SYDNEY GRAMMAR SCHOOL



2013 Annual Examination

# FORM II MATHEMATICS

Tuesday 5th November 2013

### General Instructions

- Writing time 2 hours
- Write using black or blue pen.
- · Calculators are not to be used.

### Total — 130 Marks

- All questions may be attempted.
- All necessary working should be shown.
- Start each question on a new page.

### Collection

- Write your name, class and master on each page of your answers.
- Staple your answers in a single bundle.
- Write your name and master on this question paper and submit it with your answers.

2A: BR 2B: REJ 2C: LYL 2D: SG 2E: GMC 2F: PKH 2G: MLS 2H: SO 2I: LRP 2J: DNW

## Checklist

Writing paper required.Candidature — 190 boys

Examiner

GMC

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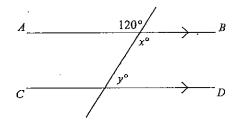
QUESTION ONE (13 marks) Start a new page.

- (a) Calculate:
  - (i)  $3+2\times(-4)$
  - (ii)  $1-\frac{2}{7}$
  - (iii)  $4.2 \div 3$
  - (iv)  $6 \times \frac{2}{3}$
- (b) Calculate:
  - (i) 30% of \$60
  - (ii)  $\frac{1}{3} + \frac{1}{4}$
- (c) Simplify:
  - (i) 5p+1-p
  - (ii)  $x^5 \div x^3$
- (d) Factorise:
  - (i) 8 + 2m
  - (ii)  $15p^2 20p$
- (e) All squares are rectangles. True or False?
- (f) Evaluate 5-3a when a=-4.
- (g) Simplify 14:21.

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QUESTION TWO (13 marks) Start a new page.

- (a) Expand and simplify 3(1-2p)+4.
- (b) Solve 2 + 3x = 14.
- (c) (i) Solve  $2x 1 \le 5$ .
  - (ii) Graph your answer to part (i) on a number line.
- (d) Calculate the area of a circle with radius 10 cm. Use the approximation  $\pi = 3.14$ .
- (e) In the diagram below, AB||CD.



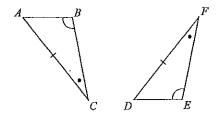
Find the value of x and y, giving reasons.

- (f) Calculate the number of minutes in 2.8 hours.
- (g) Write down the coordinates of the point four units directly above the point (2, -3).
- (h) A square has side length 2x units. Write an expression for:
  - (i) the perimeter of the square.
  - (ii) the area of the square.

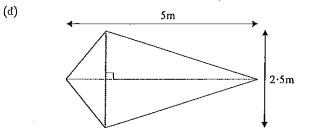
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QUESTION THREE (13 marks) Start a new page.

- (a) Name the three quadrilaterals whose diagonals intersect at right angles.
- (b) Increase \$3 by 70%.
- (c) Consider the two triangles in the diagram below.



Which of the four congruence tests could be used to justify that  $\triangle ABC \equiv \triangle DEF$ ?



Find the area of the kite in the diagram above.

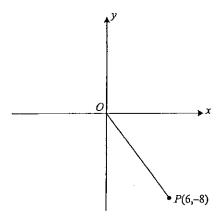
- (e) A bag contains red and blue marbles in the ratio 4:5. If there are 45 blue marbles in the bag, calculate the number of red marbles.
- (f) Divide 2km in the ratio 3:5.
- (g) Determine by substitution whether the point (7,-12) lies on the line y=-2x+5.

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QUESTION FOUR (13 marks) Start a new page.

(a) Write  $\frac{3}{8}$  as a percentage.

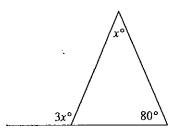
- (b) Simplify  $\frac{2}{3}:\frac{5}{6}$ .
- (c) The base of a triangle is 6 cm and its area is 21 cm<sup>2</sup>. Calculate the perpendicular height of the triangle.
- (d) In the diagram below, the coordinates of point P are (6, -8).



Calculate the distance of P from the origin.

(e) A tap is dripping at a rate of 12L per day. Express this rate in mL per hour.

(f)



In the diagram above, find the value of x, giving reasons.

(g) Solve 4x + 1 = 2x.

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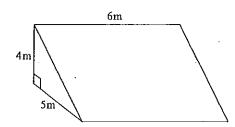
QUESTION FIVE (13 marks) Start a new page.

(a) (i) Copy the table below to your answer sheet and fill it in according to the rule y=3-2x.

x	0	1	2
y			

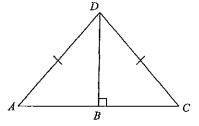
(ii) Hence graph the line y = 3 - 2x on a set of axes.

(b)



Find the volume of the triangular prism in the diagram above.

- (c) Solve 2(x+3)-4(x-1)=5.
- (d) The sum of three consecutive odd numbers is 219. Let the first number be x.
  - (i) Show that 3x + 6 = 219.
  - (ii) Hence find the three numbers.
- (e) In the diagram below, AD=CD and  $\angle CBD=90^{\circ}$ .

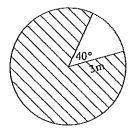


Prove that  $\triangle ABD \equiv \triangle CBD$ .

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QUESTION SIX (13 marks) Start a new page.

(a) Consider the shaded sector in the diagram below.



- (i) Show that the area of this sector is  $\frac{8}{9}$  of the area of the full circle.
- (ii) Hence calculate the area of the shaded sector. Leave your answer in exact form.
- . (b) A computer shop has a 40% off sale. If Bianca paid \$450 after the discount for her computer, calculate the amount of money she saved.
- (c) Solve the following equations:

(i) 
$$4(2-x) = -3(3-2x)$$

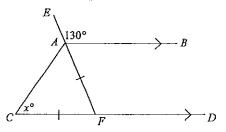
$$(ii)^{\cdot} \frac{5x}{7} = \frac{x}{2} - 1$$

(d) Solve 
$$\frac{5-4x}{2} > x$$
.

(e) Perform the constructions outlined on the tear-off sheet at the end of this examination paper. This sheet should be bundled with the rest of your answers to Question Six. SGS Annual 2013 ...... Form II Mathematics ...... Page 8

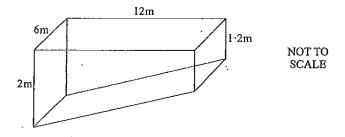
QUESTION SEVEN (13 marks) Start a new page.

- (a) Two cars are 10 km apart on a straight road and moving in the same direction. The car in front is travelling at 60 km/h and the car behind is travelling at 90 km/h.
  - (i) Calculate how long it takes for the two cars to meet.
  - (ii) Hence calculate the distance the slower car travels before the two cars meet.
- (b) Expand and simplify  $(a+b)^2 (a-b)^2$ .
- (c) Express  $\frac{ab^2}{2c} 2c$  as a single fraction.
- (d) In the diagram below, AB||CD, AF = CF and  $\angle EAB = 130^{\circ}$ .



Find the value of x, giving reasons.

(e) A swimming pool is in the shape of a trapezoidal prism, as shown in the diagram below.

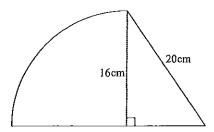


- (i) Show that the area of the cross section of the pool is 19.2 m<sup>2</sup>.
- (ii) Hence calculate the capacity of the pool in litres. Note:  $1 \, \text{m}^3 = 1000 \, \text{L}$ .

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QUESTION EIGHT (13 marks) Start a new page.

- (a) A right-angled triangle has two sides of length 2 cm and 3 cm. Give two possibilities for the length of the third side. Leave your answers in exact form.
- (b) A shape is comprised of a quarter circle and a right-angled triangle, as shown in the diagram below.



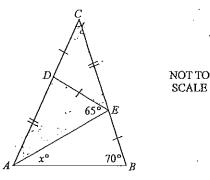
Calculate the exact perimeter of the shape.

- (c) Solve  $\frac{2}{3x} = 1 \frac{5}{2x}$ .
- (d) The length and breadth of a rectangular TV screen are in the ratio 9:4. If the area of the screen is 8100 cm<sup>2</sup>, calculate the perimeter of the screen.
- (e) The ratio of boys to girls enrolled in a university course is 4:7. If there are 24 more girls than boys, calculate the number of students enrolled in the course.

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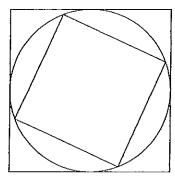
QUESTION NINE (13 marks) Start a new page.

- (a) Simplify  $\frac{p-q}{2q-2p}$ .
- (b) Solve  $\frac{1}{1+\frac{1}{x}} = 2$ .
- (c) In the diagram below AD = CE, CD = DE = EB,  $\angle ABC = 70^{\circ}$  and  $\angle AED = 65^{\circ}$ .



Find the value of x, giving reasons.

(d) A small square is circumscribed by a circle which in turn inscribes a larger square, as shown in the diagram below.



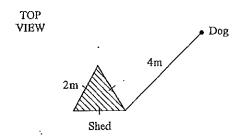
If the area of the smaller square is 4 cm<sup>2</sup>, calculate the area of the larger square.

(e) Calculate  $\frac{(2a^2b)^5}{a^8b^7}$  when  $a=-\frac{3}{4}$  and  $b=1\frac{1}{2}$ .

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QUESTION TEN (13 marks) Start a new page.

- (a) Use the result  $X^2 Y^2 = (X Y)(X + Y)$  to answer parts (i) and (ii) below. You do NOT need to prove this result.
  - (i) Show that  $5423^2 4577^2 = 8460000$ .
  - (ii) Explain why 9919 is not a prime number.
- (b) A metal cube of side length 3 units is melted down and used to make small metal cylinders each of height 1 unit and diameter 1 unit.
  - (i) Calculate the volume of one of the cylinders. Give your answer in exact form.
  - (ii) Hence calculate the maximum number of cylinders that can be made from the metal cube. Give your answer as a whole number.
- (c) Andrew walks an 18 km straight course at a constant speed of 5 km/h. Barry runs the same course at a constant speed of 12 km/h. When Barry reaches the finish, he turns around and runs back to Andrew. Barry then turns around and runs back to the finish. Barry repeats this pattern until Andrew finishes the course. How much further did Barry travel compared with Andrew?
- (d) A triangular garden shed in a large backyard has sides 2m long as shown in the diagram below. A dog is tied with a 4 metre long rope to one of the corners of the shed.



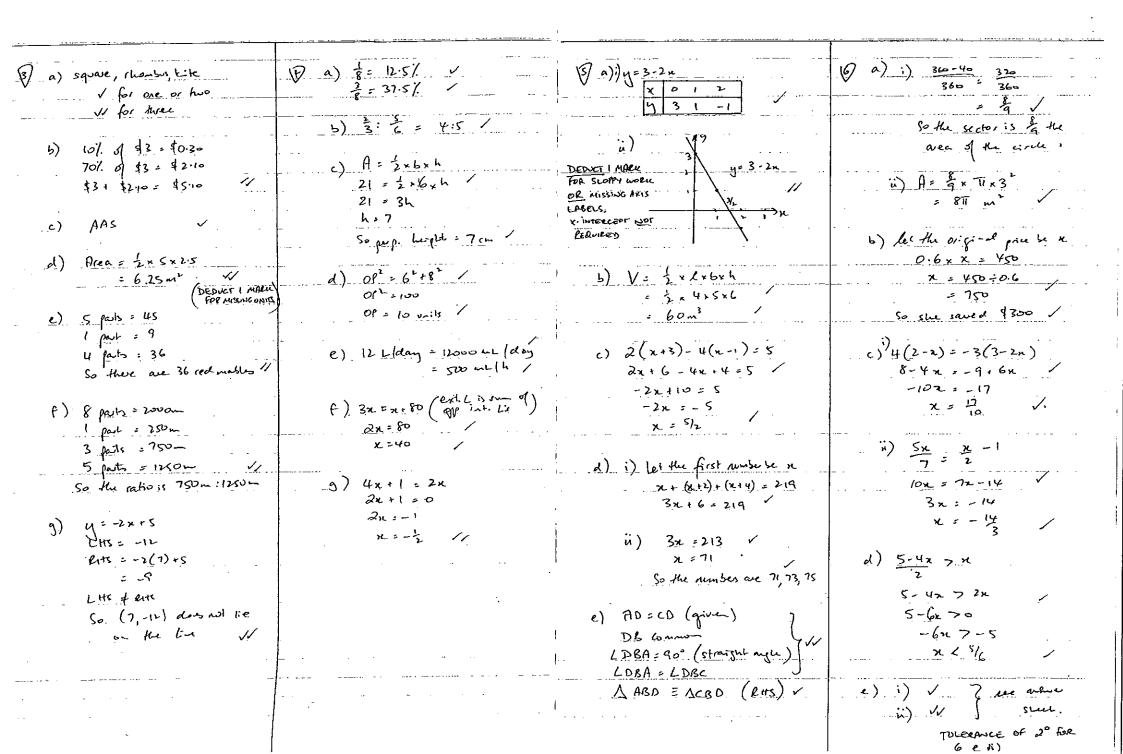
- (i) Copy the diagram above carefully and illustrate the area of the yard in which the dog can play.
- (ii) Calculate the area in which the dog has to play.

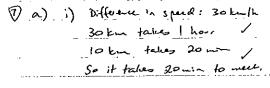
# END OF EXAMINATION

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	>	
4: -	3+2x(-4)=-5	
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DEDUCTIONS	3d) deduct I mark for	Missing or incorrect onits	8 5) deduce 1 mar for	not calabate oractoves	6 e il deduct I moth brayle	outside of 2 tolerance	
		:	_ +		<u>i</u>		١.





- ii) 60 km fales 1 hour

  20km tales 20 min.
  So the slower car travels
  20 km
- 5) (a+6) -(a-6) = a+1 2a5+6-(a2-2a5+6) /= 4a6 /
- (c)  $\frac{ab^2}{2c} \frac{2c}{2c} = \frac{ab^2 4c^2}{2c} / 1$
- d) LEFO = 130° (corresponding Lis, ABIICD)

  LCAF = x° (base Lis isos A) /

  X+X=130 (ext L = su- of 9) /

  interar Lis)

  2.566
- e) i) A= 1.2 r2 x 12 = 19.2 m² /
  - ii) V = (A.2 x L = 115.2 m<sup>3</sup> = 115200 L

x=22.32 y=32-22 x= 113 / y=55 / So the leyth could be issem or Jscm

- b) let base of triagle se x x = 12 f = 12 + 20 + 16 , 4 x 2x TT x 16
  - DEDUCT I MALE FOR APPLOXIMATION
  - $\frac{2}{3x} = \frac{1-5}{2x}$   $\frac{2}{3x} = \frac{5}{2x}$   $\frac{4}{9} = \frac{6}{9} = \frac{6}{9}$   $\frac{1}{9} = \frac{6}{9} = \frac{6}{9}$   $\frac{2}{9} = \frac{1}{9} = \frac{5}{9}$   $\frac{2}{9} = \frac{1}{9} = \frac{5}{9} = \frac{1}{9} = \frac{1}{9}$
- d) let length be 9x, breach be 4x

  9x x 4x = 8100

  36x2=8100

  x2 = 125

  x = 15

  so legth = 135, breach = 60
  - so legh = 135, breach = 60 P= 135x2+60x2 = 390cm
- e) 3 parts = 24 1 part = 8 11 parts = 84 So 88 papils in total. 111

$$\sqrt{q/a}) \frac{\rho - q}{2q - 2\rho} = \frac{\rho - q}{-2(q - \ell)}$$

$$= -\frac{1}{2}$$

- $\frac{1}{1+\frac{1}{x}} = \frac{1}{1+\frac{1}{x}}$   $\frac{1+\frac{1}{x}}{1+\frac{1}{x}} = \frac{1}{1+\frac{1}{x}}$
- c) (LCAB = 70° (base Lis of isos A)

  (ACB = 40° (angle or of A)

  (CEO = 40° (base Lis of isos A)

  x+70°:105° (external L = su

  of oppinhusor Lis)

  x=35 /
- d) Side leyth of small squae = 2

  Let d be diagonal of small squae

  d'= 2'+2'

  d = 88

  So side leyth of laye squae = 58/

  So area laye squae = ((4)'

  = 8cm. V
- e)  $(2a^{3}b)^{5}$   $32a^{10}b^{5}$   $= 32a^{2}$   $= 32(-\frac{3}{4})^{2}$   $= 32 \times (-\frac{3}{4} \frac{3}{2})^{2}$   $= 32 \times (-\frac{3}{4} \frac{3}{2})^{2}$

= 32× (-1)

- (10) a) x y = (x-y)(x+y) 1) 5423 - 4577 = (5423 + 4577) = 846 × 10000 = 846 × 0000
  - ii) 9919 = 10000 81 = 100 - 92 = 91×109
  - So 9919 is not prime.

    (b) i)  $r = \frac{1}{2}$   $V = II \times (\frac{1}{2}) \times 1$   $V = II \times (\frac{1}{2}) \times 1$ 
    - ii) vol of use = 3 = 27 ~
      - $27 \div \frac{\pi}{4} = \frac{27 \times 4}{\pi}$   $= \frac{108}{3 \cdot 1}$
      - Long Division:
        - 34 31)1080 <del>43</del> 150 124 26
      - so 34 cylinders can be made.
        - NUMBER BY MARY

c) 1875 = 33/s.

So Andrew takes 3.6 hours to

walle the corre V

3.6 x 12 = 43.2

So Borry runs 43.2 km h عيدهيد ط.3

43.2 -18 = 25.2

So Barry travels 25.2 km , further than Andrew ...

Area of play area = \$ x 11 x 42 + \frac{7}{6} x 11 x \frac{1}{2} + \frac{7}{6} x 11 x \frac{1}{2} + \frac{7}{6} = 4011 + 311 + 53 = 44TT + 53 m

ii) Area = Ex circle radius 4 + 2 x = x circle radius 2 + 1 x equilatual 1 with side length 2

Consider the equilateral triangle. Let populierla height be h

So Area of trank = 5x2x B

(ii) Copy the angle  $\angle COD$  at one end of interval EF.

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DETACH THIS SHEET AND BUNDLE IT WITH THE REST OF QUESTION SIX.

(i) Construct a perpendicular bisector of interval AB.

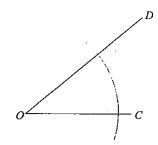
(e) In the following questions leave all construction arcs and use only a ruler and

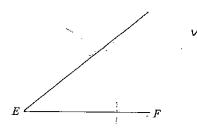
QUESTION SIX

compass.

CLASS: .....

MASTER: .....





Must show construction marks.