Marcellin College Randwick



Year 11 Mathematics Preliminary Course Assessment Task #1 2007

Weighting: 10% of Preliminary Mark			
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STUDENT'S NAME:	and the second of the second o		

MARK: * /40

OUTCOMES:

- P1 Demonstrates confidence in using Mathematics to obtain realistic solutions to problems.
- P2 Provides reasoning to support conclusions which are appropriate to the context.
- P3 Performs routine arithmetic and algebraic manipulation involving surds, simple rational expressions.
- P4 Chooses and applies appropriate arithmetic and algebraic, techniques.

Time Allowed:

40 minutes

Directions:

Answer all questions

Show all necessary working

Marks may be deducted for poorly arranged or careless work

Begin each new question on a new page.

Structure:

2 questions each worth 20 marks

Question One: (20 marks)

a) Calculate the following to 3 significant figures:

$$\sqrt{\frac{6 \cdot 35^2}{26.7 - 14.3}}$$

b) Simplify:
$$\sqrt{75} + \sqrt{32} - \sqrt{27}$$

c) Express in simplest form with a rational denominator:

$$\frac{3}{\sqrt{2}+1} - \frac{2}{\sqrt{5}-2}$$

d) Expand where necessary and simplify:

$$(2a+1)(4a-1)-3a^2-2a+1$$

e) Factorise:

i)
$$100-4p^2$$

ii) a^3+1
ii) $3p^2+10p-25$

f) Simplify the following fractions;

i)
$$\frac{(a-b)^2}{10} \times \frac{5}{(a^2-b^2)}$$

ii)
$$\frac{6}{x+3} - \frac{3}{x^2+5x+6}$$

g) Express in simplest form without the use of negative indices:

$$(8x^6)^{\frac{1}{3}}x^{-3}$$

Question Two: (20 marks)

Solve for the unknown(s): a)

i)
$$30 - 8y = 70$$

ii)
$$\frac{9}{2x} = 4 - \frac{3}{x}$$

iii)
$$(2x-1)^2 = 36$$

iii) $x^2 - 7x + 12 = 0$

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- Show that $\frac{3+\sqrt{29}}{10}$ is a solution of the equation $5x^2-3x-1=0$ 3
- Solve and graph on a number line: c)

$$5(x-3) \ge 2(x+7)$$

d) Solve:

$$|4-2x|=x-2$$

3

The number of diagonals in a figure with n sides is given by e) $d=\frac{1}{2}n(n-3).$ How many sides has a figure with 20 diagonals.

QUESTION 1

c)
$$\frac{3(\sqrt{2}-1)}{(\sqrt{2}+1)(\sqrt{2}-1)} - \frac{2(\sqrt{5}+2)}{(\sqrt{5}-2)(\sqrt{5}+2)}$$

$$=\frac{3\sqrt{2}-3}{2-1}-2\sqrt{5}+4$$

$$= 3\sqrt{2} - 3 - (2\sqrt{5} + 4)$$

$$= 3\sqrt{2} - 7 - 2\sqrt{5}$$

$$8a^{2}+2a-1-3a^{2}-2a+1$$

$$= 5a^{2}$$

e)
$$4(25-p^2)$$

= $4(5+p)(5-p)$

$$= \frac{5(a-b)}{(6(a+b))} = \frac{a-b}{2(a+b)}$$

$$\frac{(ii)}{2+3} - \frac{3}{(x+2)(x+3)}$$

$$=\frac{6(x+2)}{(x+3)(x+2)}-\frac{3}{(x+2)(x+3)}$$

$$= \frac{6x+9}{(x+3)(x+2)}$$

$$=2\chi^2.\chi^{-3}$$

QUESTION 2

$$(ii) \frac{9}{2x} \times 2x = 4 \times 2x - \frac{3}{x} \times 2x$$

$$9 = 8x - 6$$

$$\therefore x = \frac{1 \pm 6}{2} \Rightarrow x = 3\frac{1}{2} \text{ or } -2\frac{1}{2}$$

- Solutions are
$$x = -(-3) \pm \sqrt{(-3)^2 4(5)(-1)}$$

2(5)

$$= 3 \pm \sqrt{29}$$

$$20 = \frac{1}{2}n(n-3)$$

$$40 = n^2 - 3n$$

$$0 = 11^2 - 311 - 40$$

$$0 = (n-8)(n+5)$$