

## START A NEW PAGE

1. Sketch the following regions

(a)  $xy \leq 1$

(b)  $4 \leq x^2 + y^2 < 16$

4marks

2. Describe the roots of the following equations as unreal, real, distinct, equal, or rational:

(a)  $5x^2 - 4x - 7 = 0$

(b)  $4x^2 + 7x + 3 = 0$ .

3. Solve the equation for x:  $4^{2x} - 5 \cdot 4^x + 4 = 0$ .

4m

4m

4. Given the equation  $x^2 - 3x + 5 = 0$ , with roots  $\alpha$  and  $\beta$   
Evaluate the following:

(a)  $\alpha + \beta$

(b)  $\alpha\beta$

(c)  $\alpha^2 + \beta^2$

(d)  $\frac{\alpha}{\beta} + \frac{\beta}{\alpha}$

(e)  $(\alpha - \beta)^2$ , where  $\alpha > \beta$ .

8m

4. Consider the equation  $x^2 + mx + 3m = 0$ .

Find the value of m such that the equation

(a) is positive definite

(b) has roots which are reciprocals of each other

(c) has one root equal to 2.

6 marks

5. Show that the expression  $x^2 - px - 7 = 0$

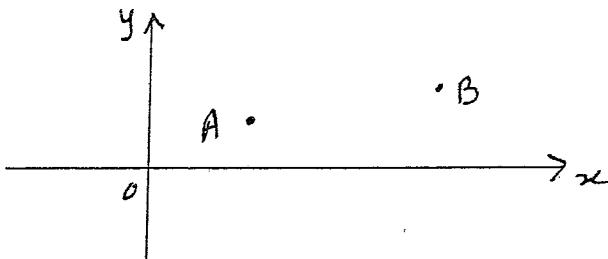
has real and different roots for all real p.

3 marks

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6. If  $2x^2 - 7x - 4 = a(x - b)(x - c)$  for all values of x, find a, b and c. 4m

7. Copy the diagram above and Sketch roughly the locus of points P(x,y) such that P is equidistant from the points A and B shown.



1m

8. State the equation of the locus of points P(x,y) which moves such that it is equidistant 6 units from the fixed point A(2,3). 2m

9. State the equation of the parabola with

- (a) Vertex (0,0) and directrix  $y=-2$
- (b) Focus (-2,0) and directrix  $x=2$

(Hint draw a sketch.) 4m

10. Given the parabola  $(x - 3)^2 = 8(y + 1)$

State the

- (a) Focal length
- (b) Coordinates of the vertex
- (c) Coordinates of the focus
- (d) Equation of the directrix
- (e) Length of the latus rectum
- (f) sketch the parabola, showing above features. 6m

11. Derive the equation of the locus of points P(x,y) which moves such that the distance from P to A(2,3) is always twice the distance from P to B(-4, 7).

Show that the equation can be simplified to

$$3x^2 + 36x + 3y^2 - 50y + 247 = 0$$

Hence show that this locus is a circle and state the centre and radius. 6m

**END**

