

# Year 10 5.2/5.3 & 9 Acc Mathematics

Half Yearly Assessment, 2013

& SOLUTIONS

Total Marks:

86

Time allowed:

100 minutes

All questions-must be answered in a separate writing booklet Show all working to gain full marks

## Section A (23 marks)

Marked by HRK

2

#### START A NEW BOOKLET

1. Factorise and simplify

$$9-9(x+y)^2$$

$$\frac{y}{x} + \frac{2x-y}{x}$$

c. 
$$\frac{a^2 - 8a - ab + 8b}{b - a}$$

2. First factorise and then solve this quadratic equation 
$$5t^2 - 11t + 2 = 0$$

3. a. Factorise and solve 
$$x^2 - 4x - 21 = 0$$

**b.** Using your answer to part **a.**, find the solutions to the following equation 
$$(x+3)^2 - 4(x+3) - 21 = 0$$
 1

4. Complete this perfect square: 
$$x^2 - \frac{3}{7}x + \dots = ($$

5. Solve 
$$2x^2 - 10x - 3 = 0$$
 by completing the square.  
Give your answers correct to 2 decimal places.

6. Use the quadratic formula to solve 
$$x^2 + 6x + 2 = 0$$
 leaving your answer in simplest surd form.

- 7. The base of a triangle is 3cm longer than its height.

  If the area of the triangle is 35cm<sup>2</sup>
  - Draw a sketch showing this information clearly
  - Form a quadratic equation and solve it to find the height.

### START A NEW BOOKLET

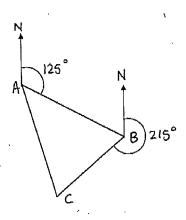
- A ladder of length 3 metres is leaning against a wall and is inclined at 62° to the ground.
  - a. Draw a diagram to represent this information.

1

- b. Calculate how far the ladder reaches up the wall. Round your answer correct to 2 dp. 1
- 2. Oscar drives 165km on a bearing of 145°. He then drives due west until he is due south of his starting point.
  - a. Draw a diagram illustrating this information.

1

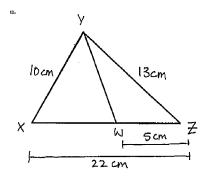
- Calculate how far he is from his starting point. Answer to the nearest kilometre.
- 3. David sails a ship from port A and travels 155 nautical miles to a lighthouse B on a bearing of 125°. He then sails 112 nautical miles to a port C on a bearing of 215°.



Find the bearing of Port C from Port A. Answer to the nearest degree.

3

4. Consider the following diagram:



**a.** Find the size of  $\angle YXZ$ . Correct to the nearest minute.

2

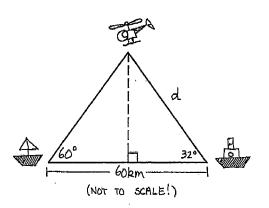
b. Find the length of YW. Correct to 1 decimal place.

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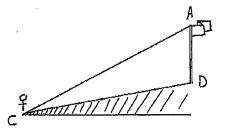
- 5. Two boats are situated at sea level 60 km apart. A helicopter is sighted simultaneously by the two boats where the angles of elevation of the helicopter from the boats at this time are 60° and 32°.
  - **a.** Find the length of distance d.

2

**b.** Find the altitude of the helicopter correct to the nearest 100 metres.



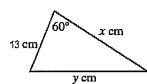
6. Blair is standing at C on a path that leads to the base D of a vertical flagpole. The path is inclined at 16° to the horizontal and the angle of elevation to the top A of the flagpole from C is 45°.



a. Explain why  $\angle ACD = 29^{\circ}$  and  $\angle CDA = 106^{\circ}$ 

2

- Given that CD is 30m, find the height of the flagpole. Answer to the nearest metre.
- 7. The area of this triangle is  $35\sqrt{3}$  cm<sup>2</sup>. Find the value of x and the exact value of y.



### START A NEW BOOKLET

1. Solve the following.
Show all necessary working to gain full marks.

a.  $\sin 2x = \cos 78^\circ$ 

2.

 $\mathbf{b.} \qquad \frac{5}{\sin \theta} = \frac{3}{\cos \theta}$ 

2

2. Prove  $\frac{\cos\theta\sin(90^\circ-\theta)}{\sin\theta\cos(90^\circ-\theta)} = \frac{1}{\tan^2\theta}$ 

2

3. Find the exact values of the following expressions, showing all working.

Ensure that your answer is a single fraction with a rational denominator.

Full marks will not be awarded if you use a calculator.

a.  $\sin^2 60^\circ$ 

2

**b.**  $2\sin 30^{\circ} - \cos^2 30^{\circ} + \tan 45^{\circ}$ 

<del>--</del>

c. cos 315°

2

d. tan 120°

2

4. Solve the following for  $0^{\circ} \le \theta \le 360^{\circ}$ .

**a.**  $\tan \theta = \frac{1}{\sqrt{3}}$ 

2

**b.**  $\sin \theta = -\frac{1}{2}$ 

2

 $2\cos^2\theta = 1$ 

4

## Section D (19 marks)

## Marked by TMS

#### START A NEW BOOKLET

1. Calculate the simple interest after 5 years of an investment of \$6400 at 7.5% p.a.

1

- Craig invests \$7900 at 5.25% p.a compound interest. Find the value of this investment after 6 years if the interest compounds yearly.
- Simon paid \$18 500 to buy equipment for his business. If the rate of depreciation is 15% p.a., find the value of the equipment after 7 years.
- 4. Peter buys a guitar with a cash price of \$9 800 on the following terms: 15% deposit with the balance paid at \$92.75 per week for 2 years.

  Assume there are 52 weeks in one year.

#### Calculate:

a. the deposit.

1

**b.** the balance owing.

1

the total cost of the guitar.

1

d. the total interest paid on the loan.

1

- James invests \$12800 at 12% p.a compound interest. Find the value of this investment after 4 years if the interest compounds quarterly.
- How much do you need to invest today at 5.2% p.a. annually compounding interest, to have \$16 000 in 3 years?

Express your answer correct to the nearest dollar.

2

- Jess deposited \$11 500 in a savings account. After 3 years he had earned \$1250 in simple interest. Find the annual interest rate correct to one decimal place.
- 8. Use the table below to answer the following questions. Show all working.

Monthly repayment per \$1000 borrowed.

	Interest Rate (p.a.)						
Term	6%	7%	8%	9%	10%	11%	
6	\$16.57	\$17.05	\$17.53	\$18.03	\$18.53	\$19.03	
7	\$14.61	\$15.09	\$15.59	\$16.09	\$16.60	\$17.12	
8	\$13.14	\$13.63	\$14.14	\$14.65	\$15.17	\$16.25	
9	\$12.01	\$12.51	\$13.02	\$13.54	\$14.08	\$14.63	
10	\$11.10	\$11.61	\$12.13	\$12.67	\$13.22	\$13.78	
11	\$10.37	\$10.88	\$11.42	\$11.96	\$12.52	\$13.09	

Amelia borrows \$190 000 over 10 years at 9% p.a. to purchase a house.

a. How much will Amelia repay altogether on this loan?

1

**b.** How much interest will she pay?

1

c. Calculate the flat yearly interest rate, correct to 2 decimal places.

places. 2

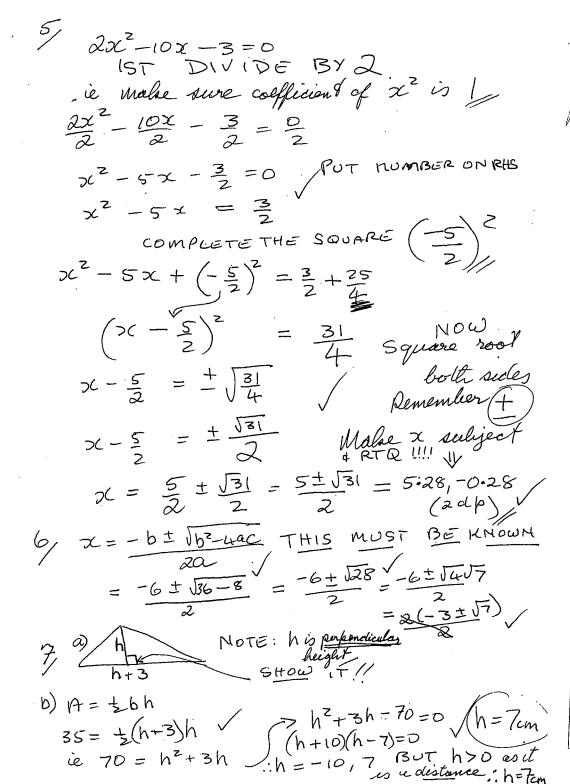
 A motor bike was purchased for \$5600 and 5 years later its value had depreciated to \$2900. Find the annual rate of depreciation.

SECTION A (23 MARKS) V=IMARIL DIFF OF 2 SQUARES BUT ... take out any (a) 9-9(x+y)2  $\int = 9\left(1 - \left(61 + 4\right)^2\right)$ Common factors FIRST - NO MATTER WHAT IT = 9 (1 - (x+y)) (1+(x+y)) looks like/leads to.  $\int_{0}^{\pi} 9 \left(1-x-y\right)\left(1+x+y\right)$ FIRST FACTORISE b)  $\frac{y}{x^2 - xy} + \frac{2x - y}{x^2 - 2xy + y^2}$ BOTH DENOMINATORS PUT ON LOWEST CI  $= \sqrt{\frac{y}{x(x-y)}} + \frac{2x-y}{(5x-y)^2}$ = (x-y)y + x(zx-y)x (x-y)2  $= \frac{x/y - y^2 + 2x^2 - xy}{3c(x - y)^2}$  $= 2x^2 - y^2$  $\sqrt{x(x-y)^2}$ 4 terms - do 2 AT ATIME c) a2-8a-ab+86  $= \frac{a(a-8) - b(a-8)}{b-9}$ NOTE: b-a=-(a-b) $= \frac{(a-8)(a+b)}{-1(a+b)}$ then denom. is -1  $=\frac{a-8}{-1}$  = -a+8 or  $8-a_{y}$ 

THE QUESTION WZ KTO READ If you do not factorise FIRST FACTORISE you will lose moras! 5t2-11t+2=0 (5t-1)(1-2)=0 t= 5,2 Q3a) RTQ AGAIN ... IN FACT EVERY TIME!!!  $x^{2}-4x-21=0 / (x-7)(x+3)=0$  x=7,-3b) & AGAIN RTO! using (a) (2+3)-4(x+3-21-0 NOTE SAME PATTERH !! 3(+3=7) on x+3=-3SO HERE x = -6 / 94 RTQ/MUST FOLLOW QUESTION REQUEST To complete the square we add the square of I the coefficient of X HERE (-3) noting = = -3  $\therefore x^{2} - \frac{3}{7}x + \left(-\frac{3}{4}\right)^{2} = \left(x - \frac{3}{4}\right)^{2}$ OBSERVE THAT BY LEAVING THE HALF of

-3 ie -3 we have exactly what

must go in the bracket





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Teacher Initials

SECTION	8	SOLUTIONS

# ASSESSMENT WRITING BOOKLET

Subject:	Y0 10	V. 4. C				
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Start here.	
out not.	
(1a)	
3,10	
×	
700° -	(/)
(1b) Sin 62 = 2e	
3	
35in62 = 2e	
$\alpha = 2.65 \text{m}$	$(\checkmark)$
2a) (45°	
10 165km	
. * 1	
17 W	( <b>/</b> )

tart here. 0=120-145 ~ 3s° 605: 35° = 22 145 x= 165 ws35 135 KM 125° 2150 0 = 180 - 125 = 550 K = 360-55-215 = 90" SOH CAN TOA SINLE 155 β = 35° 52'

Bearing of C from A is 125°+ 35°51'
= 161°. (V)
(4a)
10 / 13
X - 2
17cm W Son
2-2 cm
$\cos C = q^2 + b^2 - c^2$
$\omega SX = 10^{2} + 22^{2} - 13$
2 (10)(22)
= 19°24'
(b) $(^2 = 9^2 + b^2 - 2ab \omega SC)$ $Xw = 22 - S$
Yw = 10 + 17 = - 2(10)(17) ws190 = 17cm; (V)
Yw= 68
Yw = 8.165
= 8.3  cm
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Start here.	
5a) Latheliopher = 180-60-32	
= 23° 5	
d _ 60 (V)	A
sin60 sin88	82.
d = 605in60	/ ln d
sin 88	320
d = 51.993	600
= 52 km (/)	60
- See Brief A I	
si) : 200 - h	( 🗸 )
56) si va 32° = h 32	
h = 52 sin32	
21, 23 pw	. (/)
= 27600 m or 27.6	km (V)
	<u> </u>
(6) LACO = 43-16 adjacent	( ()
= 29° (L mm)	( \( \)
LCDA = 180-294-LCAD	
₩	:
180-4	5 = 45
LCDA = 180-29-45	/\
= 106° (2 sum of 1)	( \(  \)
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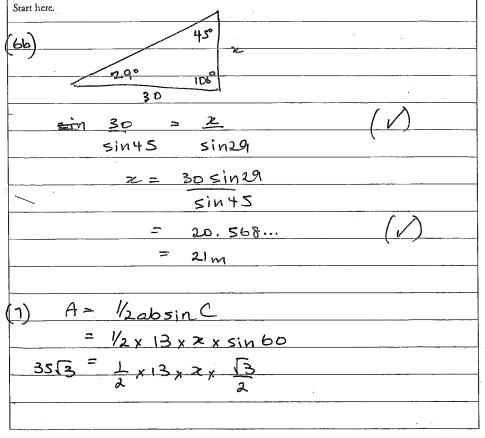


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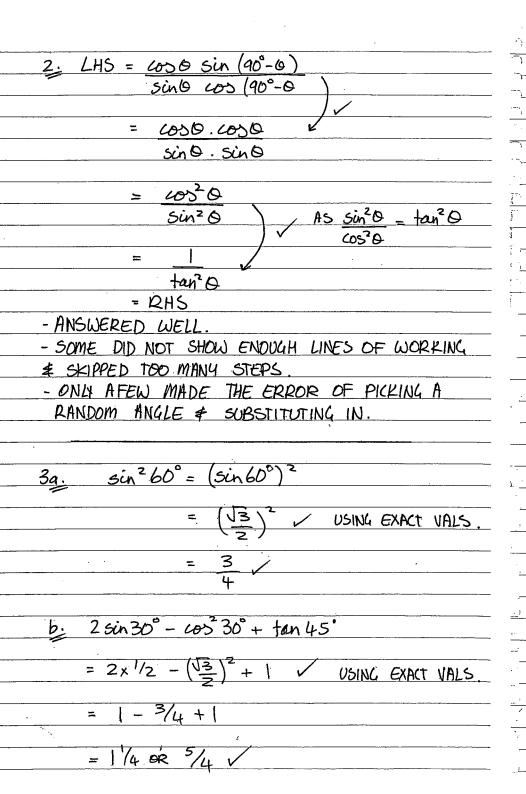
## ASSESSMENT WRITING BOOKLET

Subject:



Start here.
35(B = 13(B × (+13)
4
· >== 1010 cm (1)
$y^2 = 13^2 + (1019/3)^2 - 2 \times 13 \times 10^{19}/3 \times cos60^9$
y = 10297 12.04
y = 62.97 (12.04

7	SECTION C.
)	$lg. \sin 2x = \cos 78^{\circ}$
	$78^{\circ} + 2x = 90^{\circ} \checkmark$ complementary Ls.
· — —	$18 + 2x = 10        \text{ $
100	x = 6° /
<u>j</u> .	
	b: 5 = 3 × BOTH SIDES BY SiA O
	Sin O COSO
	·
- <del>)                                   </del>	$5 = 3 \sin 0 - Both B4 3$
, ———	(0)0
1	$\frac{5}{3} - \frac{\sin \Theta}{\cos \Theta} = \frac{\sin \Theta}{\cos \Theta}$
	2 2036
*	$\frac{5}{3}$ = tano $\sqrt{}$
	•
•	$0 = \tan^{-1}(\frac{5}{3})$ = 59°2' \(\nu\)
•	= 312
- 1	- NOT ANSWERED PARTICULARLY WELL.
	- MANY HAD NO IDEA WHAT TO DO. PLEASE REVIEW
T	CLASS EXERCISES IN YOUR STUDY.
	- SLOPPINESS WITH NOTATION (ie 6 NOT 6°) WAS
: 	COMMON.
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: 	
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<u> </u>	
<u></u>	
J	***



C: 
$$COD 315^{\circ} ... IN Q4 : tve$$
.

 $315^{\circ} = 360^{\circ} - 6$ 
 $\therefore O = 45^{\circ}$ 
 $COD 45^{\circ} = COD 315^{\circ} = \frac{1}{\sqrt{2}} OR \sqrt{2}$ 

(LEEWAY WAS GIVEN FOR LEAVING  $\frac{1}{\sqrt{2}}$  WITH AN IRRATIONAL DENOM.)

d:  $tan 120^{\circ} ... IN Q2 : -ve$ .

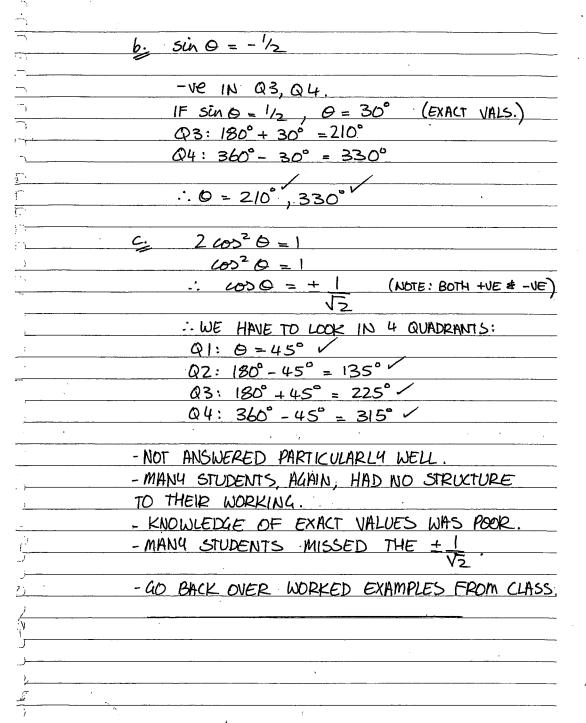
 $120^{\circ} = 180^{\circ} - 0$ 
 $\therefore 6 = 60^{\circ}$ 
 $tan 60^{\circ} = \sqrt{3}$ 
 $\therefore tan 120^{\circ} = -\sqrt{3}$ 

- MANY SHOWED THAT THEY REALLY DID NOT UNDERSTAN THE METHOD FOR 'ANGLES OF ANY MAGNITUDE' \$\frac{1}{2}\$ WENT STRAIGHT TO THEIR CALC.

- WORKING OUT WAS GENERALLY PROPELY SET OUT OR MISSING.

 $tan Q = \frac{1}{\sqrt{2}}$ 
 $tan Q = \frac{1}{\sqrt{2}}$ 
 $tan Q = 30^{\circ}$  (FROM EXACT VALS.)
 $tan Q3: 180^{\circ} + 30^{\circ} = 210^{\circ}$ 

.: 0 = 30°, 210° /





-			Т	each	er In	itials	;

SECTION	D.		
			 Student Name

## ASSESSMENT WRITING BOOKLET

Subject:	•		

Qu7. I-PRT
\$1250 = \$11500×R×3
1250 = 34500R
R = 34500
R = 0.0362
: Interest Rate - 3.6 % p.a.
Ond. (a) Total repayment: 512.67 ×190×12×10
= \$ 238 876
(b) Interest = \$288 376 - 190000
= \$98876 V
(c) Interest hate = \$98876 = 10
190000
25.2%
Ong. V: P(1-R)
2900 = 5600(1-R)5
3400 - (1-R)5
5/1900 - 1-R
R = 1 - 5 2900 5600
,
R > 0.12331
Interest rate = 12.3%
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Start here.
Notes
It was common for students
to round off to the nearest
dollar, even when not asked.
# On 7 and On 9 were poorly.
done. Students struggled to
solve the equation once they
had correctly substituted the
correct values in the formula.
ie: solving: \$2900: 5600(1-R)5
and
1250 : 11500× RX3
,