

# C.E.M. TUITION

**Student Name :** \_\_\_\_\_

**Review Topic : Probability**

**(HSC - PAPER 4)**

**Year 12 - 2 Unit**

---

**20.** It has been estimated that the probability of a dog living beyond the age of 10 is 0.7 while that of a cat is 0.9. Alison owns two cats while Greg has one of each. Calculate the probability (using a tree diagram or otherwise) that:

- (a) both of Alison's cats live past 10;
  - (b) one of Greg's animals lives beyond 10;
  - (c) at least one of Alison's animals lives beyond 10;
  - (d) all four animals survive past 10.
-

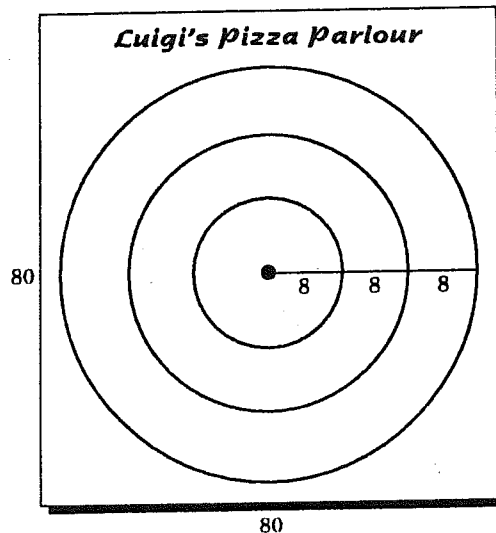
21. In Lower Warkworth the local doctor, based on years of data research, estimated that the probability of an adult catching influenza was 0.1 while the probability of a child catching the dreaded influenza was 0.3. The Blott family consists of Dad, Mum and two young Blotts. Calculate the probability that:
- (a) both adults catch influenza;
  - (b) one child catches influenza;
  - (c) one adult and one child catches influenza;
  - (d) at least one family member catches influenza.
-



**23.** One hundred tickets are sold in a chook raffle. Gregory John purchases two tickets hoping to win both first and second prizes. Find the probability that GJ wins:

- |                        |                         |
|------------------------|-------------------------|
| (a) first prize;       | (b) both prizes;        |
| (c) only second prize; | (d) a prize;            |
| (e) no prize;          | (f) at least one prize. |
-

24. Luigi has a special incentive scheme at his pizza shop. On the side wall is a specially-designed target on an  $80 \times 80$  cm board. The target consists of three concentric circles with radii 8 cm, 16 cm and 24 cm respectively. Each customer is given one dart to throw at the board. They win a free super supreme if they hit the inner circle, a medium pizza if they hit the middle area and a thickshake for the



area in the outer circle. If they miss the circles they pay full price for their order. (Anyone who misses the board is allowed a rethrow.)

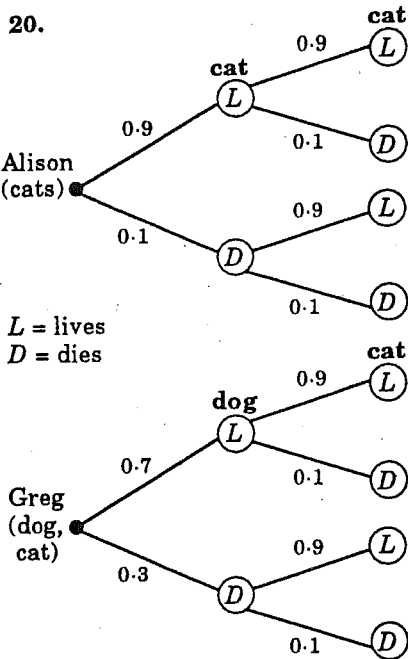
(a) Find the probability that:

- (i) Jill wins a super supreme;
- (ii) Peter wins a thickshake;
- (iii) Guiseppe wins a prize;
- (iv) Gwen pays full price.

(b) If each customer is allowed 2 throws (and possibly can win 2 prizes) find the probability that:

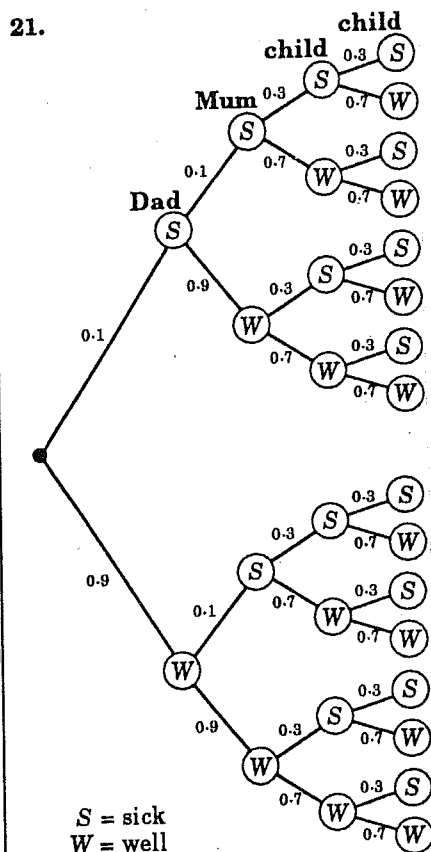
- (i) Pietra wins 2 prizes;
- (ii) Janus wins 1 prize;
- (iii) Leigh fails to win at all;
- (iv) Scotty wins at least one prize.





L = lives  
D = dies

- (a)  $P(\text{both cats live})$  [Alison]  
 $= 0.9 \times 0.9 = 0.81$
- (b)  $P(\text{one animal lives})$  [Greg]  
 $= P(LD) + P(DL)$   
 $= 0.7 \times 0.1 + 0.3 \times 0.9$   
 $= 0.34$
- (c)  $P(\text{at least one of Alison's lives}) = 1 - P(\text{both die})$   
 $= 1 - (0.1 \times 0.1) = 0.99$
- (d) Alison:  $P(\text{both live}) = 0.81$   
 Greg:  $P(\text{both live}) = 0.7 \times 0.9 = 0.63$   
 $P(\text{all 4 live}) = 0.81 \times 0.63$   
 $= 0.5103$  (Product Rule)



S = sick  
W = well

Note Entire tree is not needed for (a), (b) as Product Rule can be used—number of possible situations is small.

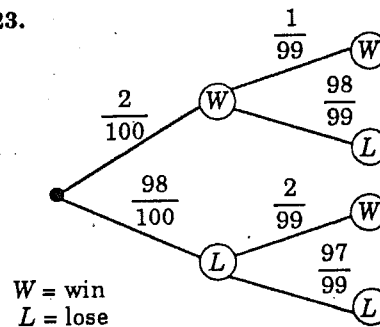
- (a)  $P(\text{both adults sick})$   
 $= 0.1 \times 0.1 = 0.01$
- (b)  $P(\text{one child sick})$   
 $= P(SW) + P(WS)$   
 $= 0.3 \times 0.7 + 0.7 \times 0.3$   
 $= 0.42$
- (c)  $P(\text{one adult, 1 child sick})$   
 $= P(SWSW) + P(SWWS)$   
 $+ P(WSSW) + P(WSWS)$   
 $= 4 \times (0.1 \times 0.9 \times 0.3 \times 0.7)$   
 $= 0.756$
- (d)  $P(\text{at least one sick})$   
 $= 1 - P(\text{all well})$   
 $= 1 - 0.9 \times 0.9 \times 0.7 \times 0.7$   
 $= 0.6031$

22.

+	1	2	3	4	5	6
1	0	0	0	0	0	0
2	0	0	1	0	1	0
3	0	1	0	1	2	0
4	0	0	1	0	1	2
5	0	1	2	1	0	1
6	0	0	0	2	1	0

- (a)  $P(0) = \frac{22}{36} = \frac{11}{18}$
- (b)  $P(3) = 0$  (does not happen)
- (c)  $P(\neq 0) = 1 - P(0) = \frac{7}{18}$
- (d)  $P(\geq 1) = P(\neq 0) = \frac{7}{18}$
- (e)  $P(\text{even}) = P(2) = \frac{4}{36} = \frac{1}{9}$

23.



- (a)  $P(\text{first prize}) = \frac{2}{100} = \frac{1}{50}$
- (b)  $P(WW)$   
 $= \frac{2}{100} \times \frac{1}{99}$   
 $= \frac{2}{9900} = \frac{1}{4950}$
- (c)  $P(LW) = \frac{98}{100} \times \frac{2}{99} = \frac{49}{2475}$   
 (only second implies lose, win)
- (d)  $P(\text{a prize})$   
 $= P(WL) + P(LW) + P(WW)$   
 $= \frac{2}{100} \times \frac{98}{99} + \frac{98}{100} \times \frac{2}{99}$   
 $+ \frac{1}{4950}$  [from (b)]  
 $= \frac{197}{4950}$  [or  $1 - P(LL)$ ]
- (e)  $P(LL) = \frac{98}{100} \times \frac{97}{99} = \frac{4753}{4950}$
- (f)  $P(\text{at least one prize})$   
 $= 1 - P(\text{no prize})$   
 $= 1 - \frac{4753}{4950} = \frac{197}{4950}$



24. We need to know the relative areas of each section.

A of inner circle

$$= \pi r^2 = \pi 8^2 = 64\pi \text{ cm}^2$$

A of middle section

$$= \pi(16)^2 - 64\pi = 192\pi \text{ cm}^2$$

A of outer ring

$$= \pi(24)^2 - 192\pi = 384\pi \text{ cm}^2$$

Also area of board

$$= 80 \times 80 = 6400 \text{ cm}^2$$

The probability of hitting any section will be the ratio of the area of each section relative to the area of the board.

(a) (i)  $P(\text{Super Supreme})$

$$= P(\text{hitting centre})$$

$$= \frac{64\pi}{6400} = 0.0314 \text{ (4 dp)}$$

(ii)  $P(\text{thickshake})$

$$= P(\text{outer ring})$$

$$= \frac{384\pi}{6400} = 0.1885 \text{ (4 dp)}$$

(iii)  $P(\text{prize}) = P(\text{hitting anywhere inside large circle})$

$$= \frac{\pi(24)^2}{6400} = 0.2827$$

(4 dp)

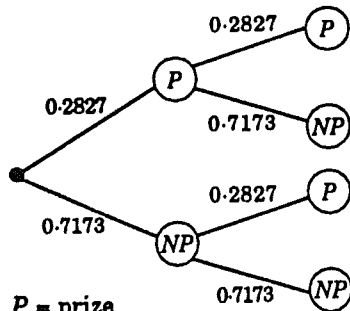
(iv)  $P(\text{no prize})$

$$= 1 - P(\text{prize}) = 0.7173$$

(4 dp)

(b)  $P(\text{prize}) = 0.2827$

$P(\text{no prize}) = 0.7173$



$P = \text{prize}$   
 $NP = \text{no prize}$

(i)  $P(P, P)$

$$= (0.2827)^2$$

$$= 0.0799 \quad (4 dp)$$

(ii)  $P(\text{one prize})$

$$= P(P, NP) + P(NP, P)$$

$$= 0.2827 \times 0.7173$$

$$+ 0.7173 \times 0.2827$$

$$= 0.4056 \quad (4 dp)$$

(iii)  $P(\text{no prizes})$

$$= P(NP, NP)$$

$$= (0.7173)^2$$

$$= 0.5145 \quad (4 dp)$$

(iv)  $P(\text{at least one prize})$

$$= 1 - P(\text{no prizes})$$

$$= 1 - 0.5145$$

$$= 0.4855 \quad (4 dp)$$