

NAME : \_\_\_\_\_



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## YEAR 12 – EXT. 1 MATHS

### REVIEW TOPIC (SP1)

### ANGLE BETWEEN LINES & RATIO FORMULA

CEM – Yr 12 – 3U Division of Lines, Angle Between Lines – Review Paper 1

- Let  $A$  be the point  $(-3, 8)$  and let  $B$  be the point  $(5, -6)$ . Find the coordinates of the point  $P$  that divides the interval  $AB$  internally in the ratio  $1:3$ .
  - Find the obtuse angle between the lines  $3x - y + 5 = 0$  and  $2x + 3y - 1 = 0$ . Give your answer correct to the nearest degree.

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3. Find the acute angle between the lines  $2x - y = 0$  and  $x + 3y = 0$   
giving the answer correct to the nearest minute.

4.  $A$  is the point  $(-2, -1)$ ,  $B$  is the point  $(1, 5)$ . Find the coordinates  
of the point  $Q$  which divides  $AB$  externally in the ratio  $5 : 2$ .

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5. The interval  $AB$ , where  $A$  is  $(2,1)$  and  $B$  is  $(3,2)$  is divided internally in the ratio  $4:3$  by the point  $P(x,y)$ . Find the values of  $x$  and  $y$ .
6. The point  $P(-3,8)$  divides the interval  $AB$  externally in the ratio  $k:1$ . If  $A$  is the point  $(6,-4)$  and  $B$  is the point  $(0,4)$ , find the value of  $k$ .

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7. The point  $P$  divides the line  $AB$  externally in the ratio  $3:2$ .  
Find  $P$  if  $A$  is  $(2, -5)$  and  $B$  is  $(6, 1)$ .

8. The interval  $AB$ , where  $A$  is  $(2,1)$  and  $B$  is  $(3,2)$  is divided internally  
in the ratio  $4:3$  by the point  $P(x,y)$ . Find the values of  $x$  and  $y$ .

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9. Find the acute angle between the lines  $3x - y - 2 = 0$  and  $x + 2y - 3 = 0$ .  
Give the answer correct to the nearest degree.

10. Find the coordinates of the point that divides H(-3,4) and K(9,-6) externally in the ratio of 3:5.

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Answers

1.  $\textcircled{1} (-3, 8) \quad (5, -6)$   $\leftarrow$   $m_1 = 3$       2.  $3x - y + 5 = 0 \quad 2x + 3y - 1 = 0$   
 $\times$   $m_2 = -\frac{2}{3}$

$$m = \frac{3(-3) + 1(5)}{1+3}, \quad \frac{3(8) + 1(-6)}{1+3} \quad \textcircled{1}$$

$$= \left( -\frac{4}{4}, \frac{18}{4} \right)$$

$$= (-1, 4\frac{1}{2}) \quad \textcircled{1}$$

$$\tan \theta = \left| \frac{3 + \frac{2}{3}}{1 + 3(-\frac{2}{3})} \right|$$

$$\theta = 75^\circ$$

$\therefore$  obtuse angle =  $105^\circ$

3.  $2x - y = 0$        $x + 3y = 0$   
 $y = 2x \therefore m_1 = 2$        $y = -\frac{x}{3} \quad m_2 = -\frac{1}{3}$   
 $\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right|$   
 $= \left| \frac{2 + \frac{1}{3}}{1 + 2 \times -\frac{1}{3}} \right|$   
 $= \left| \frac{2\frac{1}{3}}{-\frac{1}{3}} \right|$   
 $= 7$   
 $\therefore \theta = 81^\circ 51' \text{ (to nearest min)}$

4. A(-2, -1), B(1, 5)

$$\begin{aligned} & \text{mid} \\ & 5:-2 \quad Q \left( \frac{m_2 x_1 + m_1 x_2}{m_1 + m_2}, \frac{m_2 y_1 + m_1 y_2}{m_1 + m_2} \right) \\ & = \left( \frac{5 \times 1 - 2 \times -2}{5 - 2}, \frac{5 \times 5 - 2 \times -1}{5 - 2} \right) \\ & = \left( \frac{9}{3}, \frac{27}{3} \right) \\ & = (3, 9) \end{aligned}$$

5.  $x = n\frac{x_1 + mx_2}{m+n} \quad y = \frac{ny_1 + my_2}{m+n}$   
 $x = \left( \frac{3(2) + 4(3)}{7} \right), \quad y = \left( \frac{3(1) + 4(2)}{7} \right)$   
 $x = \left( \frac{6+12}{7} \right) \quad y = \left( \frac{3+8}{7} \right)$   
 $x = \frac{18}{7} \quad y = \frac{11}{7}$   
 $\therefore P \left( \frac{18}{7}, \frac{11}{7} \right) \quad \textcircled{2}$

6. The coordinates of P are given by

$$x_p = \frac{kx_2 + lx_1}{k+l}, \quad y_p = \frac{ky_2 + ly_1}{k+l}$$

$$-3 = \frac{k(0) + l(6)}{k+(-1)} \quad \checkmark$$

$$-3 = \frac{-6}{k+1}$$

$$-3(k+1) = -6$$

$$-3k - 3 = -6$$

$$-3k = -9$$

$$\therefore k = 3$$

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7. d) A(2,5) B(6,1)

$$\left( \frac{3 \times 6 + -2 \times 2}{1}, \frac{3 \times 1 + -2 \times 5}{1} \right) = (14, 13)$$

8.

$$x = n \frac{x_1 + mx_2}{m+n} \quad y = n \frac{y_1 + my_2}{m+n}$$

$$x = \left( \frac{3(2) + 4(3)}{7} \right) \quad y = \left( \frac{3(1) + 4(2)}{7} \right)$$

$$x = \left( \frac{6+12}{7} \right) \quad y = \left( \frac{3+8}{7} \right)$$

$$x = \frac{18}{7} \quad y = \frac{11}{7}$$

$$P\left(\frac{18}{7}, \frac{11}{7}\right)$$

(2)

9.

$$\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right|$$

↙

$$\begin{aligned} m_1 &= \frac{-y_2 - 3x_2}{y_2 - 3x_2} & m_2 &= \frac{2y_2 - -x_2}{y_2 - -x_2} \\ &= \frac{-y_2 - 3x_2}{y_2 - 3x_2} & &= \frac{2y_2 + x_2}{y_2 + x_2} \\ &= -3 & &= \frac{1}{2} \\ & \left| \frac{-3 - \frac{1}{2}}{1 + (-3) \cdot \frac{1}{2}} \right| & = \left| \frac{\frac{7}{2}}{-\frac{1}{2}} \right| & = \left| -7 \right| & = 7 \end{aligned}$$

10.

$$\begin{array}{c} 3 \qquad -5 \\ \hline (-3, 4) \qquad (9, -6) \end{array}$$

$$\left( \frac{-5x-3+3x-9}{3+(-5)}, \frac{-5x+3x-6}{3+(-5)} \right)$$

$$(-21, 19)$$