Basic Geometrical Concepts and Properties

Marks:

/60

Time: 1 hour 30 minutes

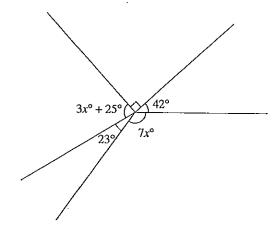
Name:	Date:

INSTRUCTIONS TO CANDIDATES

Section A (30 marks)

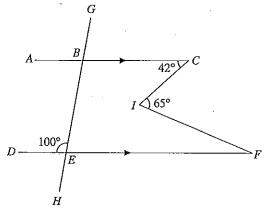
Time: 45 minutes

- 1. Answer all the questions in this section.
- 2. Calculators may not be used in this section.
- 3. All working must be clearly shown. Omission of essential working will result in loss of marks.
- 4. The marks for each question is shown in brackets [] at the end of each question.
- 1 Find the value of x in the diagram.



Answer $x = \dots [2]$

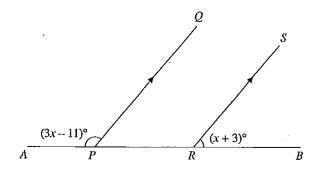
- In the diagram AC is parallel to DF. The line GH intersects AC at B and DF at E. Given that $B\hat{C}I = 42^{\circ}$, $C\hat{I}F = 65^{\circ}$ and $B\hat{E}D = 100^{\circ}$, calculate
 - (a) $D\hat{F}I$,
 - (b) $A\widehat{B}E$.



Answer (a)
$$D\hat{F}I =$$
 ° [2]

(b)
$$A\hat{B}E =$$
 ° [1]

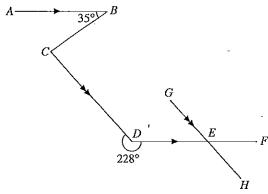
3 In the diagram PQ is parallel to RS. $A\hat{P}Q = (3x - 11)^{\circ}$ and $B\hat{R}S = (x + 3)^{\circ}$. Find the value of x.



Answer
$$x = \dots$$
 [2]

4 AB is parallel to DEF and CD is parallel to GEH, $\triangle ABC = 35^{\circ}$ and reflex $\triangle CDE = 228^{\circ}$. Calculate

- (a) $B\widehat{C}D$,
- (b) $F\hat{E}H$.

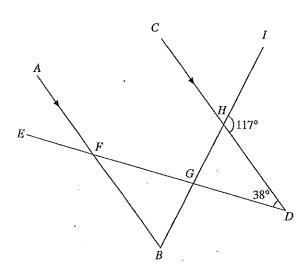


Answer (a)
$$B\hat{C}D = \dots \circ [3]$$

(b)
$$F\hat{E}H =$$
 ° [1]

In the diagram AB is parallel to CD. Given that $G\widehat{D}H = 38^{\circ}$ and $D\widehat{H}I = 117^{\circ}$, calculate

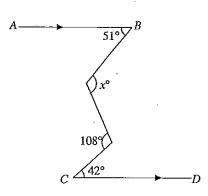
- (a) $B\widehat{F}G$,
- (b) $A\widehat{F}E$,
- (c) $F\widehat{B}G$.



Answer (a)
$$B\hat{F}G = \dots \circ [1]$$

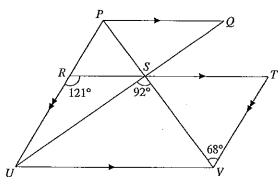
(b)
$$\hat{AFE} = \dots ^{\circ} [1]$$

(c)
$$F\widehat{B}G = \dots \circ [1]$$



Answer
$$x = \dots$$
 [3]

- In the diagram PQ is parallel to RST and UV, PRU is parallel to TV, $U\hat{S}\hat{V} = 92^{\circ}$, $U\hat{R}S = 121^{\circ}$ and $S\hat{V}T = 68^{\circ}$. Calculate
 - (a) $P\hat{S}Q$,
 - (b) $R\hat{P}S$,
 - (c) *STV*,
 - (d) $S\widehat{P}Q$.



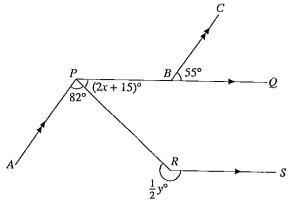
Answer (a)
$$P\hat{S}Q =$$
 ° [1]

(b)
$$R\hat{P}S =$$
 ° [1]

(c)
$$\hat{STV} = \dots ^{\circ} [1]$$

(d)
$$\hat{SPQ} = \dots ^{\circ} [1]$$

8 In the diagram PQ is parallel to RS and AP is parallel to BC. $A\widehat{P}R = 82^{\circ}$, $C\widehat{B}Q = 55^{\circ}$, $B\widehat{P}R = (2x + 15)^{\circ}$ and reflex $P\widehat{R}S = \frac{1}{2}y^{\circ}$. Find the values of x and y.

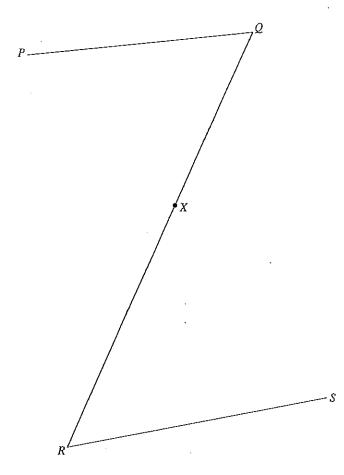


$$y = \dots [2]$$

- 9 (a) On the diagram, construct
 - (i) the angle bisector of $P\hat{Q}R$,
 - (ii) a line passing through \widetilde{X} and parallel to RS.
 - (b) Mark with the letter Y, the point of intersection of the angle bisector and the parallel line through X.

Answer (a) (i), (ii), (b)

[2]



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- 10 (a) On the line AB given below, construct
 - (i) the angle CAB such that $C\widehat{A}B = 42^{\circ}$,
 - (ii) the perpendicular bisector of AB.
 - (b) Mark with the letter C, the point of intersection of AC and the perpendicular bisector of AB. Measure and write down the length of AC.

Answer (a) (i), (ii) (b)

[2]

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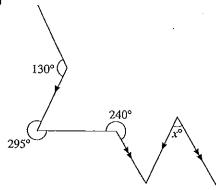
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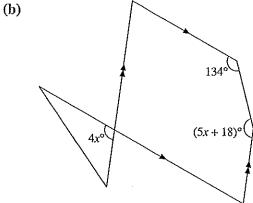
Answer (b) AC = cm [1].

INSTRUCTIONS TO CANDIDATES

Section B (30 marks)

- Answer all the questions in this section.
- Calculators may be used in this section.
- All working must be clearly shown. Omission of essential working will result in loss of marks. 3.
- The marks for each question is shown in brackets [] at the end of each question.
- 11 Find the value of x in each of the following.





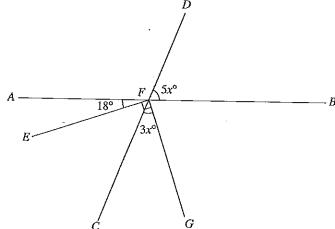
(b)
$$x = \dots [4]$$

Time: 45 minutes

- (a) x,
- (b) $E\widehat{F}C$,

 $B\hat{F}D = 5x^{\circ}$. Find

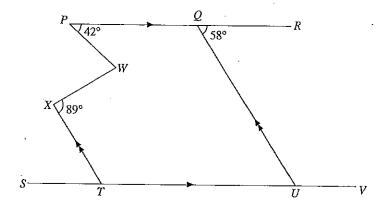
(c) $A\hat{F}D$.



(b)
$$E\hat{F}C =$$
 ° [1]

(c)
$$A\hat{F}D = \dots \circ [1]$$

- 13 In the diagram PR is parallel to SV and TX is parallel to UQ. Given that $W\hat{P}Q = 42^{\circ}$, $T\hat{X}W = 89^{\circ}$ and $U\hat{Q}R = 58^{\circ}$, calculate
 - (a) $Q\hat{U}T$,
 - (b) $U\widehat{T}X$,
 - (c) reflex $P\hat{W}X$.

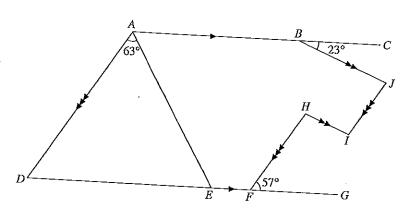


Answer (a)
$$\hat{QUT} = \dots \circ [1]$$

(b)
$$U\hat{T}X =$$
 ° [1]

(c) reflex
$$P\hat{W}X =$$
 ° [3]

- (b) In the diagram AC is parallel to DG, BJ is parallel to HI and AD is parallel to HF and JI. Given that $D\hat{A}E = 63^{\circ}$, $H\hat{F}G = 57^{\circ}$ and $C\hat{B}J = 23^{\circ}$, calculate
 - (i) $E\widehat{A}B$,
 - (ii) $H\hat{I}J$.



(b) (i)
$$E\hat{A}B = \dots \circ [2]$$

(ii)
$$H\hat{I}J =$$
 ° [2]

(i) a line perpendicular to AB, passing through A,

(ii) a line parallel to BC and passing through A.

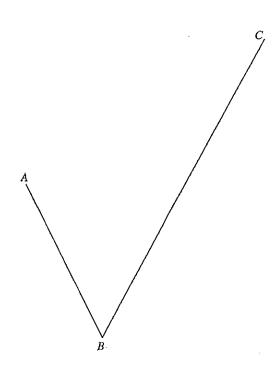
(b) The line perpendicular to A intersects the line BC at D.

(i) Mark and label the point D on the diagram.

(ii) Measure and write down the length of BD and the size of $A\widehat{D}B$.

Answer (a) (i), (ii), (b) (i)

[2]



$$\hat{ADB} = \dots \circ [2]$$

14. (a)

Teacher's Tip

For calculate the percentage discount, find the samount he saved

Amount saved

- = \$80 000 \$73 200
- = \$6800

Percentage discount

$$= \frac{\$6800}{\$80\ 000} \times 100\%$$
$$= 8.5\%$$



Teacher's Tip

The percentage discount is calculated based on the selling price, i.e. \$80,000 and not on the amount paid. (i.e. \$73,200

- (b) (i) Amount paid by hire purchase
 - = \$6800 + (60 × \$1433.50)
 - = \$6800 + \$86 010
 - = \$92 810.

5)yrs = 5 × 12 = 60 mths

- Extra cost incurred
- = \$92 810 -- \$80 000
- = \$12 810
- (ii) Principal, $P = $80\ 000 6800 = \$73 200

Interest, I = \$12 810; Time, T = 5 yrs; Rate, R = ?

$$I = \frac{PRT}{100}$$

$$$12 810 = \frac{$73 200 \times R \times 5}{100}$$

$$R = \frac{\$12\ 810\ \times\ 100}{\$73\ 200\ \times\ 5}$$
$$= 3.5\%$$

: the rate of interest charged per annum is 3.5%.



Teacher's Tip

#The extra cost incurred is the amount of interest to be a paid through the hire purchase scheme, interest is only a charged on \$731200? i.e. after deducting the deposit.

- 15. (a) Total monthly basic salary in 2002
 - $= 12 \times 5750
 - = \$69 000

Bonus received in 2002

- = 0.85% of \$1.2 million
- $= \frac{0.85}{100} \times \$1\ 200\ 000$
- = \$10 200

Total income in 2002

- = \$69 000 + \$10 200
- **= \$79 200**

(b) (i) Total basic salary in 2002 is \$69 000.

Total basic salary in 2003

= 103.2% of \$69 000

$$= \frac{103.2}{100} \times \$69\ 000$$

= \$71 208

(ii) Bonus received in 2003

= \$7276

0.85% — \$7276

$$100\% - \frac{100}{0.85} \times \$7276 = \$856\ 000$$

: the value of the sales in 2003 is \$856 000.

Test 13: Basic Geometrical Concepts and Properties

Section A

1.
$$90^{\circ} + (3x^{\circ} + 25^{\circ}) + 23^{\circ} + 7x^{\circ} + 42^{\circ} = 360^{\circ}$$
 (\angle s at $10x^{\circ} + 180^{\circ} = 360^{\circ}$ a point)

$$10x^{\circ} = 180^{\circ}$$

$$x^{\circ} = \frac{180^{\circ}}{10^{\circ}}$$

$$x^{\circ} = 18^{\circ}$$

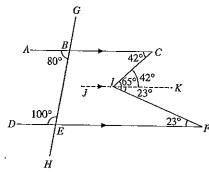
$$\therefore x = 18$$

Teacher's Tip

The sum of angles at a point is 360° $(a+b)+c+d=360^\circ$ (\angle s at a pt)



2.



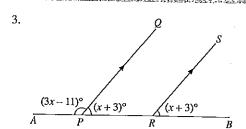
(a) Draw the line JK parallel to AC.

$$\widehat{CIK} = 42^{\circ}$$
 (alt. $\angle s$, $AC // JK$)

$$K\widehat{l}F = 65^{\circ} - 42^{\circ}$$

$$D\hat{F}I = 23^{\circ}$$
 (alt. $\angle s$, $JK // DF$)

(b)
$$A\hat{B}E = 180^{\circ} - 100^{\circ}$$
 (int. \angle s, $AC // DF$)
= 80°

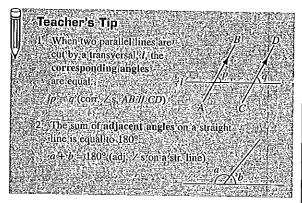


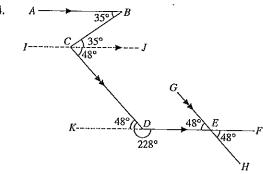
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nt)

$$Q\widehat{P}R = (x + 3)^{\circ} \text{ (corr. } \angle s, PQ \text{ // } RS\text{)}$$

 $(3x - 11)^{\circ} + (x + 3)^{\circ} = 180^{\circ} \text{ (adj. } \angle s \text{ on a str. line)}$
 $4x = 180 + 8$
 $4x = 188$
 $x = \frac{188}{4} = 47$





(a) Draw the line IJ passing through C and parallel to AB. Produce FD to K. $B\hat{C}J = 35^{\circ}$ (alt. $\angle s$, AB || IJ) $C\hat{D}K = 228^{\circ} - 180^{\circ}$ (A straight angle is 180° .)

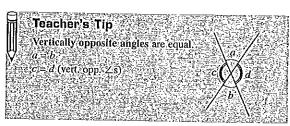
$$J\hat{C}D = 48^{\circ}$$
 (alt. $\angle s$, $IJ \parallel KF$)

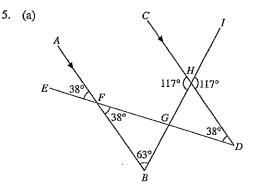
$$\therefore B\hat{C}D = B\hat{C}J + J\hat{C}D$$

$$= 35^{\circ} + 48^{\circ}$$

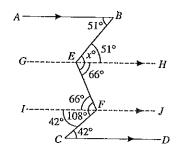
$$= 83^{\circ}$$

(b) $\widehat{GED} = 48^{\circ}$ (corr. $\angle s$, CD // GH) $\widehat{FEH} = 48^{\circ}$ (vert. opp. $\angle s$)





- (i) $B\hat{F}G = 38^{\circ}$ (alt. $\angle s$, AB // CD)
- (ii) $A\hat{F}E = 38^{\circ}$ (vert. opp. \angle s)
- (iii) $\hat{CHG} = 117^{\circ}$ (vert. opp. \angle s) $\hat{FBG} = 180^{\circ} - 117^{\circ}$ (int. \angle s, AB // CD) $= 63^{\circ}$



At the points E and F, draw two lines parallel to AB as shown.

$$B\hat{E}H = 51^{\circ}$$
 (alt. ∠s, $AB \# GH$)
 $I\hat{F}C = 42^{\circ}$ (alt. ∠s, $IJ \# CD$)
 $H\hat{E}F = E\hat{F}I$ (alt. ∠s, $GH \# IJ$)
 $= 108^{\circ} - 42^{\circ}$
 $= 66^{\circ}$
 $x^{\circ} = B\hat{E}H + H\hat{E}F$
 $= 51^{\circ} + 66^{\circ}$
 $= 117^{\circ}$
∴ $x = 117$

= 48°

(b)
$$R\hat{P}S = 68^{\circ}$$
 (alt. $\angle s$, $PU // TV$)

(c)
$$S\hat{T}V = 180^{\circ} - 121^{\circ}$$
 (int. $\angle s$, $PU // TV$)
= 59°

(d)
$$R\hat{P}Q = 121^{\circ}$$
 (corr. $\angle s$, $PQ \parallel RT$)
 $R\hat{P}S + S\hat{P}Q = 121^{\circ}$
 $68^{\circ} + S\hat{P}Q = 121^{\circ}$
 $S\hat{P}Q = 121^{\circ} - 68^{\circ} = 53^{\circ}$

8.
$$P\hat{B}C = 180^{\circ} - 55^{\circ}$$
 (adj. \angle s on a str. line)
= 125°

$$A\widehat{P}B = 125^{\circ} \text{ (alt. } \angle s, AP \text{ // }BC\text{)}$$

 $82^{\circ} + (2x + 15)^{\circ} = 125^{\circ}$
 $2x = 125 - 82 - 15$
 $= 28$
 $x = \frac{28}{2} = 14$

$$B\widehat{P}R = (2x + 15)^{\circ}$$

= $[2(14) + 15]^{\circ}$
= 43°

$$P\hat{R}S = 180^{\circ} - 43^{\circ} \text{ (int. } \angle s, PQ \text{ // } RS\text{)}$$

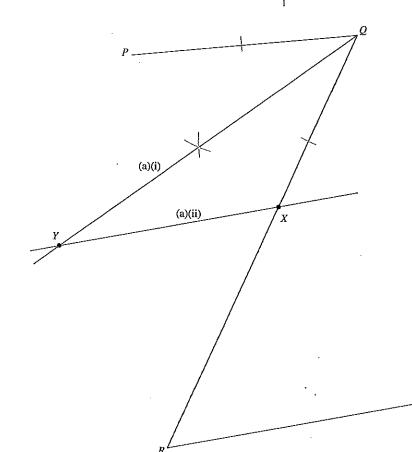
= 137°

$$\frac{1}{2}y^{\circ} + 137^{\circ} = 360^{\circ} (\angle s \text{ at a pt.})$$

$$\frac{1}{2}y = 223 y = 223 \times 2 = 446$$

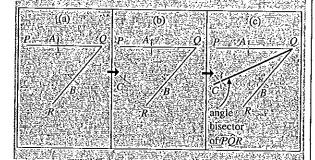
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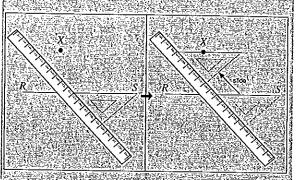


Teacher's Tip

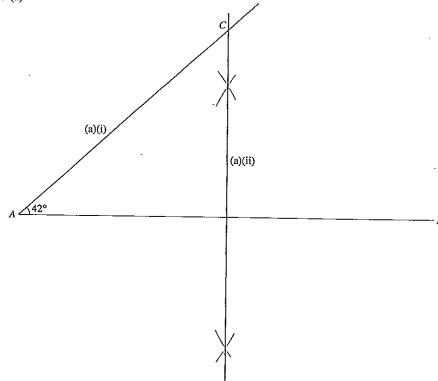
- 1. To construct the angle bisector of $P\widehat{Q}R$
 - (a) Use a pair of compasses and with Q as centre, mark an arc to cut PQ at A and an arc to cut QR at B.
 - (b) Using the same radius, with A and B as centres, draw two ares to intersect at C.
 (c) Draw a straight line from Q through C
 QC is the angle bisector of PQR



- To draw a line through X which is parallel to RS: (a) Place the set square on line RS and ruler as
 - shown: (b) Slide the set square along the length of the ruler until it passes through the point X.
 - (c) Draw the line passing through X which is parallel





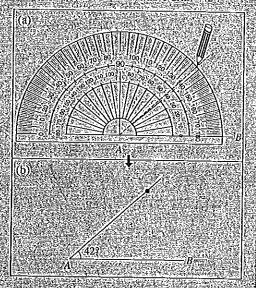


(b) AC = 7.4 cm

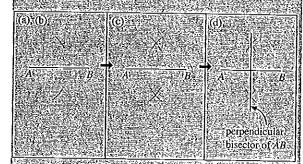
Teacher's Tip

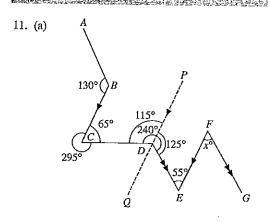
- To draw angle \widehat{CAB} such that $\widehat{CAB} = 42$
- (a) Place a protractor such that its centre is at Aranditis base is along AB as shown.

 (b) Mark'a point on the 42° graduation with your pencil
- Join the point to A and we have $\widehat{CAB} = 42^{\circ}$



- To construct the perpendicular bisector of AB
- (a) Set your compasses to more than half the length
- (b) With A as centre, mark arcs above and below AB c) Repeat the process with B as centre
- (d)Drawa straight!line passing through the two sets of intersecting arcs





Draw line PQ through D parallel to BC and FE.

$$B\hat{C}D = 360^{\circ} - 295^{\circ} (\angle s \text{ at a pt.})$$

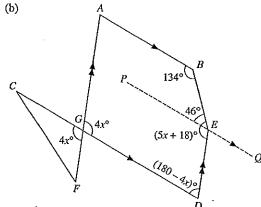
$$\widehat{CDP} = 180^{\circ} - 65^{\circ} \text{ (int. } \angle \text{s, } BC \text{ // } PQ\text{)}$$

$$P\widehat{D}E = 240^{\circ} - 115^{\circ}$$

$$D\widehat{E}F = 180^{\circ} - 125^{\circ}$$
 (int. \angle s, $PQ // FE$)

$$x^{\circ} = D\hat{E}F$$
 (alt. \angle s, $DE // FG$)
= 55°

$$\therefore x = 55$$



$$A\hat{G}D = 4x^{\circ}$$
 (vert. opp. \angle s)

$$\widehat{GDE} = (180 - 4x)^{\circ}$$
 (int. $\angle s$, $GA // DE$)

Draw the line PQ through E parallel to AB.

$$P\hat{E}B = 180^{\circ} - 134^{\circ} \text{ (int. } \angle s, AB // PQ)$$

= 46°

$$P\hat{E}D = (5x + 18)^{\circ} - 46^{\circ}$$

$$PED = (5x + 18)^{\circ} - 46^{\circ}$$

= $(5x - 28)^{\circ}$

$$P\hat{E}D + G\hat{D}E = 180^{\circ} \text{ (int. } \angle s, PQ \# GD)$$

$$(5x - 28)^{\circ} + (180 - 4x)^{\circ} = 180^{\circ}$$

$$x^{\circ} = 28^{\circ}$$

$$\therefore x = 28$$

12. (a)
$$D$$

$$A \xrightarrow{F \leq 5x^{\circ}} B$$

$$E \xrightarrow{3x^{\circ}} G$$

$$G\widehat{F}B = 180^{\circ} - 18^{\circ} - 90^{\circ}$$
 (adj. \angle s on a str. line)
= 72°

$$3x^{\circ} + 72^{\circ} + 5x^{\circ} = 180^{\circ}$$
 (adj. \angle s on a str. line)

$$8x = 180 - 72$$

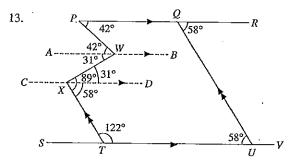
$$8x = 108$$

$$x = \frac{108}{9} = 13.5$$

(b)
$$E\widehat{F}C = 90^{\circ} - 3(13.5^{\circ})$$

= 49.5°

(c)
$$A\widehat{F}D = 180^{\circ} - 5(13.5^{\circ})$$
 (adj. \angle s on a str. line)
= 112.5°



(a)
$$Q\hat{U}T = 58^{\circ}$$
 (alt. \angle s, $PR // SV$)

(b)
$$U\hat{T}X = 180^{\circ} - 58^{\circ}$$
 (int. $\angle s$, $TX // UQ$)
= 122°

(c) At the points W and X, draw two lines parallel to PR as shown,

$$T\hat{X}D = 180^{\circ} - 122^{\circ} \text{ (int. } \angle s, CD \text{ // } SV\text{)}$$

= 58°

$$\widehat{WXD} = 89^{\circ} - 58^{\circ}$$
$$= 31^{\circ}$$

$$\widehat{AWX} = 31^{\circ} \text{ (alt. } \angle s, AB \text{ // } \widehat{CD})$$

$$P\widehat{W}A = 42^{\circ} \text{ (alt. } \angle \text{s, } PR \text{ // } AB)$$

Reflex
$$P\hat{W}X = 360^{\circ} - 42^{\circ} - 31^{\circ}$$
 (\angle s at a pt.)
= 287°

14. (a)
$$\hat{BCD} = 43^{\circ}$$
 (alt. \angle s, $AB \text{ // }CD$)
 $(5x^{\circ} + 22^{\circ}) + 43^{\circ} = 360^{\circ}$ (\angle s at a pt.)
 $5x = 360 - 43 - 22$

$$3x = 300 - 43 - 2$$

$$= 295$$

$$x = \frac{295}{5} = 59$$

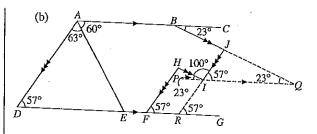
$$D\widehat{E}F = (x - 11)^{\circ}$$
$$= 59^{\circ} - 11^{\circ}$$

$$\hat{CDE} = 48^{\circ} \text{ (alt. } \angle \text{s, } \hat{CD} \text{ // } EF\text{)}$$

$$2y^{\circ} = 180^{\circ} - 48^{\circ}$$
 (adj. \angle s on a str. line)

$$2y=132$$

$$y = \frac{132}{2}$$



(i)
$$A\hat{D}E = 57^{\circ}$$
 (corr. \angle s, $AD // HF$)

$$D\widehat{A}B = 180^{\circ} - 57^{\circ} \text{ (int. } \angle s, AC // DG)$$

$$E\widehat{A}B = 123^{\circ} - 63^{\circ}$$

(ii) Draw line PQ through I parallel to AC. Produce BJ to Q and JI to R.

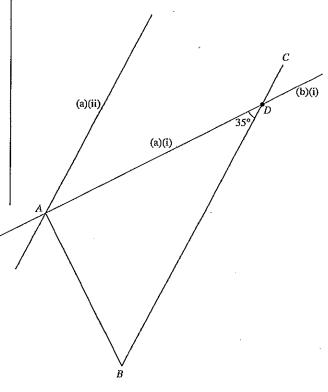
$$J\hat{Q}I = 23^{\circ}$$
 (alt. \angle s, $BC // IQ$)

$$\hat{HIP} = 23^{\circ} \text{ (corr. } \angle \text{s, } HI \text{ // } JQ)$$

$$I\widehat{R}G = 57^{\circ} \text{ (corr. } \angle \text{s, } HF \text{ // } IR\text{)}$$

$$J\hat{I}Q = 57^{\circ} \text{ (corr. } \angle s, IQ // RG)$$

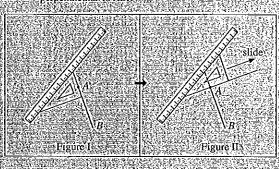
$$H\widehat{I}J = 180^{\circ} - 23^{\circ} - 57^{\circ}$$
 (adj. \angle s on a str. line)
= 100°



(b) (ii) BD = 7.85 cm $A\widehat{D}B = 35^{\circ}$

Teacher's:Tip

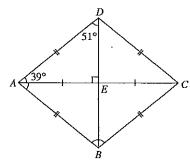
- To construct a line perpendicular to AB passing through
- (a) Place set square on line AB and ruler as shown in Figure I.
- (b) Slide set square along the length of the ruler until the edge of the set square passes through A as shown in Figure III: Draw the line passing through Aland perpendicular to AB



Test 14: Angle Properties of Trianglesand Quadrilaterals 🖘 🗄

Section A

1.

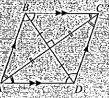


(a) $B\hat{A}E = D\hat{A}E$ $= 180^{\circ} - 51^{\circ} - 90^{\circ}$ = 39°

Since AE = EC, DEBis a diagonal. The diagonals of a rhombus bisect each other at right angles. $\bullet \equiv B\hat{A}E \equiv D\hat{A}E$ since the diagonal AC bisect

Teacher's Tip

- A rhombus is a parallelográm
- with all sides equal in length. 2. The diagonals bisect each other at right angles.
- Opposite angles are equal:
- The diagonals bisect the

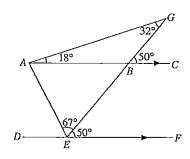


(b) $A\hat{B}C = A\hat{D}C$ $= 2 \times 51^{\circ}$

 $=102^{\circ}$

Opposite angles are equal.

2.



- (a) $B\widehat{E}F = 50^{\circ}$ (corr. $\angle s$, AC // DF)
- (b) $A\hat{G}B + 18^{\circ} = 50^{\circ}$ (ext $\angle = \text{sum of int. opp. } \angle s$) $A\hat{G}B = 50^{\circ} - 18^{\circ} = 32^{\circ}$
- (c) $E\widehat{A}B + A\widehat{E}F = 180^{\circ}$ (int. \angle s, $AC \parallel DF$) $E\hat{A}B + 67^{\circ} + 50^{\circ} = 180^{\circ}$ $E\hat{A}B = 180^{\circ} - 67^{\circ} - 50^{\circ}$ $= 63^{\circ}$

Teacher's Tip

- When two parallel lines are cut by a transversal?
 - (a) the corresponding angles are equal; ≈ a = b (corr. / ∠s, AB // CD)

 - (b) the interior angles are supplementary $b+c=180^\circ$ (int. $\angle s$; AB/II(CD)



The exterior angle of a triangle is equal to the sum of the interior opposite angles

 $\vec{b} + c$ (ext; $\angle ' = \text{sum'of int.' opp.} / \angle s$)



Since *BCDE* is a kite, BC = BE and $DC = DE^{\circ}$