

St Catherine's School

Year: 11
Subject: Extension 1 Mathematics
Time allowed: 55 minutes

Assessment Task No: 1
Date: March 2005

Student Name: _____
Teacher's Name: _____

Directions to candidates:

- All questions are to be attempted.
- Marks may be deducted for careless or badly arranged work
- All necessary **working** must be shown in every question.
- Approved calculators and rulers are required.

TEACHERS' USE ONLY

Q 1 - 4	Total	12½	/22
Q 5 - 8	Total	11	/15
	TOTAL	23½	/37

START A NEW PAGE

1. Express as a fraction in simplest form: $0.4\dot{5}\dot{3}$

2marks

2. Factorise

$$(x+y)^2 - (w-p)^2$$

2marks

3. Solve for x :

(a) $(x-2)(x+3) > 0$

(b) $\frac{1}{x-4} \leq 2$

(c) $|x-2| = 3$

(d) $|x-1| = 2x+3$

10m

4. Sketch the following functions showing distinguishing features, and state the domain and range for each:

(a) $y = |x| - 1$

(b) $y = 9 - x^2$

(c) $y = \sqrt{9 - x^2}$

(d) $y = -\frac{3}{x}$

8 marks

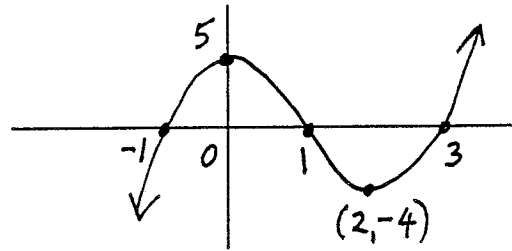
5. State the domain of the following functions:

(a) $y = \frac{1}{x^2 - 9}$

(b) $y = |x+5| + \frac{1}{\sqrt{x^2 - 9}}$

3 marks

6. Consider the graph of $y = f(x)$ as shown in the diagram.



Use your knowledge of graph effects to sketch the following on the axes provided over page:

- (a) $y = f(x) + 2$
- (b) $y = |f(x)|$
- (c) $y = f(x+1)$

5 marks

- 7. (a) Factorise $a^6 - b^6$ by first using a difference of two squares.
- (b) Factorise $a^6 - b^6$ by first using a difference of two cubes.
- (c) Hence show that

$$a^4 + a^2b^2 + 1 = (a^2 + ab + 1)(a^2 - ab + 1)$$

3 marks

- 8. (a) Expand $\left(x + \frac{1}{x}\right)^2$.

(b) If $x = \sqrt{3} - \sqrt{2}$,

(i) evaluate $x + \frac{1}{x}$

(ii) hence evaluate $x^2 + \frac{1}{x^2}$.

4 marks

END

Let $x = 0.4535353\dots$
 $100x = 45.3535\dots$
 $-x = 0.4535\dots$

 $99x = 44.900$
 $x = \frac{44.9}{99}$ (2)
 $= \frac{449}{990}$

$(x+y)^2 - (w-p)^2$ (2)
 $= (x+y-w+p)(x+y+w-p)$
 $= (x+y-w+p)(x+y+w-p)$
 a) $(x-2)(x+3) > 0$

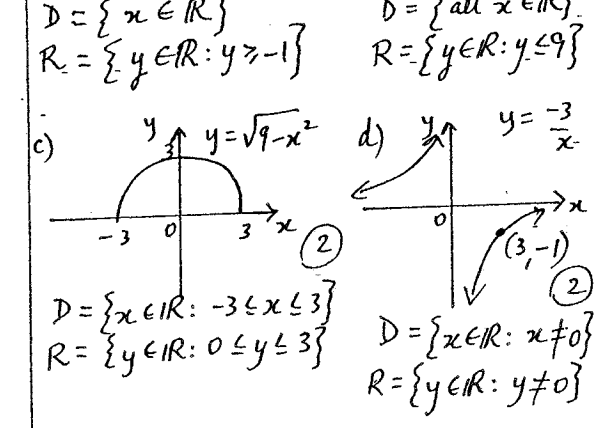
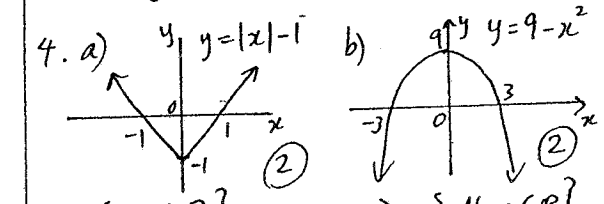
Test around critical values:
 $\leftarrow + \quad - \quad + \rightarrow$ (2)
 $\quad -3 \quad 2$
 $\therefore x < -3$ or $x > 2$

b) $\frac{1}{x-4} \leq 2, x \neq 4$
 $\frac{1}{x-4} - 2 \leq 0$ (3)
 $\frac{1-2(x-4)}{x-4} \leq 0$
 $\frac{x-4}{x-4} \leq 0$
 $\frac{9-2x}{x-4} \leq 0, x \neq 4$

Test around critical values:
 $\leftarrow - \quad + \quad - \rightarrow$
 $\quad 4 \quad 4\frac{1}{2}$
 $\therefore x < 4$ or $x > 4\frac{1}{2}$

3 c) $|x-2|=3$ (2)
 $\therefore x-2=3$ or $x-2=-3$
 $x=5$ or $x=-1$
 d) $|x-1|=2x+3$
 $2x+3 \geq 0$
 $\therefore x \geq -\frac{3}{2}$ and $x-1=2x+3$
 $-4=x$ ✗
 \therefore No sol'n

OR $x \geq -\frac{3}{2}$ and $-(x-1)=2x+3$
 $-x+1=2x+3$
 $-2=3x$
 $x=-\frac{2}{3}$ ✓
 \therefore only solution $x=-\frac{2}{3}$ (3)

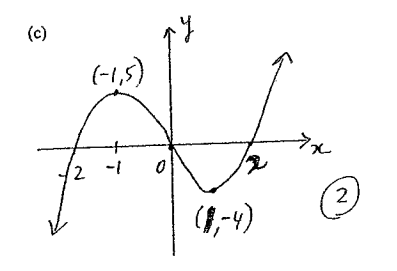
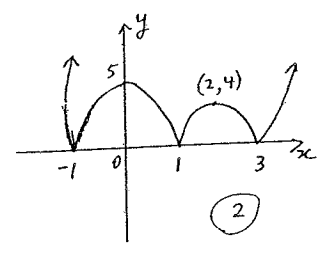
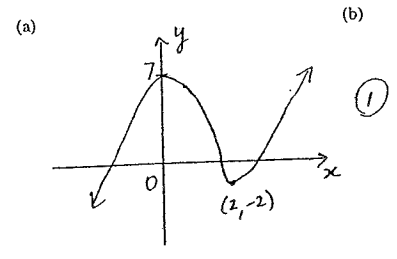


5. a) $y = \frac{1}{x^2-9}$ $D = \{x \in \mathbb{R} : x \neq 3, -3\}$
 $= \frac{1}{(x+3)(x-3)}$ (1)

b) $y = |x+5| + \frac{1}{\sqrt{x^2-9}}$
 $= |x+5| + \frac{1}{\sqrt{(x-3)(x+3)}}$ (2)

Restriction: $(x-3)(x+3) > 0$
 Test around critical values:
 $\leftarrow + \quad - \quad + \rightarrow$
 $\quad -3 \quad 3$
 $\therefore D = \{x \in \mathbb{R} : x < -3$ or $x > 3\}$

6. ANSWERS TO QUESTION 6 NAME: SOLUTIONS



7 a) $a^6 - b^6 = (a^3 - b^3)(a^3 + b^3)$ (1)
 $= (a-b)(a^2+ab+b^2)(a+b)(a^2-ab+b^2)$

b) $a^3 - b^3 = (a^2 - b^2)(a^4 + a^2b^2 + b^4)$ (1)
 $= (a-b)(a+b)(a^4 + a^2b^2 + b^4)$

c) $a^4 + a^2b^2 + b^4 = (a^2+ab+b^2)(a^2-ab+b^2)$
 (1) (since eqns of equals are equal)

8. a) $(x + \frac{1}{x})^2 = x^2 + 2 + \frac{1}{x^2}$ (1)

b) i) $x + \frac{1}{x} = \sqrt{3} - \sqrt{2} + \frac{1}{\sqrt{3}-\sqrt{2}} \cdot \frac{\sqrt{3}+\sqrt{2}}{\sqrt{3}+\sqrt{2}}$
 $= \sqrt{3} - \sqrt{2} + \frac{\sqrt{3}+\sqrt{2}}{3-2}$ (2)
 $= 2\sqrt{3}$

ii) $\therefore x^2 + \frac{1}{x^2} = (x + \frac{1}{x})^2 - 2$
 $\therefore = (2\sqrt{3})^2 - 2$ (1)
 $= 10$