

# Inequalities

## Exercise 5S Skills Practice

- 1 Solve each inequality.
- a  $3x - 1 < 14$       b  $2b + 6 \geq 10$       c  $2x + 3 > 4$   
 d  $4y + 11 \leq 3$       e  $3x - 7 > 1$       f  $9x - 20 < 43$   
 g  $3 + 2a \geq 14$       h  $5x + 2 \leq -1$       i  $8y - 15 > -1$   
 j  $13 - x < 22$       k  $5p + 9 \geq 7$       l  $15 - 3x \leq 11$
- 2 Find the set of values of  $x$  for which
- a  $4x > 3x + 5$       b  $7x - 8 \leq 3x$       c  $5x + 1 < 4x + 9$   
 d  $6x \leq 4x + 5$       e  $3(x + 2) > 9$       f  $5x - 4 \geq 7x$   
 g  $5(x + 3) < 8x$       h  $9x + 2 \leq 5x + 5$       i  $3x + 1 > 6x + 10$   
 j  $x - 3 \geq \frac{1}{2}x + 1$       k  $2(x + 4) < 3(3 - x)$       l  $9 - 2x > x + 6$   
 m  $6 - 2(5 - 3x) \leq 0$       n  $9 - 3x \geq 1 - 7x$       o  $7(2x + 3) - 5x < 9$
- 3 Solve each inequality.
- a  $(x - 3)(x - 5) < 0$       b  $(x - 3)(x - 5) > 0$       c  $(2x - 1)(x + 4) \leq 0$   
 d  $x^2 + 6x + 5 > 0$       e  $a^2 + 10a + 21 \geq 0$       f  $x^2 - 3x + 2 < 0$   
 g  $x^2 - 6x \geq 0$       h  $x^2 + x - 6 \leq 0$       i  $18 + 3y - y^2 > 0$   
 j  $2a^2 + 3a + 1 > 0$       k  $5x^2 - 11x + 2 \leq 0$       l  $b^2 + 21b + 108 < 0$   
 m  $3x^2 + 5x + 2 \geq 0$       n  $y^2 + 15y - 54 < 0$       o  $15 - 7x - 2x^2 \geq 0$
- 4 Solve each inequality, giving answers in surd form.
- a  $x^2 - 2x - 2 < 0$       b  $y^2 + 3y + 1 \geq 0$       c  $x^2 - 6x + 3 > 0$   
 d  $4 - b - 2b^2 \leq 0$       e  $x^2 - 8x - 4 \geq 0$       f  $5a^2 + 7a + 1 \leq 0$
- 5 Giving non-exact answers correct to 2 dp, find the set of values of  $x$  for which
- a  $x^2 + 9x + 20 > 0$       b  $x^2 - 2x < 3$       c  $x^2 - 5x + 1 \leq 0$   
 d  $6x^2 + 3x > 7$       e  $2x(4x - 5) + 3 \geq 0$       f  $x^2 < 3 - x$   
 g  $(x - 2)^2 > 5x - 4$       h  $2x(3 - x) \leq x - 12$       i  $x(7 - 2x) \geq (x + 1)^2$
- 6 Solve each inequality, giving non-exact answers in surd form.
- a  $4x(3x - 2) \geq 0$       b  $x^2 - 2 \leq \frac{1}{6}x$       c  $4 - b - \frac{1}{4}b^2 > 0$   
 d  $20y^2 - 43y + 14 \geq 0$       e  $\frac{1}{2}x(2 - x) < -60$       f  $6x^2 - 8x \leq 1$

### Exercise 5S Skills Practice

- 1 a  $x < 5$       b  $b \geq 2$       c  $x > \frac{1}{2}$       d  $y \leq -2$   
 e  $x > \frac{8}{3}$       f  $x < 7$       g  $a \geq \frac{11}{2}$       h  $x \leq -1$   
 i  $y > \frac{7}{4}$       j  $x > -9$       k  $p \geq -\frac{2}{5}$       l  $x \geq \frac{4}{3}$
- 2 a  $x > 5$       b  $x \leq 2$       c  $x < 8$       d  $x \leq \frac{5}{2}$   
 e  $x > 1$       f  $x \leq -2$       g  $x > 5$       h  $x \leq \frac{3}{4}$   
 i  $x < -3$       j  $x \geq 8$       k  $x < \frac{1}{5}$       l  $x < 1$   
 m  $x \leq \frac{2}{3}$       n  $x \geq -2$       o  $x < -\frac{4}{3}$
- 3 a  $3 < x < 5$       b  $x < 3, x > 5$       c  $-4 \leq x \leq \frac{1}{2}$   
 d  $x < -5, x > -1$       e  $a \leq -7, a \geq -3$   
 f  $1 < x < 2$       g  $x \leq 0, x \geq 6$   
 h  $-3 \leq x \leq 2$       i  $-3 < y < 6$   
 j  $a < -1, a > -\frac{1}{2}$       k  $\frac{1}{5} \leq x \leq 2$   
 l  $-12 < b < -9$       m  $x \leq -1, x \geq -\frac{2}{3}$   
 n  $-18 < y < 3$       o  $-5 \leq x \leq \frac{3}{2}$

<b>Exercise 5E   Exam Practice</b>
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- 1 a Solve the equation

$$y(y-3) = 10(y-4).$$

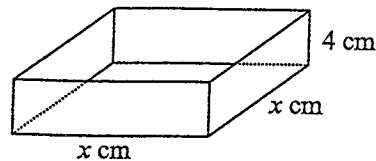
(3 marks)

- b Hence, or otherwise, find the set of values of  $y$  for which

$$y(y-3) \geq 10(y-4).$$

(2 marks)

2



The diagram shows an open-topped box in the shape of a cuboid of height 4 cm and with a square base of side  $x$  cm.

Given that the area of card used to make the box must be no more than  $192 \text{ cm}^2$ ,

- a write down an inequality that  $x$  must satisfy.

(3 marks)

Given also that the volume of the box must be greater than  $100 \text{ cm}^3$ ,

- b write down another inequality that  $x$  must satisfy.

(2 marks)

- c By solving your inequalities, find the set of possible values of  $x$ .

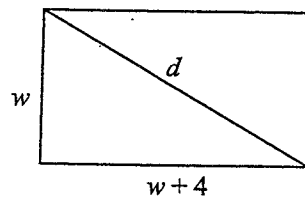
(5 marks)

- 3 Find the set of values of  $x$  for which

$$(2x-1)(x-3) < 6(x-2).$$

(5 marks)

4



The diagram shows a rectangular garden of width  $w$  metres and length  $(w+4)$  metres.

- a Show that if the length of the garden's diagonal is  $d$  metres, then

$$d^2 = 2w^2 + 8w + 16.$$

(2 marks)

Given also that  $d$  must be at least twice as big as  $w$ ,

- b show that the maximum value of  $w$  can be expressed in the form  $(a + b\sqrt{3})$  metres where  $a$  and  $b$  are integers to be found.

(6 marks)

<b>Exercise 5E   Exam Practice</b>
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1 a 5, 8   b  $y \leq 5, y \geq 8$

2 a  $x^2 + 16x \leq 192$    b  $4x^2 > 100$   
c  $5 < x \leq 8$

3  $\frac{3}{2} < x < 5$

4 b  $2 + 2\sqrt{3}$

<b>Exercise 5E   Exam Practice</b>
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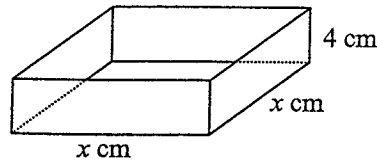
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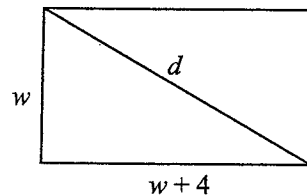
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- 3 Find the set of values of  $x$  for which

$$(2x-1)(x-3) < 6(x-2). \quad (5 \text{ marks})$$

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