Name:	!	Class:	

## St George Girls High School

Year 9

**Common Test 1** 

**May 2008** 



# **Mathematics**

Time Allowed: 75minutes

Marks 74

## **Instructions:**

- Set out work clearly
- Show all working when required.
- Calculators may be used.

	Marks
Section A	/20
Section B	
Question 1	/13
Question 2	_/13
Question 3	/14
Question 4	714
Total	/74

#### **SECTION A**

20 questions - 1 mark each. (Answers only in the ANSWER column).

QUESTION	ANSWER
1. Expand $5x(2x-7)$	
2. Express 3 570 000 in scientific notation	
3. Find the area of the parallelogram  9.4 cm  15.8 cm  NOT DRAWN TO SCALE	-
4. This spreadsheet shows winners of a book award	

	Α	В	C
1	Year	Author	Title
2	2001	Frances Clarke	A Town's Lament
3	2002	Jill Saunders	Kitten and Snake
4	2003	Jeff Hardy	The Quiet Room

What is the content of cell B3?

- (A) 2003
- (B) Jill Saunders
- (C) Kitten and Snake
- (D) Jeff Hardy
- 5. Solve the equation.

$$\frac{5n+3}{6} = 8$$

QUESTION	ANSWER
6. Change 8⋅104×10 <sup>-7</sup> to its basic numeral	
7. Find the perimeter of the triangle (1 decimal place)	
NOT DRAWN TO SCALE	
8. Write $\sqrt[4]{y^3}$ in full index notation	
9. Solve the equation. $(y+5)^2 = 36$	
10. Estimate the result of 9.476×17.489	
11. Factorise fully $12m^3 - 9m^2$	
12. Change the subject of the equation to $m$ . $k = mn - y$	
13. A rectangular swimming pool is 25 metres long by 8 metres wide and is surrounded by a path of width 1 metre.  What is the perimeter around the outside edge of the path?	

## QUESTION

**ANSWER** 

14. The students of Jones High School need to purchase their own textbooks. This spreadsheet shows the cost of each textbook to be purchased by Felicity Howard, a year 9 student.

	$\mathbf{A}$	В	Ċ
1	Felicity Howard		
2			
3	Textbook	Price	
4	Mathematics	\$42.85	
5	English	\$31.45	
6	Science	\$64.95	
7	History	\$23.95	
8	Creative Arts	\$18.00	
9			

If the formula =B4+B5+B6+B7+B8 is entered into cell B1, what value is shown in B1?

- 15. A rhombus has one diagonal equal to 12 cm and has an area of 78 cm<sup>2</sup>. What is the length of the other diagonal?
- 16. Express 27 kg/h in g/s.
- 17. Simplify by expanding the brackets.

$$(27x^6y^3)^{\frac{1}{3}}$$

Questions 18. and 19. relate to the following spreadsheet.

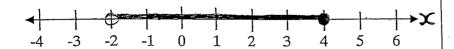
This spreadsheet shows the times taken for a group of students to each walk 50 metres. The speed of each student was calculated using a formula.

	$^{+}$ $^{-}$ $^{-}$ $^{-}$ $^{-}$ $^{-}$	В	C
. 1	Name	Time(s)	Speed (m/s)
2	Sarah	25	2.00
3	Ben ·	22	2.27
4	Alex	27	1.85
5	Cynthia	30	1.67
- 6	Rhys	18	2.78
7	Michael	19	2.63
- 8	Ellen	20	2.50
9	Maria	16	3.13

- 18. What formula could be entered into cell C2 to get the result shown (the formula must use a cell address)?
- 19. After entering the formula into cell C2, which option allowed the formula to be copied into the remaining cells?
  - (A) Cut and Paste
- (C) Fill Down

(B) Replace

- (D) Sort
- 20. Write the inequality that is represented by the diagram



End of Section A

#### **SECTION B**

Show all necessary working in the space provided.

**MARKS** 

#### Ouestion 1 – (13 marks) Rational Numbers – Show all working

- (a) Evaluate giving your answer in scientific notation correct to 3 significant figures.
  - (i)  $4.86 \times 10^{-3} + 5.97 \times 10^{-2}$

2

(ii)  $3.75 \times 10^6 \div 6.28 \times 10^{10}$ 

2

- (b) A worker in a local factory earns \$12.72 per hour.
  - (i) How much does she earn in a 40 hour week?

1

(ii) If she receives the same amount for the week's work but only works a 38 hour week, what will be her new hourly rate to the nearest cent?

1

(c) The temperature at 2:30 pm was 11° C and fell steadily until it reached -2° C at 1:45 am. Find the average rate of decrease per hour correct to 2 decimal places.

#### Question 1 (cont'd)

**MARKS** 

- (d) 18 litres of petrol are needed for a car to travel 261 km.
  - (i) How far would the same car travel on 13 litres of petrol?

1

(ii) How much petrol would the car use to travel 340 km?

1

- (e) For the calculation  $\frac{4.76 + (5.2)^2}{3.87}$ 
  - (i) Find the upper and lower boundary estimates

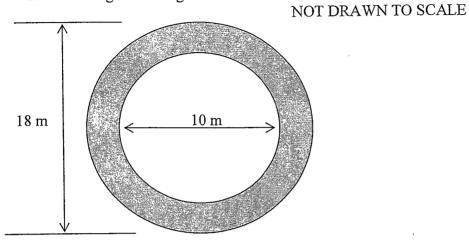
2

(ii) Calculate the answer correct to 2 decimal places.

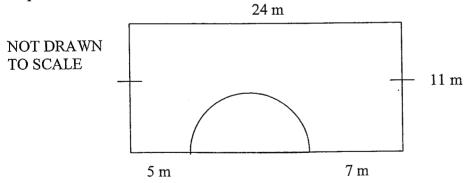
#### Question 2 - (13 marks) Measurement - Show all working

**MARKS** 

(a) A circular path with diameters is shown in the diagram. Find the shaded area correct to 3 significant figures.



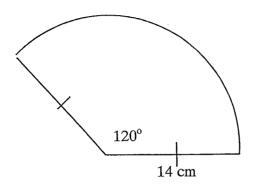
(b) A rectangular sheet of metal has a semicircle cut out of one side as shown. Find the perimeter correct to the nearest metre.



#### Question 2 (cont'd)

**MARKS** 

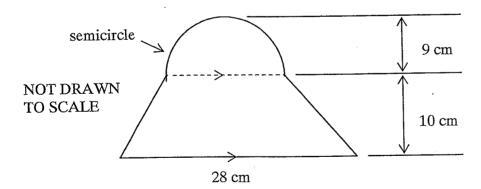
(c) Find the perimeter of the sector in centimetres correct to 2 decimal places.



NOT DRAWN TO SCALE

2

(d) Find the area of the composite shape in man correct to 2 decimal places.



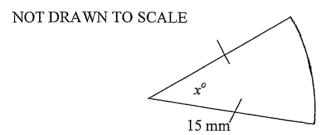
#### Question 2 (cont'd)

**MARKS** 

(e) A circle and a square have the same area. If the radius of the circle is 8 cm, find the length of each side of the square in centimetres correct to 2 decimal places.

2

(f) Find the size of the angle  $x^o$  in the sector correct to the nearest degree if its area is  $84 \, \text{cm}^2$ .



## Question 3 — (14 marks) Equations — Show all working

(a) Solve the equations

(i) 
$$3(5x-2)+3x = 2(7x+6)$$

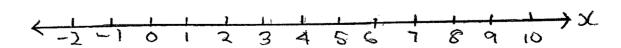
2

(ii) 
$$\frac{2m}{3m-4} = \frac{3}{5}$$

2

(b) Solve the inequation and display the solution on the number line.

$$5 - 3x \le -13$$



Question 3 (cont'd)

(c) Given that 
$$M = \frac{a^2 + b^2}{12}$$
 find a when  $M = 97.15$  and  $b = 19.65$ 

2

(d) Solve the inequation for x when we know that x is always positive

$$13 - 3x \ge 3 + 2x$$

2

- (e) Gladys has only 20 cent pieces and 50 cent pieces in her purse. The total value of these coins is \$12.30. She has two less 50 cent pieces than 20 cent pieces. Use x to represent the number of 20 cent pieces and:
  - (i) Form an equation from the above information.

2

(ii) Solve the equation and state how many 20 cent pieces she has in her purse

Question 4 – (14 marks) Algebra – Show all working

- (a) Expand (i)  $(4x + 5)^2$

(ii)  $\frac{-3}{4}n^2(4n^2-8n+5)$ 

- (b) Expand and simplify (i)  $2n(3n-2)-2(n-n^2)$
- (ii)  $n^2 (2n+1)(2n-1)$

- (c) Factorise fully (i)  $6m^2n 12mn + 18mn^2$
- (ii) (3x+1)(x+1)+5(x+1)

Question 4 (cont'd)

MARKS

- (d) Simplify (i)  $(x^{-3})^{-2}$
- (ii)  $m^0 \div m$
- (iii)

(e) Find x

 $9^x = 27$ 

End of Paper

#### SECTION A

20 questions - 1 mark each. (Answers only in the ANSWER column).

QUESTION	ANSWER
1. Expand $5x(2x-7)$ = $10x^2 - 35x$	10x2-35x
2. Express 3 570 000 in scientific notation	3.57×106
3. Find the area of the parallelogram  9.4 cm  12.7 cm  15.8 cm	9.4x15.8 = 148.52 cm <sup>2</sup>
4. This spreadsheet shows winners of a book award  A B C 1 Year Author Title 2 2001 Frances Clarke A Town's Lament 3 2002 Jill Saunders Kitten and Snake 4 2003 Jeff Hardy The Quiet Room	
What is the content of cell B3?  (A) 2003 (B) Jill Saunders (C) Kitten and Snake (D) Jeff Hardy	**
5. Solve the equation. $\frac{5n+3}{6} = 8$ $5n+3=48$ $5n=45$ $n=9$	n=9/

 $y^{2} + 10y + 25 = 36$   $y^{2} + 10y = 11$   $y^{2} + 5y + 5y + 5y + 25$   $y^{2} + 10y + 25$ 

Page 3

QUESTION	ANSWER
6. Change 8⋅104×10 <sup>-7</sup> to its basic numeral	0,0000008104
7. Find the perimeter of the triangle (1 decimal place)  14 cm  8 cm  NOT DRAWN TO SCALE	38.1 cm / (correct to I decimal place)
8. Write $\sqrt[4]{y^3}$ in full index notation	y 34 J
9. Solve the equation. $(y+5)^2 = 36$	; y2+10y=1)
10. Estimate the result of 9.476×17.489	9.5x17.5 = 166.25
11. Factorise fully $3m^2(4m-3)$ $12m^3-9m^2$	3m2(4m-3)
12. Change the subject of the equation to $m$ . $k = mn - y$ $k = mn - y$ $k = mn - y$	m=k+y
13. A rectangular swimming pool is 25 metres long by 8 metres wide and is surrounded by a path of width 1 metre. What is the perimeter around the outside edge of the path?	JAM.

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	QUESTION		ANSWER
<ol> <li>The students of Jor own textbooks. Thi textbook to be pure student.</li> </ol>	\$181.20		
			ψι -1. 20
A	В	C	
1 Felicity Howard		ļ <u> </u>	
2   3   Textbook	n.:		
4 Mathematics	Price 942.95		
5 English	\$42.85 \$31.45		
6 Science	\$64.95		
7 History	\$23.95		
8 Creative Arts	\$18.00		
9			
15. A rhombus has on area of 78 cm <sup>2</sup> . W	e diagonal equal to 12 cm hat is the length of the oth	er diagonal?	length of the other diagonal is 13 cm
16. Express 27 kg/h is 27000 g 450 g 7.50	7.5g/s.V		
17. Simplify by expa	nding the brackets.		j
(27x°y³) <sup>½</sup> 3x²y			3×24 V
3562	)		J

Questions 18. and 19. relate to the following spreadsheet.

This spreadsheet shows the times taken for a group of students to each walk 50 metres. The speed of each student was calculated using a formula.

7. j	A	В	C
1	Name	Time(s)	Speed (m/s)
, 2	Sarah	25	2.00
-6-3	Ben	22	2.27
- 4	Alex	27	1.85
5	Cynthia	30	1.67
- 6	Rhys	18	2.78
7.	Michael	19	2.63
- 8	Ellen	20	2.50
- 9	Maria	16	3.13

18. What formula could be entered into cell C2 to get the result shown (the formula must use a cell address)?

50 + B2

50+B2=02

- 19. After entering the formula into cell C2, which option allowed the formula to be copied into the remaining cells?
  - (A) Cut and Paste

((C)) Fill Down

(B) Replace

(D) Sort

20. Write the inequality that is represented by the diagram

-2< x < 4

End of Section A

#### SECTION B

Show all necessary working in the space provided.

MARKS

#### Ouestion 1 – (13 marks) Rational Numbers – Show all working

(a) Evaluate giving your answer in scientific notation correct to 3 significant figures.

(i)  $4.86 \times 10^{-3} + 5.97 \times 10^{-2}$ 

6.46 × 10-2 V

2

(ii)  $3.75 \times 10^6 \div 6.28 \times 10^{10}$ 

5.97x10-5

2

1

(b) A worker in a local factory earns \$12.72 per hour.

How much does she earn in a 40 hour week?

\$508,80

If she receives the same amount for the week's work but only works a 38 hour week, what will be her new hourly rate to the

\$13.40 is her new hourly rate

\$508.80 = 13,39

(c) The temperature at 2:30 pm was 11° C and fell steadily until it reached -2° C at 1:45 am. Find the average rate of decrease per hour correct to 2 decimal places.

1.18° of decrease per hour.

13-111.25

Thus.

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Ouestion 1 (cont'd)

(d) 18 litres of petrol are needed for a car to travel 261 km.

How far would the same car travel on 13 litres of petrol?

14.5 km/per litte

188,5 km

How much petrol would the car use to travel 340 km?

23 11+4es

MARKS

1

(rounded to whole humber)

(e) For the calculation  $\frac{4.76 + (5.2)^2}{3.87}$ 

Find the upper and lower boundary estimates

8.5 ~ 9.6 7.5 8.5

5+27=32=8



1

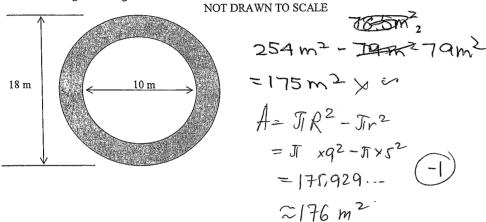
Calculate the answer correct to 2 decimal places.

8.2)

#### Question 2 – (13 marks) Measurement – Show all working

**MARKS** 

(a) A circular path with diameters is shown in the diagram. Find the shaded area correct to 3 significant figures.

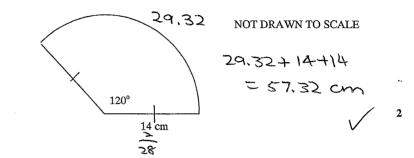


(b) A rectangular sheet of metal has a semicircle cut out of one side as shown. Find the perimeter correct to the nearest metre.

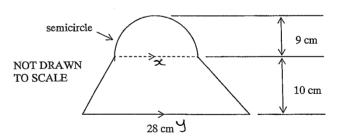
11+24+11+7+19+5=77m .:. the permeter is 77m. Question 2 (cont'd)

MARKS

(c) Find the perimeter of the sector in centimetres correct to 2 decimal places.



(d) Find the area of the composite shape in man correct to 2 decimal places.



trapezium =  $(x+y)h = (18+28)10 = 230 \text{ cm}_3^2$ Circle =  $\frac{1}{2}x71x92 = 127.23 \text{ cm}^2$ : total area is 357.23 cm<sup>2</sup>

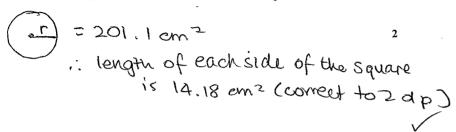
2

2

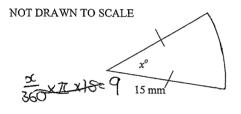
Question 2 (cont'd)

MARKS

(e) A circle and a square have the same area. If the radius of the circle is 8 cm, find the length of each side of the square in centimetres correct to 2 decimal places.



(f) Find the size of the angle  $\dot{x}^o$  in the sector correct to the nearest degree if its area is  $84 \frac{1}{1000}$ .



X 360 X 1EX 15° = 84 360 X

30 XII X

84 + 707 = 0.12 x 360

43°.

: the size of the angre xo= 43°



2

Question 3 – (14 marks) Equations – Show all working

(a) Solve the equations

(i) 
$$3(5x-2)+3x = 2(7x+6)$$
  
 $15x-6+3x=14x+12$   
 $18x-6=14x+12$   
 $4x-6=12$   
 $4x=18$   
 $x=41$ 

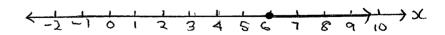
(ii) 
$$\frac{2m}{3m-4} = \frac{3}{5}$$
  
 $2mx5 = 3(3m-4)$   
 $10m = 9m-12$   
 $m = -12$ 

(b) Solve the inequation and display the solution on the number line.

$$5-3x \le -13$$

$$-3x \le -18$$

$$x \ge 6$$



MARKS

Ouestion 3 (cont'd)

(c) Given that  $M = \frac{a^2 + b^2}{12}$  find a when M = 97.15 and b = 19.65

$$97.15 = 0^2 + 19.65$$

1165.8 = 02 + 19.652

1146.15 = 02

+133.85 = a (correct to 2 do)

(d) Solve the inequation for x when we know that x is always positive

$$13 - 3x \ge 3 + 2x$$

$$13 \ge 3 + 5x$$

$$10 \ge 5x$$

$$2 \ge x$$

$$2 \le x$$

$$2 \le x$$

$$10 \le x = 0$$

$$10 < x \le 9$$

(e) Gladys has only 20 cent pieces and 50 cent pieces in her purse. The total value of these coins is \$12.30. She has two less 50 cent pieces than 20 cent pieces. Use x to represent the number of 20 cent pieces and:

(i) Form an equation from the above information.

0x + 50(x-2)20x+50x-100=\$1230 20x+50y-2x 20x150x=1330=2-2-2=

18x+50y=412.30

70x = 1330

20x+50x(x-2)=1230

X=19 her purse

(ii) Solve the equation and state how many 20 cent pieces she has in

20x +50(x-27 = 20x+50x-100=1230¢ V = 20x +50x = 1330¢ = 70x=1230 ¢

= x= 19

She has 19 20 cent preced

Ouestion 4 – (14 marks) Algebra – Show all working

(a) Expand (i)  $(4x+5)^2$  (4x+5)(4x+5) = 4x(4x+5)+5(4x+5)(ii)  $\frac{-3}{4}n^2(4n^2-8n+5)$   $\frac{-3}{4}n^2(4n^2-8n+5)$  $=16x^{2}+20x+20x+25/7-3n^{4}+6n^{3}-\frac{15}{4}n^{2}$ =16x2 440x425

(b) Expand and simplify (i)  $2n(3n-2)-2(n-n^2)$ 

(ii)  $n^2 - (2n+1)(2n-1)$ 

6n2-4n-2n+2n2 n22n2+  $=8n^2-6n$  022n(2n-1)+1(2n-1)

 $= 4n^2 - 2n + 2n - 1$ 

 $=4m^2-1$ n2-(4n2-1)

(c) Factorise fully

(i)  $6m^2n - 12mn + 18mn^2$ 

(ii) (3x+1)(x+1) + 5(x+1)

6mn(m-2+3h) 3x(x+1)+1(x+1)

= 3x2+3x+x+1 =3x2+4x+1+5x+5

= 3(x2+3x+2)=3(xt)(xt2), ym do need to expand first factorisms here factorisms

Question 4 (cont'd)

MARKS

(d) Simplify (i)  $(x^{-3})^{-2}$ 

(e) Find x

$$9^{x} = 27$$
 $3^{3}$ 
 $3^{3}$ 

28x=3

X=18232 or 11/2

End of Paper