

# C.E.M. TUITION

Name : \_\_\_\_\_

**Review Paper No. 2**

**Basic Arithmetic & Algebra**

**Year 11 - 2 Unit**

1. Factorise

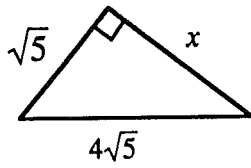
(i)  $x^2 - y^2 + 2x + 2y$

(ii)  $2x^3 + 54$

2. Simplify  $\frac{x}{x-1} - \frac{2}{x+1} - \frac{2}{x^2-1}$

3.

Figure 1.2



Use Pythagoras' Theorem to find the value of  $x$  in simplest exact form.

4. If  $S = \frac{a(r^n - 1)}{r - 1}$  find the value of  $S$  in simplest exact form when  $a = 2$ ,  $n = 4$ ,  $r = \sqrt{3}$ .

5. Solve simultaneously

$$x + 4y - 11 = 0$$

$$3x - 2y + 9 = 0$$

6. Solve

(i)  $|2x - 1| = 4 - 3x$

(ii)  $-2 < 3 - x \leq 4$

7. Solve  $\frac{x}{x+2} = \frac{3}{x+4}$ .

8. In a rectangle of area  $4 \text{ cm}^2$  the width is  $x \text{ cm}$  and the length is  $2 \text{ cm}$  longer than the width.
- (i) Show that  $x^2 + 2x - 4 = 0$ .
  - (ii) Find the dimensions of the rectangle in simplest exact form.

$$\begin{aligned}
 1. \quad (i) \quad & x^2 - y^2 + 2x + 2y \\
 & = (x-y)(x+y) + 2(x+y) \\
 & = (x+y)(x-y+2)
 \end{aligned}$$

$$\begin{aligned}
 (ii) \quad & 2x^3 + 54 = 2(x^3 + 3^3) \\
 & = 2(x+3)(x^2 - 3x + 9)
 \end{aligned}$$

$$\begin{aligned}
 2. \quad & \frac{x}{x-1} - \frac{2}{x+1} - \frac{2}{x^2-1} \\
 & = \frac{x(x+1) - 2(x-1) - 2}{(x-1)(x+1)} \\
 & = \frac{x^2 - x}{(x-1)(x+1)} \\
 & = \frac{x(x-1)}{(x-1)(x+1)} \\
 & = \frac{x}{x+1}
 \end{aligned}$$

3. Using Pythagoras' Theorem,

$$\begin{aligned}
 x^2 + (\sqrt{5})^2 & = (4\sqrt{5})^2 \\
 x^2 + 5 & = 16 \times 5 \\
 x^2 & = 75 \\
 x & = 5\sqrt{3}
 \end{aligned}$$

4.  $a=2$ ,  $n=4$ ,  $r=\sqrt{3}$

$$\begin{aligned}
 S & = \frac{a(r^n - 1)}{r - 1} \\
 & = \frac{2((\sqrt{3})^4 - 1)}{\sqrt{3} - 1} \\
 & = \frac{2(9 - 1)}{\sqrt{3} - 1} \\
 & = \frac{16(\sqrt{3} + 1)}{(\sqrt{3} - 1)(\sqrt{3} + 1)} \\
 & = \frac{16(\sqrt{3} + 1)}{3 - 1} \\
 & = 8(\sqrt{3} + 1)
 \end{aligned}$$

$$\begin{aligned}
 5. \quad & x + 4y - 11 = 0 \quad (1) \\
 & 3x - 2y + 9 = 0 \quad (2)
 \end{aligned}$$

Take  $(1) + 2 \times (2)$  to eliminate  $y$ :

$$\begin{aligned}
 & x + 4y - 11 = 0 \\
 \oplus & 6x - 4y + 18 = 0 \\
 \hline
 & 7x + 7 = 0 \\
 & x = -1
 \end{aligned}$$

Substitute for  $x$  in (1):

$$\begin{aligned}
 & 4y - 12 = 0 \\
 & y = 3 \\
 \therefore & x = -1, \quad y = 3
 \end{aligned}$$

6. (i)  $|2x - 1| = 4 - 3x$   
 Since  $LHS \geq 0$ ,  $RHS \geq 0$ . Noting this restriction on  $x$ , we can square both sides.

$$\begin{aligned}
 3x \leq 4 \quad \text{and} \quad (2x - 1)^2 & = (4 - 3x)^2 \\
 (2x - 1)^2 - (4 - 3x)^2 & = 0 \\
 (3 - x)(5x - 5) & = 0
 \end{aligned}$$

$$\begin{aligned}
 (3 - x)(x - 1) & = 0 \\
 \therefore x \leq \frac{4}{3} \quad \text{and} \quad \{x = 3 \text{ or } x = 1\} \\
 \therefore x & = 1
 \end{aligned}$$

$$\begin{aligned}
 (ii) \quad & -2 < 3 - x \leq 4 \\
 & -5 < -x \leq 1 \\
 & 5 > x \geq -1 \\
 & -1 \leq x < 5
 \end{aligned}$$

$$\begin{aligned}
 7. \quad & \frac{x}{x+2} = \frac{3}{x+4} \\
 x(x+4) & = 3(x+2), \quad x \neq -2, \quad x \neq -4 \\
 x^2 + 4x & = 3x + 6 \\
 x^2 + x - 6 & = 0 \\
 (x+3)(x-2) & = 0 \\
 \therefore x & = -3 \quad \text{or} \quad x = 2
 \end{aligned}$$

8. The sides are  $x$  and  $x+2$ .

$$\begin{aligned}
 (i) \quad \text{Area is } 4 & \Rightarrow x(x+2) = 4 \\
 & x^2 + 2x = 4 \\
 & x^2 + 2x - 4 = 0
 \end{aligned}$$

(ii) Using the quadratic formula :

$$x = \frac{-b \pm \sqrt{\Delta}}{2a}$$

$$\left. \begin{array}{l} a=1 \\ b=2 \\ c=-4 \end{array} \right\} \Rightarrow \begin{array}{l} \Delta = b^2 - 4ac \\ = 4 - 4(-4) \\ = 20 \end{array}$$

$$\sqrt{\Delta} = 2\sqrt{5}$$

$$x = \frac{-2 \pm 2\sqrt{5}}{2}$$

$$x = \frac{2(-1 \pm \sqrt{5})}{2}$$

$$\therefore x = -1 + \sqrt{5} \text{ or } x = -1 - \sqrt{5}$$

But  $x$  cm is a length  $\Rightarrow x \geq 0$

$$\therefore x = -1 + \sqrt{5}, \quad x + 2 = 1 + \sqrt{5}$$

Hence the dimensions are

$(-1 + \sqrt{5})$  cm by  $(1 + \sqrt{5})$  cm.