

C.E.M. TUITION

Name : _____

HSC PROOFS

2/3 Unit

TUTOR : PETER OOI

PHONE : 9666-3331

FAX : 9316-4996

2 Unit

Sequence and Series

- [1] A sequence in arithmetic progression is in the form $a, a + d, a + 2d, \dots, a + (n - 1)d$
Show that $S_n = \frac{n}{2}(a + l)$ where $l = a + (n - 1)d$

[2] A sequence in geometric progression is given by $a, ar, ar^2, \dots, ar^{n-1}$.
Show that $S_n = \frac{a(1-r^n)}{1-r}$

Differentiation from first principles

[1] $\frac{dy}{dx} = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$, find $f'(x)$ if

[a] $f(x) = \sqrt{x}$

[b] $f(x) = \frac{1}{x}$

Quadratic equation

If α and β are the roots of the quadratic equation $ax^2 + bx + c = 0$, show that

[a] $\alpha + \beta = -\frac{b}{a}$ [b] $\alpha\beta = \frac{c}{a}$

3 Unit : Cubic equation

Similarly, if α , β and γ are the roots of the cubic equation $ax^3 + bx^2 + cx + d = 0$
Show that :

[a] $\alpha + \beta + \gamma = -\frac{b}{a}$ [b] $\alpha\beta + \beta\gamma + \gamma\alpha = \frac{c}{a}$ [c] $\alpha\beta\gamma = -\frac{d}{a}$

Finance Maths

Compound interest : P : Principal, $r\%$: rate of interest per period, n : periods.
 A_n : Amount at the end of n periods.

Show that $A_n = PR^n$ where $R = 1 + \frac{r}{100}$



Superannuation :

Show that \$ P invested at the beginning of each period for n periods at $r\%$ per period is

$$A_n = \frac{PR(R^n - 1)}{R - 1}$$



Time payments or annuities :

Show that the amount owing at the end of n periods on a loan of $\$P$ over n periods at $r\%$ per period with a regular repayments (i.e instalments) of $\$M$ is given by :

$$A_n = PR^n - \frac{M(R^n - 1)}{R - 1}$$



Parabola :

Show that the locus of $P(x, y)$ whose distance from a fixed point $S(0, a)$ equal to its distance from a fixed line $y = -a$ is given by $x^2 = 4ay$.



3 Unit : Acceleration as a function of x

Show that $a = \frac{d}{dx} \left(\frac{1}{2} v^2 \right)$



3 Unit : Inverse Trigonometric Ratios

Show that [1] if $y = \sin^{-1}x$ then $\frac{dy}{dx} = \frac{1}{\sqrt{1-x^2}}$

[2] If $y = \tan^{-1}x$, then $\frac{dy}{dx} = \frac{1}{1+x^2}$

3 Unit : Binomial theorem

Show that $\binom{n}{k} = \frac{n(n-1)(n-2)\dots(n-k+1)}{1 \times 2 \times 3 \times \dots \times k}$ for $1 \leq k \leq n$ by mathematical induction.