

The word "Geometry" means "Earth Measure".

'Plane geometry' deals with the study of 2-dimensional (flat) figures. It deals with all of the properties and measurements associated with them. We study their shapes and sizes, and calculate lengths, angles and areas.

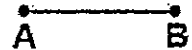
This section will also cover measurements for 3 dimensional figures (solids).

Geometric Terms and Figures:

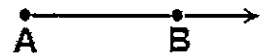
A point, P, has only position and has NO size.



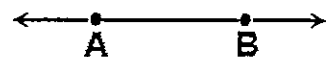
An interval, AB, is the shortest path between 2 points A and B.



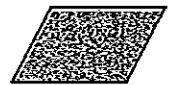
A ray, AB, is an interval extended infinitely in one direction.



A line, AB, is an interval extended infinitely in both directions.



A plane is a 2-Dimensional "flat" figure, which has an area.

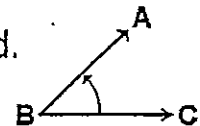


A solid is a 3-Dimensional object, which has a volume.



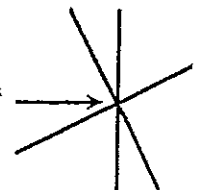
An angle  $\angle ABC$  is formed when an interval is rotated about one end.

- the rays BA and BC are called the "arms" of the angle.

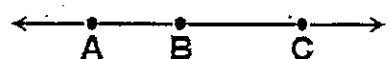


Two or more lines are said to be concurrent if they intersect (meet) at the one common point.

common point

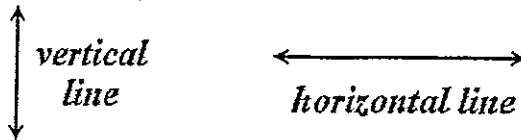


Points are said to be collinear if they are on the same line.

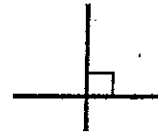


Types of Lines:

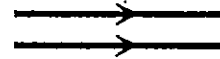
Vertical and horizontal lines:



Perpendicular lines – lines which meet at right angles ( $90^\circ$ ).



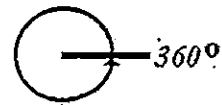
Parallel lines – lines which head in the same direction.  
Co-planar lines which never meet.



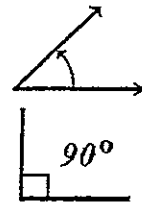
All measurements require a "unit of measurement" associated with them.  
For angles this is called the "degree" –  $360^\circ$  (degrees) make one revolution.

Types of Angles:

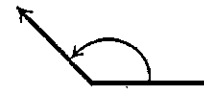
An acute angle – is an angle less than  $90^\circ$ .



A right angle – is a quarter of a revolution, i.e.  $90^\circ$ .



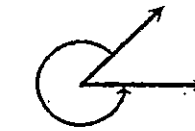
An obtuse angle – is an angle between  $90^\circ$  and  $180^\circ$ .



A straight angle – is half of a revolution. So it is  $180^\circ$ .



A reflex angle – is any angle between  $180^\circ$  and  $360^\circ$ .

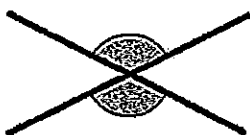


Adjacent angles – angles that are "next to" each other.

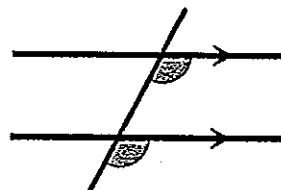


Complementary angles – add up to  $90^\circ$ . Supplementary angles – add up to  $180^\circ$ .

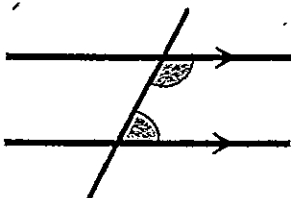
Vertically Opposite Angles are Equal



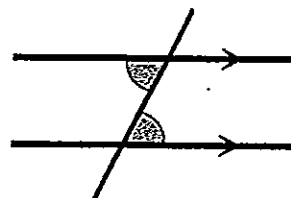
Corresponding Angles are Equal



Co-interior Angles are Supplementary

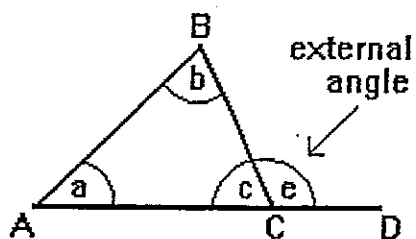


Alternate Angles are Equal



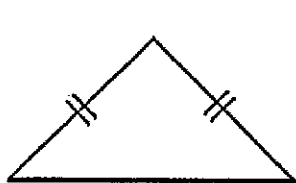
## PLANE FIGURES

### TRIANGLES

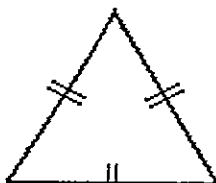


$$a+b+c=180^{\circ}$$

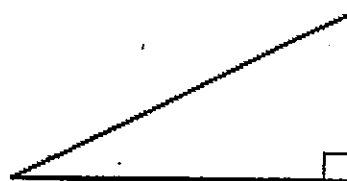
- ◆ Any three sided *closed* plane figure is called a triangle. ("tri" means "three" and thus "3 angles")
- ◆ The angle-sum of all triangles is  $180^{\circ}$ .
- ◆ The 3 angles formed inside a triangle are called internal angles.
- ◆ Any angle formed outside a triangle is called an external angle.
- ◆ There are a number of different types of triangles:-



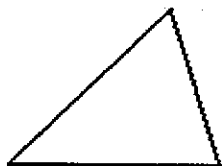
Isosceles triangle



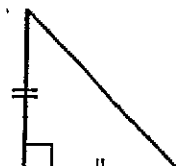
Equilateral triangle



Right angle triangle



Scalene triangle

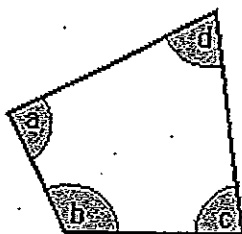


Right isosceles triangle



Obtuse angled triangle

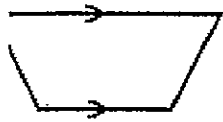
### QUADRILATERALS



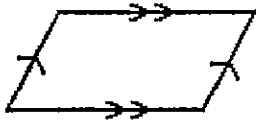
$$a+b+c+d=360^{\circ}$$

- ◆ Any four sided closed plane figure is called a quadrilateral. ("quad" means "four" and "lateral" means "sides")
- ◆ The angle-sum of all quadrilaterals is  $360^{\circ}$ .
- ◆ There are a number of different types of quadrilaterals:-

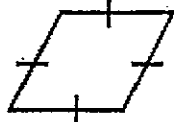
## Types of Quadrilaterals:



Trapezium



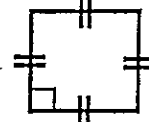
Parallelogram



Rhombus



Rectangle



Square



Kite

A trapezium has only one pair of parallel sides.

A parallelogram has 2 pairs of opposite sides parallel.

A rhombus has all 4 sides equal.

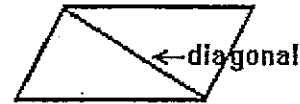
A rectangle has 2 pairs of parallel sides and a right angle.

A square has 4 sides equal and a right angle.

A kite has 2 pairs of adjacent sides equal.

The point where any 2 sides meet is called a vertex - (plural is "vertices").

A diagonal is any line that joins 2 vertices on opposite sides of the figure.



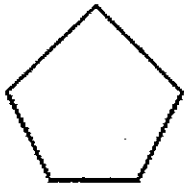
## POLYGONS

Plane figures made up of straight lines are called "polygons".

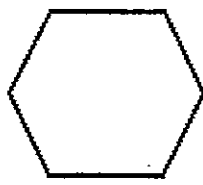
As the number of sides (intervals) varies so do their names.

If the polygon is a closed plane figure and all the sides and angles are equal, then it is called a regular polygon.

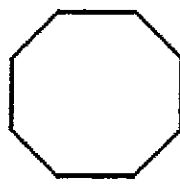
Some common polygons and their names are shown below:



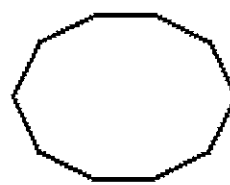
Pentagon



Hexagon



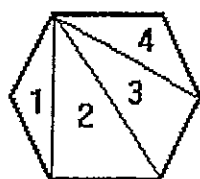
Octagon



Decagon

To calculate the sum of the internal angles of any polygon, join one vertex to all other vertices of the polygon, forming a number of triangles.

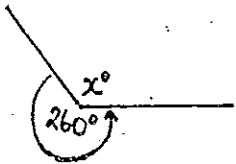
The angle-sum of the polygon then =  $180^\circ \times$  the number of triangles formed.



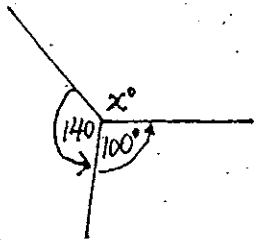
$$\begin{aligned} \text{Angle-sum} \\ &= 4 \times 180^\circ = 720^\circ \end{aligned}$$

LESSON 17 - HOMEWORK

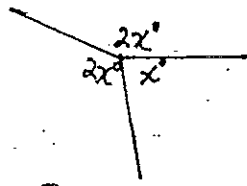
6992.T



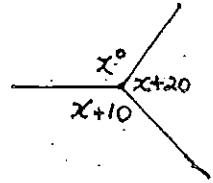
①  $x =$



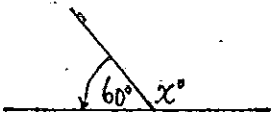
②  $x =$



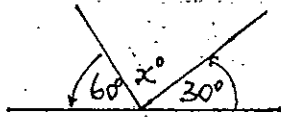
③  $x =$



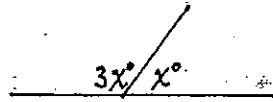
④  $x =$



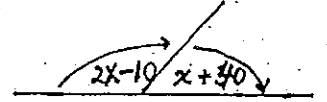
⑤  $x =$



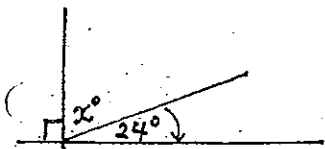
⑥  $x =$



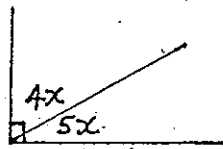
⑦  $x =$



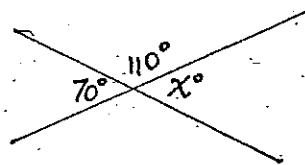
⑧  $x =$



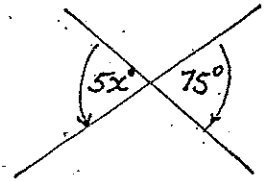
⑨  $x =$



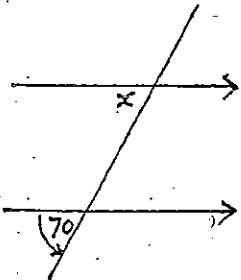
⑩  $x =$



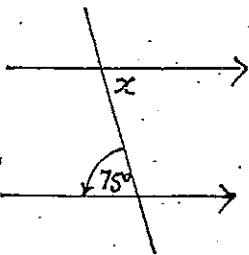
⑫  $x =$



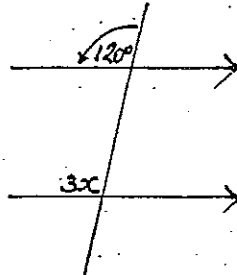
⑬  $x =$



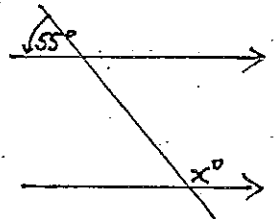
⑭  $x =$



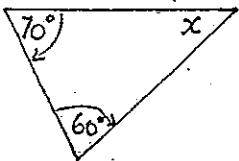
⑮  $x =$



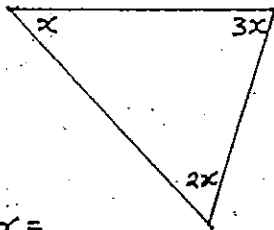
⑯  $x =$



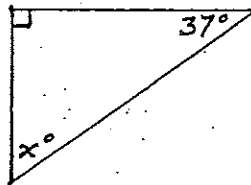
⑰  $x =$



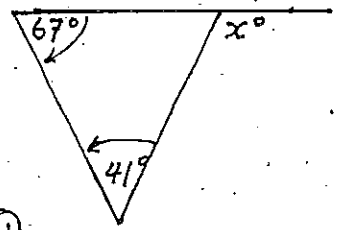
⑱  $x =$



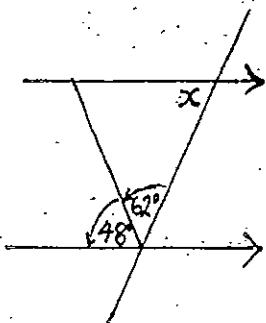
⑲  $x =$



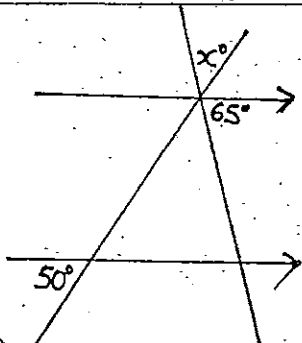
⑳  $x =$



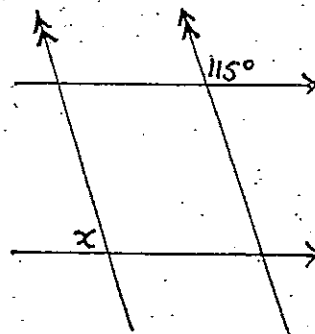
㉑  $x =$



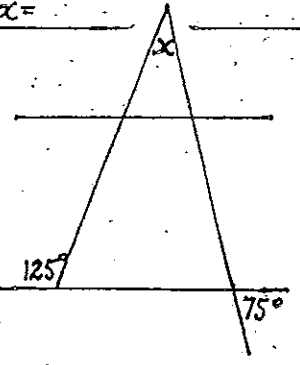
㉒  $x =$



㉓  $x =$



㉔  $x =$



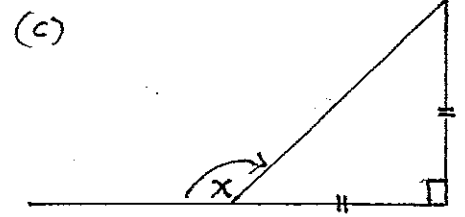
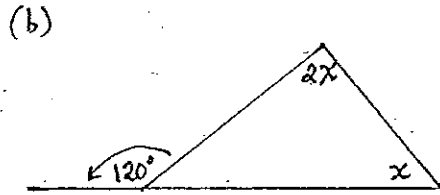
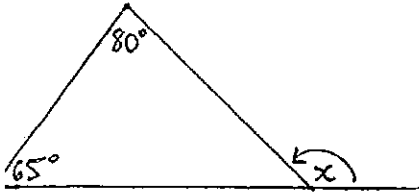
㉕  $x =$

ANSWERS

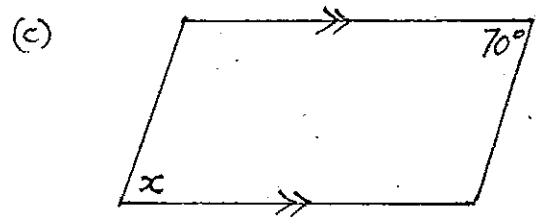
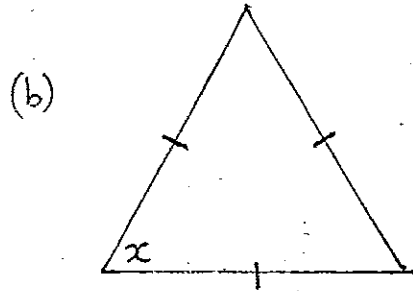
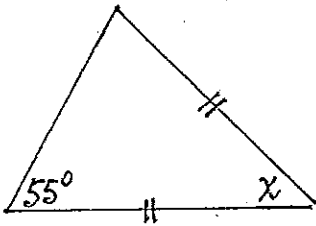
FIND  $x$  in all the above diagrams

- ①  $100^\circ$  ②  $120^\circ$  ③  $22^\circ$  ④  $110^\circ$  ⑤  $120^\circ$  ⑥  $90^\circ$  ⑦  $45^\circ$  ⑧  $50^\circ$  ⑨  $66^\circ$  ⑩  $10^\circ$  ⑪  $70^\circ$  ⑫  $70^\circ$  ⑬  $15^\circ$   
 ⑭  $70^\circ$  ⑮  $75^\circ$  ⑯  $40^\circ$  ⑰  $125^\circ$  ⑱  $50^\circ$  ⑲  $30^\circ$  ⑳  $53^\circ$  ㉑  $108^\circ$  ㉒  $70^\circ$  ㉓  $65^\circ$  ㉔  $65^\circ$  ㉕  $50^\circ$

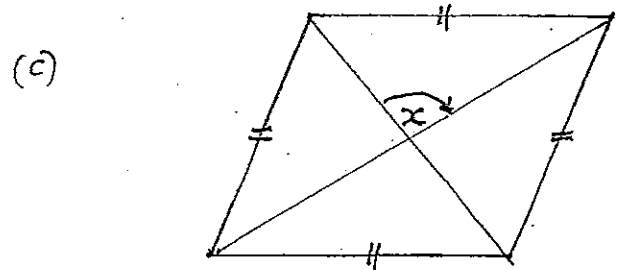
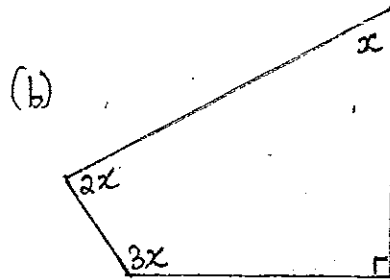
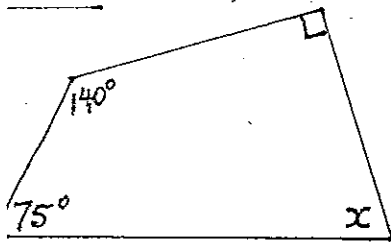
est ① - Find  $x$ .



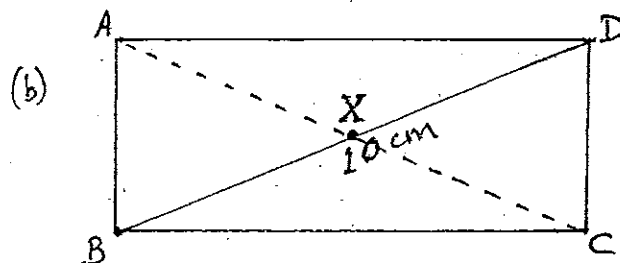
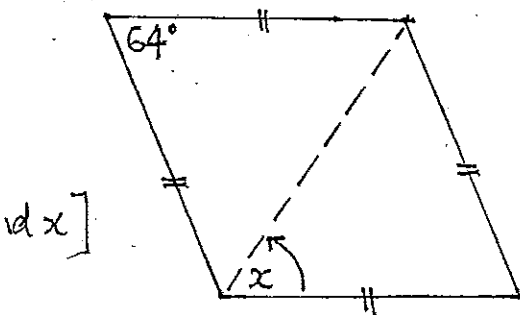
est ② - Find  $x$



est ③ - Find  $x$



est ④



ABCD is a rectangle  
AC meets BD at X  
BD = 10 cm

Find (i) BX (ii) AC

ANSWERS: ① a) 145° b) 40° c) 135°

② a) 70° b) 60° c) 70°

③ a) 55° b) 45° c) 90°

④ a) 58° b) (i) 5cm (ii) 10cm.

11-1 Angles on a Straight Line - total  $180^\circ$

WORKSHEET

Find the value of the pronumeral in the diagrams below:-

<p><u>Example</u></p> <p> <math>2m + 4m + 36 = 180</math>  <math>6m + 36 = 180</math>  <math>6m = 144</math>  <math>m = 24</math> </p>	a)		b)		c)	
	d)		e)		f)	
	g)		h)		i)	

11-2 Angles at a Point - total  $360^\circ$

Find the value of the pronumeral in each of the following:-

<p><u>Example</u></p> <p> <math>2p + 3p + 80 = 360</math>  <math>5p + 80 = 360</math>  <math>5p = 280</math>  <math>p = 56</math> </p>	a)		b)		c)	
	d)		e)		f)	

11-3 Vertically Opposite Angles - are equal. Determine the value of the pronumerals

a)		b)		c)		d)		e)		f)	
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11-4 Angles in a Triangle: total  $180^\circ$ . Find the value of the pronumeral in each case:

<p><u>Example</u></p> <p> <math>2p + 4p + 84 = 180</math>  <math>6p + 84 = 180</math>  <math>6p = 96</math>  <math>p = 16</math> </p>	a)		b)		c)	
	d)		e)		f)	
	g)		h)		i)	

ANSWERS: 11-1 a) 55° b) 40° c) 49° d) 105° e) 25° f) 45° g) 45° h) 46° i) 105° 11-2 a) 22.5° b) 65° c) 120° d) 44° e) 102.5° f) 25° 11-3 a) 85° b) 65° c) 22° d) 56° e) 20° f) 55° g) 60° h) 56.5° i) 30°

X TRANSVERSALS.

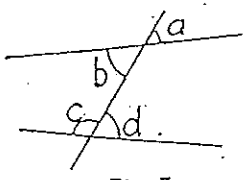


Fig. 7.

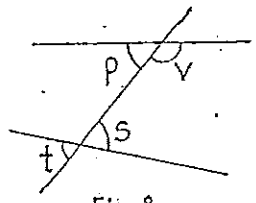
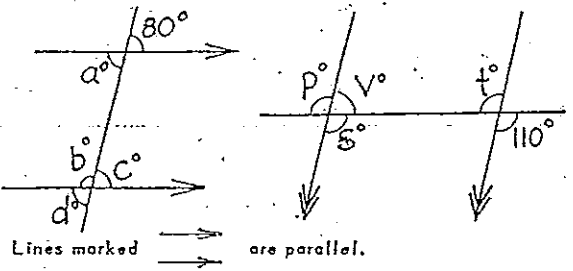


Fig. 8.

Place the appropriate pairs of letters opposite the name of the angles listed below.

- |                           | Fig. 7        | Fig. 8        |
|---------------------------|---------------|---------------|
| 57. ALTERNATE             | .....and..... | .....and..... |
| 58. CORRESPONDING         | .....and..... | .....and..... |
| 59. CO-INTERIOR or ALLIED | .....and..... | .....and..... |
| 60. VERTICALLY OPPOSITE   | .....and..... | .....and..... |
| 61. ADJACENT              | .....and..... | .....and..... |

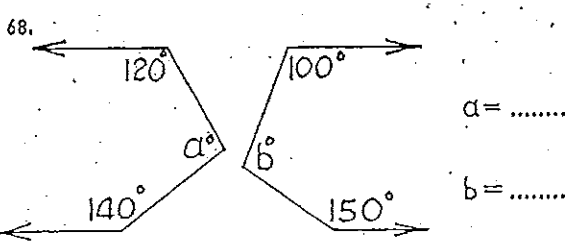
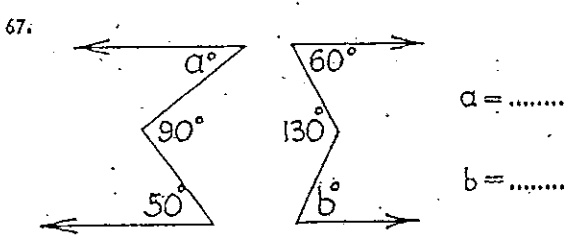
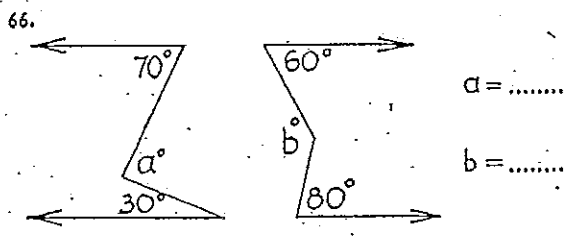
XI PARALLEL LINES PROBLEMS.



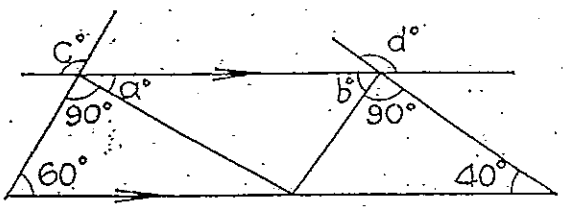
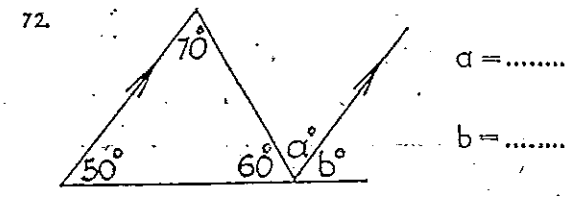
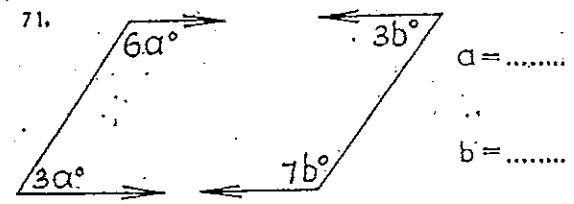
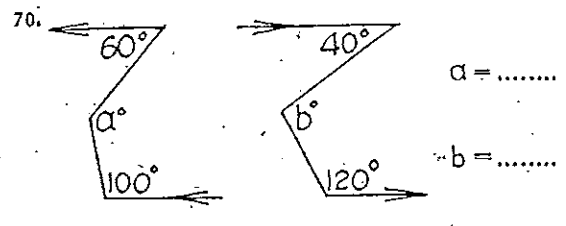
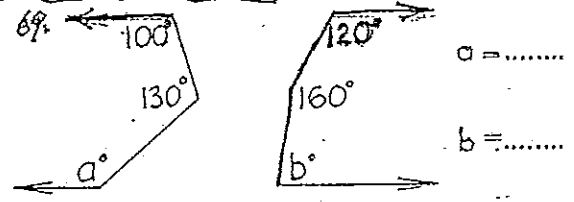
Write down the value of each of the following angles.

62.  $a = \dots\dots\dots$   $t = \dots\dots\dots$   
 63.  $b = \dots\dots\dots$   $v = \dots\dots\dots$   
 64.  $c = \dots\dots\dots$   $s = \dots\dots\dots$   
 65.  $d = \dots\dots\dots$   $p = \dots\dots\dots$

In questions 66 to 72 write down the value of  $a$  and  $b$ .

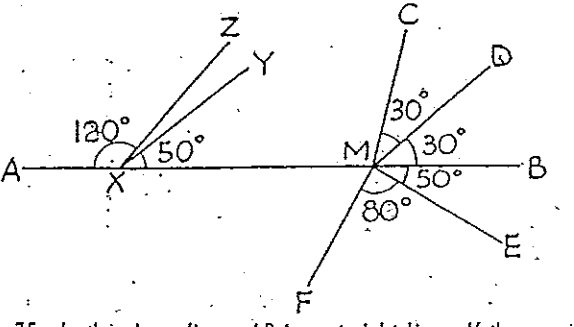


Class Exercises



Write down the value of each of the following angles.

73.  $a = \dots\dots\dots$   
 $b = \dots\dots\dots$   
 74.  $c = \dots\dots\dots$   
 $d = \dots\dots\dots$



75. In the above figure AB is a straight line. If the angles had been drawn accurately, which line would be parallel with  
 XY .....  
 XZ .....