

Student Number: \_\_\_\_\_

STUDENT NAME/NUMBER \_\_\_\_\_

St. Catherine's School  
Waverley

2010  
Yearly Examination  
ASSESSMENT TASK 4  
(Weighting 45%)

Mathematics Preliminary  
Year 11

**General Instructions**

- Reading time – 5 minutes
- Working time – 2 hours
- There are 7 questions of equal value.
- Each question is to be answered in a new booklet.
- If any additional booklet is used, please label it clearly and attach it to the appropriate booklet.
- Write using black or blue pen only.
- Board-approved calculators may be used.
- All necessary working must be shown.
- Marks may be deducted for careless or badly arranged work.

**Total marks – 84**

- Attempt all questions.

**Total marks – 84**  
**Attempt Questions 1 - 7**  
**All questions are of equal value.**

Start each question in a SEPARATE writing booklet. Extra writing booklets are available.

**Question 1. (12 marks)** Marks

(a) Evaluate  $\sqrt[3]{6.91 \times 10^{-5}}$  correct to three significant figures. 2

(b) Factorize  $2x^2 + x - 28$ . 2

(c) Simplify  $\frac{2x+3}{3} - \frac{x+2}{4}$ . 2

(d) Express  $(2\sqrt{3} + 1)(2 - \sqrt{3})$  in the form  $a\sqrt{3} + b$ . 2

(e) A pair of jeans were discounted by 15% to a selling price of \$63.75. Find the original marked price of the jeans before the discount was applied. 2

(f) Solve the following inequality.  $|3x - 5| \geq 2$ . 2

**Question 2.** (12 marks) Start a new writing booklet.

(a) Solve the equation  $\frac{2x-1}{5} = \frac{3x+2}{4}$ .

Marks

2

(b) Simplify  $\frac{x^2-9}{x^2+x-12}$ .

2

(c) Consider  $f(x) = \begin{cases} -3 & \text{if } x \leq -1 \\ 2x-3 & \text{if } x > -1 \end{cases}$ . Evaluate  $f(-1) + f(1)$ .

1

(d) Determine whether the function  $f(x) = \frac{1}{x^2-4}$  is odd, even or neither odd nor even. WORKING MUST BE SHOWN.

1

(e) Sketch graphs of the following functions and state the domain of each.

(i)  $y = \frac{3}{2x-1}$ .

2

(ii)  $y = |2-3x|$ .

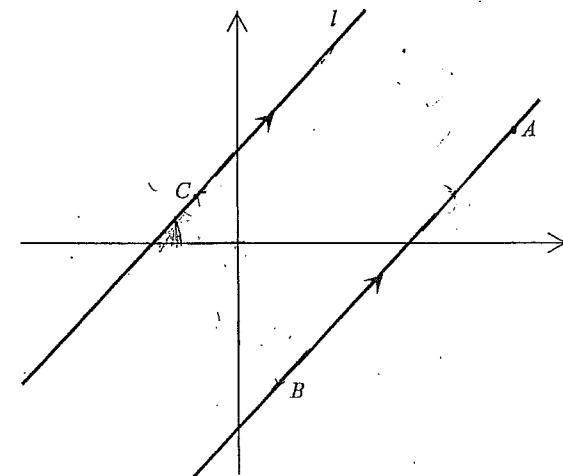
2

(f) Solve  $2\sin^2 x = 1$  where  $-180^\circ \leq x \leq 180^\circ$ .

2

**Question 3.** (12 marks) Start a new writing booklet.

(a)



NOT TO SCALE

The line  $l$  passes through  $C(-1, 2)$  and has equation  $y = 2x + 4$ .

The point  $B$  has coordinates  $(1, -6)$  and the line  $AB$  is parallel to line  $l$ .

Copy the diagram into your examination booklet writing the coordinates of  $B$  and  $C$  onto this diagram.

(i) Find the length of the interval  $BC$ .

1

(ii) Find the midpoint of  $BC$ .

1

(iii) Write down the slope of the line  $l$  and find the angle  $l$  makes with the positive  $x$ -axis.

2

(iv) Show that  $AB$  has equation  $y = 2x - 8$ .

1

(v) If  $P$  is a point which lies on  $AB$  and on the line  $y = 2$ , find the coordinates of  $P$ .

1

(vi) Find the perpendicular distance of  $P$  from the line  $l$ .

2

(vii) Find the size of  $\angle ABC$  to the nearest minute.

1

Question 3 continued on next page.

Marks

Question 3. continued.

- (b) A regular polygon has interior angles measuring  $156^\circ$ .  
How many sides does the polygon have?

1

- (c) The gradient of the tangent to the curve  $y = ax^2 - 2x - 14$  is 10 when  $x = 2$ .  
Find the value of  $a$ .

2

Marks

Question 4. (12 marks) Start a new writing booklet.

- (a) Consider  $f(x) = x^2 - 5x$

- (i) Using  $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ , differentiate  $f(x)$  from first principles. 2

- (ii) Find the gradient of the tangent when  $x = 1$ . 1

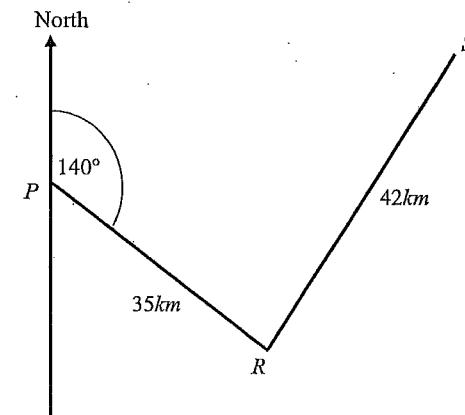
- (iii) Find the equation of the normal through the point  $(1, -4)$ . 2

- (b) Find the exact value of  $\cot 330^\circ$ . 2

Question 4. continued.

Marks

(c)



NOT TO SCALE

A tourist drives 35km from the town of Pine Vale (P) on a bearing of  $140^\circ$  T to the town of Radiatagrove (R). He then drives 42km on a bearing of  $38^\circ$  T to the town of Spruceville (S).

Copy this diagram into your writing booklet.

- (i) Show that  $\angle PRS = 78^\circ$ . 1

- (ii) Show that the distance from Spruceville to Pine Vale (SP) is 49km, correct to the nearest kilometre. 1

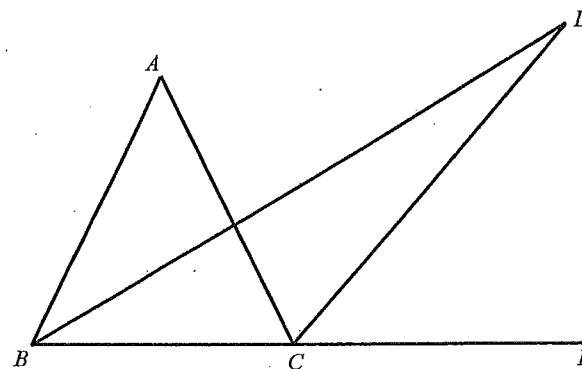
- (iii) Show the size of  $\angle SPR = 57^\circ$  to the nearest degree. 1

- (iv) Hence, or otherwise, find the bearing of Pine Vale from Spruceville. Show all necessary working.. 2

Marks

**Question 5.** (12 marks) Start a new writing booklet.

(a)



NOT TO SCALE

*ABC* is an isosceles triangle in which  $AB = AC$  and  $\angle BAC = 64^\circ$ .  
*BC* is produced to *E*. *BD* bisects  $\angle ABC$  and *CD* bisects  $\angle ACE$ .

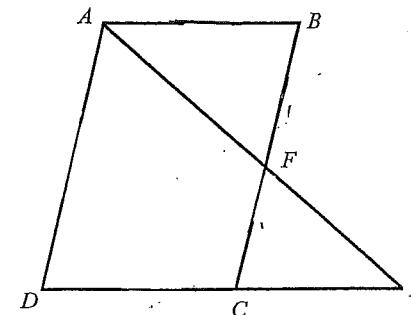
Copy or trace the diagram into your writing booklet and mark on it all the given information.

- (i) Find the size of  $\angle ABC$  giving reasons. 1
- (ii) Find the size of  $\angle BDC$  giving reasons. 2
- (b) By expressing  $\sec \theta$  and  $\tan \theta$  in terms of  $\sin \theta$  and  $\cos \theta$ , show that  $\sec^2 \theta - \tan^2 \theta = 1$ . 1
- (c) If  $\sin \theta = -\frac{4}{11}$  and  $\tan \theta > 0$  find the exact value of  $\cos \theta$ . 2
- (d) Given the equation  $3x^2 + 7x - 4 = 0$  has roots  $\alpha$  and  $\beta$ , without finding  $\alpha$  or  $\beta$  evaluate  $\alpha^2 + \beta^2$ . 3

Marks

**Question 5.** continued.

(e)



*ABCD* is a parallelogram. *DC* is produced to *E*. *AE* cuts *BC* at *F*.  
 $AD = 16\text{cm}$ ,  $CE = 9\text{cm}$  and  $BF = 10\text{cm}$ .

- (i) Prove that  $\triangle ABF$  is similar to  $\triangle ECF$ . 2
- (ii) Find  $AB$ . 1

Marks

Question 7. (12 marks) Start a new writing booklet.

Marks

Question 6. (12 marks) Start a new writing booklet.

(a) For the parabola  $(x-2)^2 = 8(y+3)$ 

(i) Find the coordinates of the vertex.

1

(ii) Find the value of the focal length.

1

(iii) Find the coordinates of the focus.

1

(iv) Find the equation of the directrix.

1

(v) Sketch the parabola labelling the vertex, focus and directrix.

1

(a) Evaluate  $\lim_{x \rightarrow \infty} \frac{3x^2 - 2x - 6}{4 - 2x^2}$ .

1

(b) Find the value of  $k$  for which the equation  $x^2 - (k+4)x + (k-3) = 0$  has(i) one root equal to  $-2$ .

1

(ii) roots which are reciprocals of each other.

1

(iii) roots which are equal in absolute value but opposite in sign.

1

(c) Find all real numbers  $x$  which satisfy the equation  $x^4 = 8(x^2 + 6)$ .

2

(d) Differentiate

(i)  $\frac{3x^2 - 5}{2x + 1}$

2

(ii)  $\sqrt[5]{(2x+7)^2}$

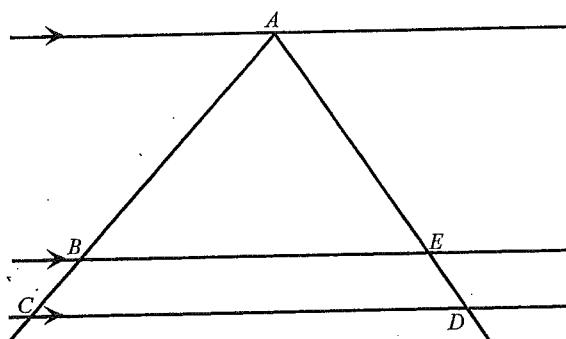
2

(e) Find, as a relationship between  $a$ ,  $b$  and  $c$ , the condition for the quadratic equation in  $x$ 

$$(a^2 - b^2)x^2 + 2b(a - c)x + (b^2 - c^2) = 0$$

2

to have equal roots. Simplify your answer as far as possible.



NOT TO SCALE

AB = 7cm, BC = 4cm, ED = 6cm. Find AD giving reasons.

2

(c) Express  $9x^2 + 2x - 5$  in the form  $ax(x+1) + b(x+1) + c$ .

3

(d) For what values of  $k$  will the expression  $kx^2 - 4x + k$  always be positive?

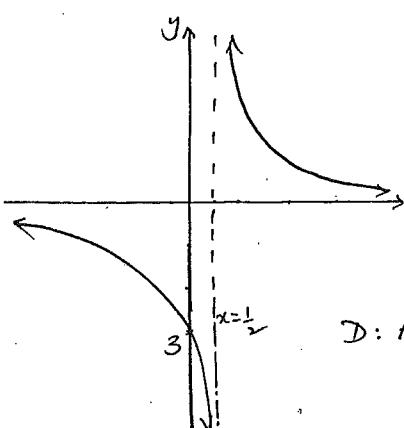
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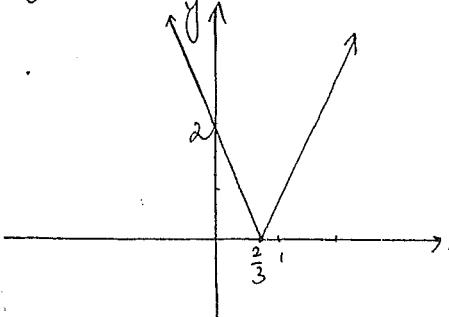
End of paper

YR11 - END OF PRELIMINARY EXAMINATION - 2-unit

Qn	Solutions	Marks	Comments: Criteria
Q1	(a) $\sqrt[3]{6.91 \times 10^{-5}}$ $= 0.0410356 \dots$ $= 0.041$ (to 3 sig. fig.)	1 1	
	(b) $2x^2 + x - 28$ $= (2x - 7)(x + 4)$	2	-1/2 sign incorrect.
	(c) $\frac{2x+3}{3} - \frac{x+2}{4}$ $= \frac{4(2x+3) - 3(x+2)}{12}$ $= \frac{8x+12 - 3x-6}{12}$ $= \frac{5x+6}{12}$	1	
	(d) $(2\sqrt{3} + 1)(2 - \sqrt{3})$ $= 4\sqrt{3} - 6 + 2 - \sqrt{3}$ $= 3\sqrt{3} - 4$	1	-1/2 sign incorrect.
	(e) $85\% \times \text{cost} = \$63.75$ $\text{Cost} = 63.75 \div 0.85$ $\text{Cost} = \$75.00$	1	
f	$ 3x - 5  \geq 2$ <u>Case 1:</u> $3x - 5 \geq 0$ $3x - 5 \geq 2$ $3x \geq 7$ $x \geq \frac{7}{3}$	2	Case 2: $3x - 5 < 0$ $-(3x - 5) \geq 2$ $3x - 5 \leq -2$ $3x \leq 3$ $x \leq 1$

Qn	Solutions	Marks	Comments: Criteria
Q2	(a) $\frac{2x-1}{5} = \frac{3x+2}{4}$ $4(2x-1) = 5(3x+2)$ $8x - 4 = 15x + 10$ $8x - 15x = 10 + 4$ $-7x = 14$ $x = -2$	1	
	(b) $\frac{x^2 - 9}{x^2 + x - 12}$ $= \frac{(x-3)(x+3)}{(x-3)(x+4)}$ $= \frac{x+3}{x+4}$	1	1/2 incorrect signs.
	(c) $f(-1) = -3$ $f(1) = 2(1) - 3$ $= -1$ $\therefore f(-1) + f(1)$ $= -3 + -1$ $= -4$	1	$f(-1) \frac{1}{2}$ $f(1) \frac{1}{2}$ each.

Qn	Solutions	Marks	Comments: Criteria
Q2(d)	$f(x) = \frac{1}{x^2 - 4}$		
	$f(a) = \frac{1}{a^2 - 4}$		
	$f(-a) = \frac{1}{(-a)^2 - 4}$	1	
	$= \frac{1}{a^2 - 4} = f(a)$		
	$\therefore f(x) = \frac{1}{x^2 - 4}$ is an even function		
Q2(e)(i)	$y = \frac{3}{2x-1}$		
			
		2	1 sketch 1 domain

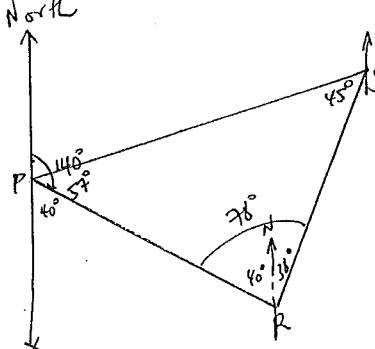
Qn	Solutions	Marks	Comments: Criteria
Q2(e)(ii)	$y =  2 - 3x $		
			1 sketch 1 domain
	D: For all real x.	2.	
	$2\sin^2 x = 1$		
	$\sin^2 x = \frac{1}{2}$		
	$\sqrt{\sin^2 x} = \pm \sqrt{\frac{1}{2}}$		
	$\sin x = \pm \frac{1}{\sqrt{2}}$		
	$\sin x = \frac{1}{\sqrt{2}} \quad \cancel{x} \quad \cancel{x}$		
	$x = 45^\circ, 135^\circ$		
	$\sin x = -\frac{1}{\sqrt{2}} \quad \cancel{x} \quad \cancel{x}$		
	$x = -45^\circ, -135^\circ$		
	1/2.	1/2.	1

Qn	Solutions	Marks	Comments: Criteria
Q3(a)			
(i)	$BC = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ $= \sqrt{(-1 - 1)^2 + (-6 - 2)^2}$ $= \sqrt{2^2 + (-8)^2}$ $= \sqrt{68}$ $= 2\sqrt{17}$	1	
(ii)	$\text{Midpoint of } BC = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$ $= \left( \frac{-1 + 1}{2}, \frac{-6 + 2}{2} \right)$ $= (0, -2)$	1	
(iii)	$m = 2$ $\tan \theta = 2$ $\therefore \theta = 63^\circ 26'$	1	
(iv)	$y - y_1 = m(x - x_1)$ $y + 6 = 2(x - 1)$ $y + 6 = 2x - 2$ $y = 2x - 8$	1	

Qn	Solutions	Marks	Comments: Criteria
Q3(v)	<p>Solve <math>y = 2</math> and <math>y = 2x - 8</math></p> $2x - 8 = 2$ $2x = 10$ $x = 5$ $\therefore P(5, 2)$	1	
(vi)	$d = \frac{ Ax + By + C }{\sqrt{A^2 + B^2}}$ line $l \Rightarrow 2x - y + 4 = 0$ $P(5, 2)$ $d = \frac{ 2(5) - 1(2) + 4 }{\sqrt{2^2 + (-1)^2}}$ $= \frac{ 10 - 2 + 4 }{\sqrt{4+1}}$ $= \frac{12}{\sqrt{5}}$ $= \frac{12}{\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}}$ $= \frac{12\sqrt{5}}{5} \text{ units}$	1	
(vii)	$\sin \theta = \frac{12}{\sqrt{5}} \div 2\sqrt{17}$ $\therefore \theta = 40^\circ 36'$	1	-1/2 incorrect signs.

Qn	Solutions	Marks	Comments: Criteria
Q3(b)	<p>each interior angle = <math>156^\circ</math></p> $\frac{(n-2)180^\circ}{n} = 156^\circ$ $(n-2)180 = 156n$ $180n - 360 = 156n$ $180n - 156n = 360$ $24n = 360$ $n = 15$	1	
Q4(c)	<p><math>y = ax^2 - 2x - 14</math></p> $\frac{dy}{dx} = 2ax - 2 \quad (\text{gradient function})$ <p>at <math>x=2</math>, <math>\frac{dy}{dx} = 10</math></p> <p>i.e. <math>2ax - 2 = 10</math></p> $2a(2) - 2 = 10$ $4a - 2 = 10$ $4a = 12$ $a = 3$	1	

Qn	Solutions	Marks	Comments: Criteria
Q4(a)	$f(x) = x^2 - 5x$ $f(x+h) = (x+h)^2 - 5(x+h)$ $= x^2 + 2xh + h^2 - 5x - 5h$ $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ $= \lim_{h \rightarrow 0} \frac{x^2 + 2xh + h^2 - 5x - 5h - (x^2 - 5x)}{h}$ $= \lim_{h \rightarrow 0} \frac{x^2 + 2xh + h^2 - 5x - 5h - x^2 + 5x}{h}$ $= \lim_{h \rightarrow 0} \frac{2xh + h^2 - 5h}{h}$ $= \lim_{h \rightarrow 0} \frac{h(2x + h - 5)}{h}$ $= 2x - 5$	1	
Q4(ii)	<p>when <math>x=1</math>, <math>f'(1) = 2(1) - 5</math></p> $= -3$	1	
Q4(iii)	<p>gradient of normal is <math>\frac{1}{3}</math></p> $y - y_1 = m(x - x_1)$ $y - 4 = \frac{1}{3}(x - 1)$ $y + 4 = \frac{1}{3}(x - 1)$ $3y + 12 = x - 1$ $x - 3y - 13 = 0$	1	<p>if found the equation of tangent.</p> <p>0.5%</p>

Qn	Solutions	Marks	Comments: Criteria
Q4(b)	$\cot 330^\circ$ $= \frac{1}{\tan 330^\circ} \times$ $= \frac{1}{-\tan 30^\circ} \times$ $= \frac{1}{-\frac{1}{\sqrt{3}}} \times$ $= -\sqrt{3} \times$	1	
(c)		1	-0.5 mark if negative is not shown
(i)	$\angle XPR = 180^\circ - 140^\circ$ $= 40^\circ$ (adj. supp. $\angle$ s). $\angle PRN = 40^\circ$ (alt. $\angle$ s, $PX \parallel NR$ ) $\therefore \angle PRS = 40^\circ + 38^\circ$ $= 78^\circ$	1	
(ii)	$SP^2 = 35^2 + 42^2 - 2 \times 35 \times 42 \cos 78^\circ$ $SP = \sqrt{35^2 + 42^2 - 2 \times 35 \times 42 \cos 78^\circ}$ $= 49 \text{ km}$	1	
(iii)	$\frac{\sin \theta}{42} = \frac{\sin 78^\circ}{49}$ $\sin \theta = \frac{\sin 78^\circ}{49} \times 42$ OR $(\text{use of the cosine rule is acceptable.})$ $\therefore \theta = 57^\circ$	1	

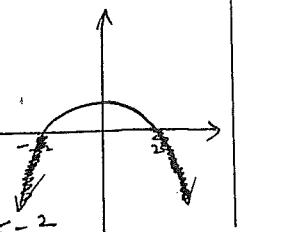
Qn	Solutions	Marks	Comments: Criteria
Q4(iii)	$\angle PSR = 180^\circ - (57^\circ + 78^\circ)$ ( $\angle$ sum of $\triangle$ ) $= 45^\circ$  $\text{Bearing} = 180^\circ + 38^\circ + 45^\circ$ $= 263^\circ$	1	

Qn	Solutions	Marks	Comments: Criteria
Q5	<p>(a)</p> <p>i) <math>\angle ABC = \frac{180^\circ - 64^\circ}{2} = 58^\circ</math> (base angles of isosc. <math>\triangle</math>)</p> <p>ii) Since <math>BD</math> bisects <math>\angle ABC</math>  <math>\therefore \angle DBC = \frac{58^\circ}{2} = 29^\circ</math>  and <math>\angle ACB = 58^\circ</math> (base angles of isosc. <math>\triangle</math>)  <math>\therefore \angle ACE = 180^\circ - 58^\circ = 122^\circ</math> (adj. supp. <math>\angle</math>)  and since <math>CD</math> bisects <math>\angle ACE</math>  <math>\therefore \angle ACD = 61^\circ</math>  <math>\therefore \angle BDC = 180^\circ - (29^\circ + (61^\circ + 58^\circ)) = 32^\circ</math> (<math>\angle</math> sum of <math>\triangle</math>)</p>	1	
Q48	$\begin{aligned} b) &= \sec^2 \theta - \tan^2 \theta \\ &= \frac{1}{\cos^2 \theta} - \frac{\sin^2 \theta}{\cos^2 \theta} \\ &= \frac{1 - \sin^2 \theta}{\cos^2 \theta} \\ &= \frac{\cos^2 \theta}{\cos^2 \theta} \\ &= 1 = \text{RHS} \end{aligned}$	1	-0.5 if solution is not in terms of $\cos \theta \equiv \sin \theta$
		1/2	-1 mark for not giving reasons

Qn	Solutions	Marks	Comments: Criteria
Q5c)	$\sin \theta = -\frac{4}{11}$ (3rd or 4th) $\tan \theta > 0$ (1st or 3rd) $\therefore \theta$ in 3rd quad $\checkmark$ $\cos \theta = -\frac{\sqrt{105}}{11}$ $\checkmark$ +1 for correct ratio 	2	-0.5 if not exact form
Q6)	$3x^2 + 7x - 4 = 0$ $\alpha + \beta = -\frac{b}{a} = -\frac{7}{3} \checkmark$ $\alpha \beta = \frac{c}{a} = -\frac{4}{3} \checkmark$ $(\alpha + \beta)^2 = \alpha^2 + 2\alpha\beta + \beta^2$ $\therefore \alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta \checkmark$ $= \left(-\frac{7}{3}\right)^2 - 2\left(-\frac{4}{3}\right)$ $= \frac{49}{9} + \frac{8}{3} \checkmark$ $= 8\frac{1}{9} \checkmark$	3	
Q7)			

Qn	Solutions	Marks	Comments: Criteria
Q5 (i)	In $\triangle ABF \not\sim \triangle ECF$ , we have $\angle AFB = \angle EFC$ (vert. opp. $\angle$ s) ✓ $\angle ABF = \angle ECF$ (alt. $\angle$ s, $AB \parallel DE$ ) ✓ $\therefore \triangle ABF \sim \triangle ECF$ (equiangular) ✓	2	
(ii)	$FC = 16 - 10$ $= 6$ (opp. sides of parallelogram)		
	$\frac{AB}{CE} = \frac{BF}{CF}$ (corresponding sides of 2 similar $\triangle$ s)	1	
	$\frac{AB}{9} = \frac{10}{6}$		
	$6AB = 90$		
	$AB = \frac{90}{6}$		
	$\therefore AB = 15 \text{ cm}$		

Qn	Solutions	Marks	Comments: Criteria
Q6 (a)	$(x-2)^2 = 8(y+3)$	1	
(i)	$V(2, -3)$	1	
(ii)	$4a = 8$ $a = 2$		
(iii)		1	
(iv)	Directrix: $y = -5$	1	
(v)	see part (iii)	1	
(b)	$\frac{AE}{ED} = \frac{AB}{BC}$ ( $\parallel$ lines cut off intercepts in the same ratio)		
	$\frac{AE}{6} = \frac{7}{4}$		
	$4AE = 42$		
	$AE = 10\frac{1}{2}$		
	$\therefore AD = AE + ED$ $= 10\frac{1}{2} + 6$ $= 16\frac{1}{2} \text{ cm}$	1	

Qn	Solutions	Marks	Comments: Criteria
Q6(c)	$9x^2 + 2x - 5 = ax(x+1) + b(x+1) + c$ $= ax^2 + ax + bx + b + c$ $= ax^2 + x(a+b) + b+c$ $\boxed{a=9}$ $a+b=2$ $9+b=2$ $b=2-9$ $\boxed{b=-7}$ $b+c=-5$ $-7+c=-5$ $c=-5+7$ $\boxed{c=2}$ $9x^2 + 2x - 5 = 9x(x+1) - 7(x+1) + 2$ <p>(d) <math>kx^2 - 4x + k</math> (positive definite  <math>\therefore k &gt; 0</math> and <math>\Delta &lt; 0</math>)</p> $\Delta = b^2 - 4ac$ $= (-4)^2 - 4k \cdot k$ $= 16 - 4k^2$ $16 - 4k^2 < 0$ $4(4 - k^2) < 0$ $4(2 - k)(2 + k) < 0$ $\therefore k > 2 \text{ or } k < -2$ 	3	
		2	

Qn	Solutions	Marks	Comments: Criteria
Q7(a)	$\lim_{x \rightarrow \infty} \frac{3x^2 - 2x - 6}{4 - 2x^2}$ $= \lim_{x \rightarrow \infty} \frac{\frac{3x^2}{x^2} - \frac{2x}{x^2} - \frac{6}{x^2}}{\frac{4}{x^2} - \frac{2x^2}{x^2}}$ $= \lim_{x \rightarrow \infty} \frac{3 - \frac{2}{x} - \frac{6}{x^2}}{\frac{4}{x^2} - 2}$ $= \frac{3}{-2}$ $(b) x^2 - (k+4)x + (k-3) = 0$ <p>i) If one of the roots is -2      Then <math>x = -2</math> must satisfy the equation</p> $\therefore (-2)^2 - (k+4)(-2) + k-3 = 0$ $4 + 2(k+4) + k - 3 = 0$ $4 + 2k + 8 + k - 3 = 0$ $3k + 9 = 0$ $k = -\frac{9}{3}$ $k = -3$ <p>ii) Let the roots be <math>\alpha</math> &amp; <math>\frac{1}{\alpha}</math></p> $\alpha \cdot \frac{1}{\alpha} = \frac{c}{a}$ $1 = \frac{k-3}{1}$ $\therefore k = 4$	1	Some have $\frac{-6}{4}$ from $\frac{3x^2 - 2x - 6}{4 - 2x^2}$ $\frac{3}{2} = \frac{1}{2} m.$
		1	

Qn	Solutions	Marks	Comments: Criteria
d) b) (iii)	<p>Let the roots be <math>\alpha \pm i\alpha</math></p> $\alpha + (-\alpha) = -\frac{b}{a}$ $\alpha - \alpha = -\frac{b}{a}$ $0 = -\frac{(k+4)}{1}$ $k+4=0$ $\therefore k=-4$	1	
c)	$x^4 = 8(x^2 + 6)$ $x^4 = 8x^2 + 48$ $x^4 - 8x^2 - 48 = 0$ <p>Let <math>m = x^2</math></p> $m^2 - 8m - 48 = 0$ $(m-12)(m+4) = 0$ $m=12 \text{ or } m=-4$ $x^2 = 12 \quad x^2 = -4$ <p><math>x = \pm \sqrt{12}</math>      no real solution</p> $x = \pm 2\sqrt{3}$	2	

Qn	Solutions	Marks	Comments: Criteria
d) f) (i)	$\frac{d}{dx} \left( \frac{3x^2 - 5}{2x+1} \right)$ $\begin{array}{l l} \text{let } u = 3x^2 - 5 & v = 2x+1 \\ u' = 6x & v' = 2 \end{array}$ $\begin{aligned} \frac{d}{dx} \left( \frac{3x^2 - 5}{2x+1} \right) &= \frac{u'v - v'u}{v^2} \\ &= \frac{6x(2x+1) - 2(3x^2 - 5)}{(2x+1)^2} \\ &= \frac{12x^2 + 6x - 6x^2 + 10}{(2x+1)^2} \\ &= \frac{6x^2 + 6x + 10}{(2x+1)^2} \end{aligned}$	2	
(ii)	$\frac{d}{dx} \left( \sqrt[5]{(2x+7)^2} \right)$ $\begin{aligned} &= \frac{d}{dx} \left( (2x+7)^{\frac{2}{5}} \right) \\ &= \frac{2}{5} (2x+7)^{\frac{2}{5}-1} \cdot 2 \\ &= \frac{4}{5} (2x+7)^{-\frac{3}{5}} \\ &= \frac{4}{5 \sqrt[5]{(2x+7)^3}} \end{aligned}$	2	

Qn	Solutions	Marks	Comments: Criteria
Q7(a)	For the quad. eqn. to have equal roots $\Delta = 0$		
	i.e. $b^2 - 4ac = 0$		
	$[2b(a-c)]^2 - 4(a^2 - b^2)(b^2 - c^2) = 0$	✓	
	$4b^2(a-c)^2 - 4(a^2b^2 - a^2c^2 - b^4 + b^2c^2) = 0$		
	$4b^2(a^2 - 2ac + c^2) - 4a^2b^2 + 4a^2c^2 + 4b^4 - 4b^2c^2 = 0$		
	<del><math>4a^2b^2 - 8ab^2c + 4b^2c^2</math></del> $= 4a^2b^2 + 4a^2c^2 + 4b^4 - 4b^2c^2 = 0$		
	$-8abc + 4a^2c^2 + 4b^4 = 0$	✓	
	$4(b^4 - 2acb^2 + a^2c^2) = 0$	2	
	$4(b^2 - ac)^2 = 0$		
	$(b^2 - ac)^2 = 0$	✓	
	$b^2 - ac = 0$		
	$b^2 = ac$	✓	