6)$ (b) 25 units^2

Question 4 :

- (a) Find the equation of the line passing through the point (2, 7) and parallel to the line $2x - 3y = 8$.
 (b) On a sketch indicate, by suitable shading and labelling, the region $\{(x, y) : y \geq x\} \cap \{(x, y) : 0 \leq y \leq 6\}$.

(a) $3y = 2x + 8$
 $m = \frac{2}{3} \therefore y - 7 = \frac{2}{3}(x - 2)$
 $3y - 21 = 2x - 4$
 $\therefore 2x - 3y + 17 = 0$



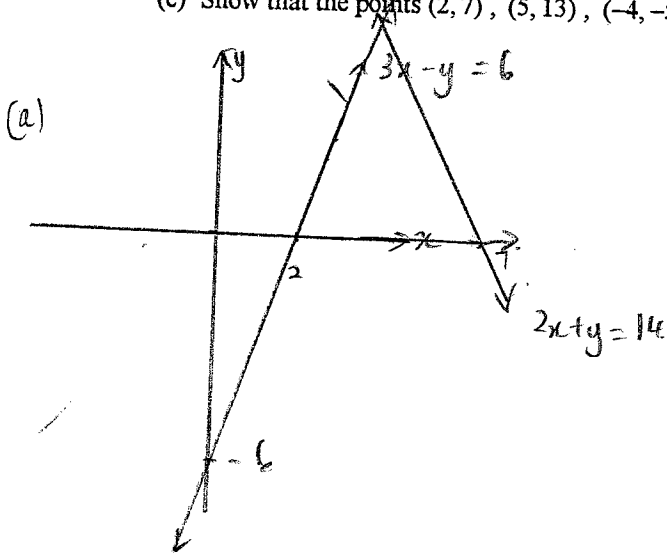
(a) $2x - 3y + 17 = 0$

Question 5:

(a) The three lines $3x - y = 6$, $2x + y = 14$ and $y = 0$ enclose a triangle. Find its area.

(b) The two perpendicular lines $3x + 2y = 12$, $2x + ay = b$ intersect at the point $(2, 3)$. Find the values of a and b .

(c) Show that the points $(2, 7)$, $(5, 13)$, $(-4, -5)$ are collinear.



$$3x - y = 6 \quad \text{--- ①}$$

$$2x + y = 14 \quad \text{--- ②}$$

$$\text{①} + \text{②} : 5x = 20 \quad \checkmark$$

$$x = 4 \quad \text{sub in ①}$$

$$12 - y = 6$$

$$6 = y \quad \checkmark \Rightarrow (4, 6)$$

$d = 6$ units.

$$\therefore A = 6 \times 5 \times \frac{1}{2} \quad \checkmark$$

$$= 15 \text{ units}^2$$

(b) $2y = -3x + 12$

$$y = -\frac{3}{2}x + 12$$

$$m = -\frac{3}{2}$$

$$\therefore m_{\perp} = \frac{2}{3} \quad \checkmark$$

$$\therefore ay = -2x + b$$

$$y = -\frac{2}{a}x + \frac{b}{a}$$

$$\therefore -\frac{2}{a} = \frac{2}{3}$$

$$2a = -6$$

$$a = -3 \quad \checkmark$$

$$2(2) + 3(3) = b$$

$$4 + 9 = b$$

$$b = 13 \quad \checkmark$$

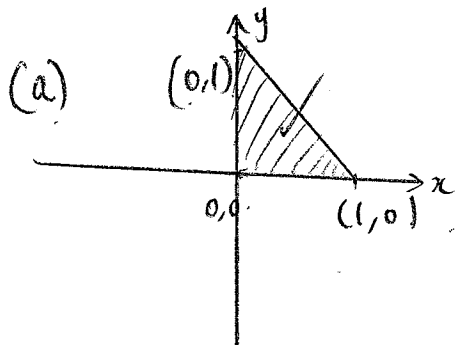
$$\therefore a = -3$$

$$b = 13$$

(a) 15 units^2 (b) $a = -3, b = 13$

Question 6 :

- (a) Give three inequalities satisfied by every point in the interior of the triangle with vertices $(0, 0)$, $(1, 0)$, $(0, 1)$ and such that no point outside the triangle satisfies all three inequalities.
- (b) R is the foot of the perpendicular from the point $P(-5, 10)$ to the line $4x - 3y = 0$. Find the coordinates of R .



(a) $y \geq 0 \cap x \geq 0 \cap y \leq -x + 1$
 interior only.

(b) $3y = 4x$
 $m = \frac{4}{3}$ ✓
 $m_{\perp} = -\frac{3}{4}$

$\therefore y - 10 = -\frac{3}{4}(x + 5)$
 $4y - 40 = -3x - 15$ ✓
 $\therefore 3x + 4y = 25$ — ①

$4x - 3y = 0$ — ②

① $\times 3$: $9x + 12y = 75$ — ③

② $\times 4$: $16x - 12y = 0$ — ④

③ + ④ : $25x = 75$ ✓

$x = 3$ sub in ②

$12 - 3y = 0$ ✓

$\therefore y = 4$

$\therefore R = (3, 4)$

(a) $x > 0, y > 0, x + y < 1$ (b) $R(3, 4)$