

2015

HIGHER SCHOOL CERTIFICATE TRIAL PAPER

Mathematics

General Instructions

- Reading time 5 minutes.
- Working time 2 hours.
- Write using black or blue pen.
- Board approved calculators may be used.
- All necessary working should be shown in every question if full marks are to be awarded.
- Marks may NOT be awarded for messy or badly arranged work.
- Leave your answers in the simplest exact form, unless otherwise stated.
- Start each NEW question in a separate answer booklet.

Extension 1

(Section I)

Total Marks - 70

Pages 2-4

10 Marks

- Attempt Questions 1–10
- Allow about 15 minutes for this section.

Section II

Pages 6-11

60 marks

- Attempt Questions 11–I4
- Allow about 1 hour and 45 minutes for this section

Examiners: R. Elliot & J. Chen

This is an assessment task only and does not necessarily reflect the content or format of the Higher School Certificate.

HSC Mathematics

STANDARD INTEGRALS

$$\int x^{n} dx = \frac{1}{n+1} x^{n+1}, \ n \neq -1; x \neq 0, \text{if } n < 0$$

$$\int \frac{1}{x} dx = \ln x, \ x > 0$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax}, \ a \neq 0$$

$$\int \cos ax \, dx = \frac{1}{a} \sin ax, \ a \neq 0$$

$$\int \sin ax \, dx = -\frac{1}{a} \cos ax, \ a \neq 0$$

$$\int \sec^2 ax \, dx = \frac{1}{a} \tan ax, \ a \neq 0$$

$$\int \sec ax \tan ax \, dx = \frac{1}{a} \sec ax, \ a \neq 0$$

$$\int \frac{1}{a^2 + x^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a}, \ a \neq 0$$

$$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \frac{x}{a}, \ a > 0, \ -a < x < a$$

$$\int \frac{1}{\sqrt{x^2 - a^2}} dx = \ln\left(x + \sqrt{x^2 - a^2}\right), \ x > a > 0$$

$$\int \frac{1}{\sqrt{x^2 + a^2}} dx = \ln\left(x + \sqrt{x^2 + a^2}\right)$$

NOTE:
$$\ln x = \log_a x$$
, $x > 0$

Section I

10 marks

Attempt Questions 1-10

Allow about 15 minutes for this section

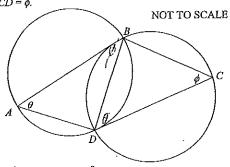
Use the multiple-choice answer sheet for Questions 1-10.

- 1. The roots of $3x^3 2x^2 + x 1 = 0$ are α , β and γ . What is the value of $\alpha^2 \beta \gamma + \alpha \beta^2 \gamma + \alpha \beta \gamma^2$?

 - (D)
- What is the minimum value of $\sqrt{7}\sin x 3\cos x$?
 - (A)
 - (B)
 - (B)
- What is the domain and range of $y = \sin^{-1}\left(\frac{2x}{5}\right)$?
 - Domain: $-1 \le x \le 1$;
- Range: $-\pi \le y \le \pi$
- Domain: $-1 \le x \le 1$;
- Range: $-\frac{\pi}{2} \le y \le \frac{\pi}{2}$
- Domain: $-\frac{5}{2} \le x \le \frac{5}{2}$; Range: $-\frac{\pi}{2} \le y \le \frac{\pi}{2}$
- (D) Domain; $-\frac{5}{2} \le x \le \frac{5}{2}$;
- Range: $-\pi \le y \le \pi$
- Evaluate $\lim_{x\to 0} \frac{\sin 3x}{2x}$.
 - (A)
 - (B)
 - (C)
 - (D)

In the diagram below, AB is a tangent to the circle BCD. Also, CD is a tangent to the circle ABD.

 $\angle BAD = \theta$ and $\angle BCD = \phi$.



Which of the following is a true statement?

- $\triangle ABD \equiv \triangle BDC$
- ABCD is a cyclic quadrilateral
- $\triangle ABD \parallel \triangle BDC$
- $AB \parallel CD$
- A particle moves in simple harmonic motion so that its velocity, v, is given by

$$y^2 = 6 - x - x^2$$
.

Between which two points does it oscillate?

- x = 6 and x = 3
- x = -2 and x = 3
- x = 1 and x = 2
- x = 2 and x = -3
- Which of the following is an expression for $\int \cos^3 x \sin x \, dx$?
 - (A) $-\cos^4 x + c$

 - $\cos^4 x + c$
 - (D) $\frac{1}{4}\cos^4 x + c$

- Which of the following is the correct expression for the inverse of $f(x) = e^{1-2x}$?
 - (A) $f^{-1}(x) = -2e^{1-2x}$
 - (B) $f^{-1}(x) = -\frac{1}{2}e^{1-2x}$
 - (C) $f^{-1}(x) = -\frac{1}{2}\log_{\epsilon}(1-2x)$
 - (D) $f^{-1}(x) = \frac{1}{2}(1 \log_e x)$
- 9 Three Mathematics study guides, four Mathematics textbooks and five exercise books are randomly placed along a bookshelf. What is the probability that the Mathematics textbooks are all next to each other?
 - (A) $\frac{41}{12!}$
 - (B) $\frac{9!}{12!}$
 - (C) $\frac{4!3!5}{12!}$
 - (D) $\frac{4191}{121}$
- 10 A particle moves on the x-axis with velocity v m/s, such that $v^2 = 16x x^2$. Which of the following is the particle's maximum speed and the position of where this maximum speed occurs?
 - Maximum speed = 16 m/s at x = 0
 - (B) Maximum speed = 8 m/s at x = -8
 - (C) Maximum speed = -8 m/s at x = 8
 - (D) Maximum speed = 8 m/s at x = 8

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Section II

60 marks

Attempt Questions 11-14

Allow about 1 hour and 45 minutes for this section

Answer each question in a NEW writing booklet. Extra pages are available

In Questions 11-14, your responses should include relevant mathematical reasoning and/or calculations.

Question 11 (15 Marks) Start a NEW Writing Booklet

(a) Differentiate $\sin^{-1}(\log x)$.

(b) Find
$$\int \frac{1}{\sqrt{4-9x^2}} dx.$$

1

1

2

2

(c) (i) Simplify $\sin(A+B) + \sin(A-B)$.

(ii) Hence, evaluate
$$\int_0^{\frac{\pi}{6}} \sin 3x \cos x \, dx.$$
 2

(d) The point $P(6p, 3p^2)$ is a point on the parabola $x^2 = 12y$.

- (i) Find the equation of the tangent at P. 2
- (ii) The tangent at P cuts the y-axis at B.
 The point A divides PB internally in the ratio 1:2.
 Find the locus of the point A as P varies.
- (e) A piece of meat at temperature T° C is placed in an oven, which has a constant temperature of H° C.

The rate at which the temperature of the meat warms is given by

$$\frac{dT}{dt} = -K(T-H),$$

where t is in minutes and for some positive constant K.

- (i) Show that $T = H + Be^{-R}$, where B is a constant, is a solution of the differential equation above.
- (ii) If the meat warms from 10° C to 50° C in the oven, which has a constant temperature of 180° C, in 30 minutes, find the value of K.
- (iii) How long will it take the meat to get to a temperature of 150° C?

 Express your answer correct to the nearest minute.

Question 12 (15 Marks) Start a NEW Writing Booklet

- (a) (i) Solve $\cos x \sqrt{3} \sin x = 1$ for $0 \le x \le 2\pi$.
 - (ii) Hence, or otherwise, find a general solution to $\cos x \sqrt{3} \sin x = 1$.

1

2

- (b) (i) On the same set of axes sketch the graphs of $y = \cos 2x$ and $y = \frac{x+1}{3}$
 - (ii) Use the graph to determine the number of solutions to the equation 1

$$3\cos 2x = x+1$$

- (iii) One solution of the equation $3\cos 2x = x + 1$ is close to 0.5.

 Use one application of Newton's Method to find another approximation, correct to 3 decimal places.
- (c) Evaluate $\int_0^{\frac{\pi}{4}} \sin^2 2x \, dx$ 3
- (d) When x cm from the origin, the acceleration of a particle moving in a straight 3 line is given by:

$$\frac{d^2x}{dt^2} = -\frac{5}{\left(x+2\right)^3}$$

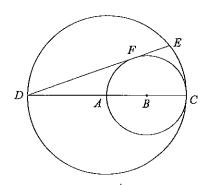
It has an initial velocity of 2 cm/s at x = 0. If the velocity is V cm/s, find V in terms of x.

Question 13 (15 Marks)

Start a NEW Writing Booklet

(a) In the diagram below, DC is a diameter of the larger circle centred at A.
 AC is a diameter of the smaller circle centred at B.
 DE is tangent to the smaller circle at F and DC = 12.

Copy the diagram to your answer booklet. Determine the length of *DE*.



(b) (i) Simplify $k! + k \times k!$

(ii) Prove, by mathematical induction, that

$$1 \times 11 + 2 \times 21 + 3 \times 31 + ... + n \times n! = (n+1)! - 1$$

for all positive integers n.

- (o) (i) Using the substitution $x = 3 + 3\sin\theta$ find $\int \sqrt{x(6-x)} dx$
 - (ii) Let R be the region bounded by the curve $y = \sqrt[4]{x(6-x)}$ and the x-axis. Find the volume of the solid of revolution generated by revolving R about the x-axis.

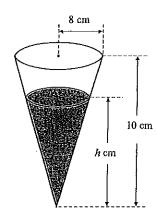
End of Question 13

Question 14 (15 Marks) Start a NEW Writing Booklet

(a)

1

3



The figure above shows an inverted conical cup with base radius 8 cm and height 10 cm.

Some water is poured into the cup at a constant rate of $\frac{2\pi}{5}$ cm³ per minute.

Let the depth of the water be h cm at time t minutes.

Find the rate of change in the area of the water surface when h = 4

b) A particle is projected horizontally at 30 ms⁻¹ from the top of a 100 m high wall.
Assume that acceleration due to gravity is 10 ms⁻² and that there is no air resistance.

The flight path of the particle is given by:

$$x = 30t$$
, $y = 100 - 5t^2$ (Do NOT prove this)

3

1

2

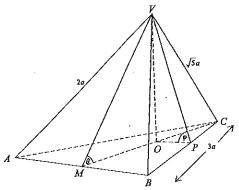
where t is the time in seconds after take-off.

- i) Find the time taken for the particle to reach the ground.
- ii) Find the angle and speed at which the particle strikes the ground.

Question 14 continues on page 11

Question 14 (continued)

(c) The diagram below shows a tetrahedron such that VA = VB = AB = 2a, CA = CB = 3a and $VC = \sqrt{5}a$. O is the foot of the perpendicular from V to the base ABC. M is the midpoint of AB. P is a point on BC such that BP = ra where $0 \le r \le 3$. $\angle VMC = \theta$ and $\angle VPO = \varphi$.



3

1

- (i) By considering $\triangle VMC$, show that $\cos \theta = \frac{\sqrt{6}}{4}$.
- (ii) Hence find the exact value of VO.
- (iii) Show that $VP^2 = \frac{1}{3} (3r^2 8r + 12)a^2$
- (iv) Hence show that $\sin \varphi = \sqrt{\frac{45}{8(3r^2 8r + 12)}}$
- (v) Hence, or otherwise, find the maximum value of φ as r varies.

End of paper



2015

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Mathematics Extension 1 Sample Solutions

Question	Teacher
Q11	RB
Q12	BK
Q13	BD
Q14	PB

MC Answers

Q1	D
Q2	В
Q3	C
Q4	D
Q5	C
Q6	D
Q7	В
Q8	D
Q9	D
Q10	D

Section I

10 marks

- 1 The roots of $3x^3 2x^2 + x 1 = 0$ are α , β and γ . What is the value of $\alpha^2 \beta \gamma + \alpha \beta^2 \gamma + \alpha \beta \gamma^2$?
 - (A) $-\frac{1}{9}$
 - (B) $-\frac{2}{9}$
 - $\begin{array}{c}
 \text{(C)} & 1 \\
 \text{(D)} & \frac{2}{9}
 \end{array}$

ANSWER: D

$$3x^3 - 2x^2 + x - 1 = 0$$

$$\alpha\beta\gamma = -\frac{d}{a} \qquad \alpha + \beta + \gamma = -\frac{b}{a}$$

$$= \frac{1}{3} \qquad \qquad = \frac{2}{3}$$

$$\alpha^2\beta\gamma + \alpha\beta^2\gamma + \alpha\beta\gamma^2 = \alpha\beta\gamma(\alpha + \beta + \gamma)$$

$$= \frac{1}{3} \times \frac{2}{3}$$

$$= \frac{2}{9}$$

- 2 What is the minimum value of $\sqrt{7} \sin x 3\cos x$?
 - (A) -2
 - (B) -4
 - (B) -16
 - (D) $\sqrt{7} 3$

ANSWER: B

$$\sqrt{7} \sin x - 3\cos x$$

$$r = \sqrt{(\sqrt{7})^2 + 3^2}$$

$$= \sqrt{7 + 9}$$

$$= 4$$
Let $\sqrt{7} \sin x - 3\cos x = r\sin(\theta - \alpha)$

$$= 4\sin(\theta - \alpha)$$
No matter what the value of α

$$-1 \le \sin(x - \alpha) \le 1$$

Therefore the minimum value is x = -4.

 $-4 \le 4\sin(x-\alpha) \le 4$

- What is the domain and range of $y = \sin^{-1}\left(\frac{2x}{5}\right)$? 3
 - Domain: $-1 \le x \le 1$:

Range: $-\pi \le y \le \pi$

- Domain: $-1 \le x \le 1$;
- Range: $-\frac{\pi}{2} \le y \le \frac{\pi}{2}$
- (C) Domain: $-\frac{5}{2} \le x \le \frac{5}{2}$; Range: $-\frac{\pi}{2} \le y \le \frac{\pi}{2}$
- (D) Domain: $-\frac{5}{2} \le x \le \frac{5}{2}$; Range: $-\pi \le y \le \pi$

ANSWER: C

$$y = \sin^{-1}\left(\frac{2x}{5}\right) \Rightarrow \sin y = \left(\frac{2x}{5}\right)$$

Domain: $-1 \le \sin y \le 1$

$$-1 \le \frac{2x}{5} \le 1$$

$$\frac{-5}{2} \le x \le \frac{5}{2}$$

Range: $-\frac{\pi}{2} \le y \le \frac{\pi}{2}$ as this is the range of $y = \sin^{-1} x$

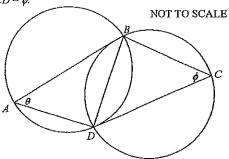
- Evaluate $\lim_{x\to 0} \frac{\sin 3x}{2x}$
 - (A)

ANSWER: D

$$\lim_{x \to 0} \frac{\sin 3x}{2x} = \frac{3}{2} \lim_{x \to 0} \frac{\sin 3x}{2x} \times \frac{2}{3}$$
$$= \frac{3}{2} \lim_{x \to 0} \frac{2\sin 3x}{2 \times 3x}$$
$$= \frac{3}{2} \times 1$$
$$= \frac{3}{2}$$

In the diagram below, AB is a tangent to the circle BCD. Also, CD is a tangent to the circle ABD.

 $\angle BAD = \theta$ and $\angle BCD = \phi$.



Which of the following is a true statement?

- $\Delta ABD \equiv \Delta BDC$
- ABCD is a cyclic quadrilateral



 $\Delta ABD ||| \Delta BDC$

 $AB \parallel CD$

ANSWER: C

In $\triangle ABD$ and $\triangle DCB$:

 $\angle DCB = \angle DBA$ (angle in the alternate segment)

ie $\angle DCB = \angle ABD$

 $\angle BAD = \angle BDC$ (angle in the alternate segment)

ie $\angle BAD = \angle CDB$

BD is but not respective to angles.

Therefore $\triangle ABD \neq \triangle DCB$

Hence, triangles are equiangular they are similar and $\Delta ABD \parallel \Delta DCB$

A particle moves in simple harmonic motion so that its velocity, ν , is given by

$$v^2 = 6 - x - x^2$$
.

Between which two points does it oscillate?

- x = 6 and x = 3
- x = -2 and x = 3
- x = 1 and x = 2
- x = 2 and x = -3

ANSWER: D

 $v^2 = 6 - x - x^2$

For the particle to reach its oscillation points v = 0.

$$v^2 = 6 - x - x^2$$

$$0 = 6 - x - x^2$$

$$0 = (3+x)(2-x)$$

 $\therefore x = -3 \text{ and } 2$

- Which of the following is an expression for $\int \cos^3 x \sin x \, dx$?
 - $-\cos^4 x + c$

 - (D) $\frac{1}{4}\cos^4 x + c$

ANSWER: B
$$\int \cos^3 x \sin x \, dx, \text{ testing solutions:}$$

$$\frac{d}{dx} (\cos^4 x) = 4\cos^3 x \times -\sin x$$

$$\frac{d}{dx} - \frac{1}{4} (\cos^4 x) = \cos^3 x \sin x$$

$$-\frac{1}{4} \cos^4 x = \int \cos^3 x \sin x \, dx$$

- Which of the following is the correct expression for the inverse of $f(x) = e^{1-2x}$?
 - (A) $f^{-1}(x) = -2e^{1-2x}$

 - (B) $f^{-1}(x) = -\frac{1}{2}e^{1-2x}$ (C) $f^{-1}(x) = -\frac{1}{2}\log_{\epsilon}(1-2x)$ (D) $f^{-1}(x) = \frac{1}{2}(1-\log_{\epsilon}x)$

Let
$$y = e^{1-2x}$$

$$y = e^{1-2x}$$

$$\ln y = 1-2x$$

$$2x = 1 - \ln y$$

$$x = \frac{1}{2} (1 - \ln y)$$

$$\therefore f^{-1}(x) = \frac{1}{2} (1 - \ln y)$$

- 9 Three Mathematics study guides, four Mathematics textbooks and five exercise books are randomly placed along a bookshelf. What is the probability that the Mathematics textbooks are all next to each other?
 - (A) 12!
 - **(B)**
 - (C)

ANSWER: D

Since there are 9 elements counting the textbooks as 1 element, hence these can be arranged in 9! ways. Also the textbooks can be arranged in 4! ways.

As there are 12 separate elements, the divisor for population can be counted in 12! ways.

Therefore, the probability is $\frac{9!4!}{12!}$

- A particle moves on the x-axis with velocity v m/s, such that $v^2 = 16x x^2$. Which of the following is the particle's maximum speed and the position of where this maximum speed occurs?
 - Maximum speed = 16 m/s at x = 0(A)
 - Maximum speed = 8 m/s at x = -8
 - Maximum speed = -8 m/s at x = 8(C)
 - (D) Maximum speed = 8 m/s at x = 8

ANSWER: D

$$v^{2} = 16x - x^{2}$$

$$\frac{1}{2}v^{2} = 8x - \frac{x^{2}}{2}$$

$$\frac{d}{dx}\left(\frac{1}{2}v^{2}\right) = 8 - \frac{2x}{2}$$

$$= 8 - x$$

$$\ddot{x} = 8 - x$$

When $\ddot{x} = 0$ the speed is the greatest so, $\ddot{x} = 8 - x$

$$0=8-x$$

$$x = 8$$

At
$$x = 8$$
,

$$v^{2} = 16x - x^{2}$$
$$= 16(8) - (8)^{2}$$
$$= 64$$

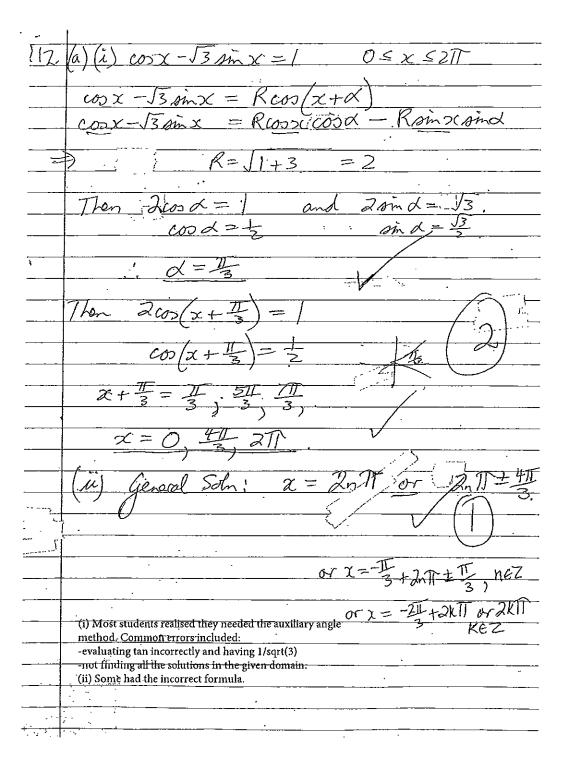
$$v = \pm 8$$

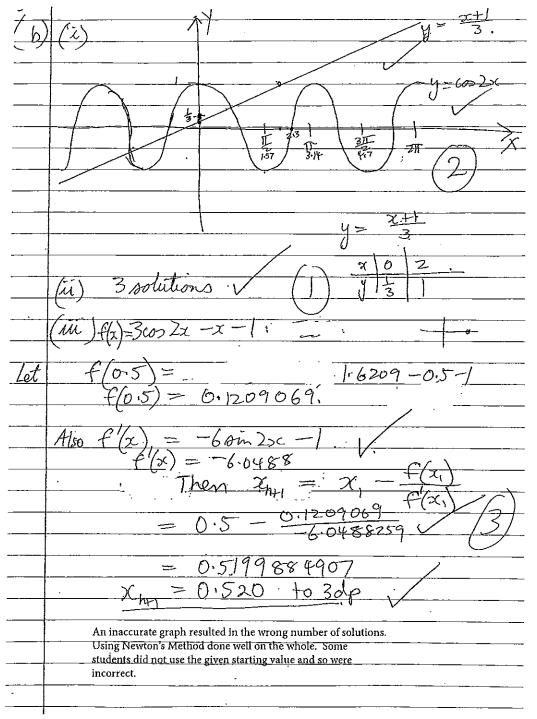
As v, velocity can take positive and negative values, but the speed can only be positive, the maximum speed is 8 m/s.

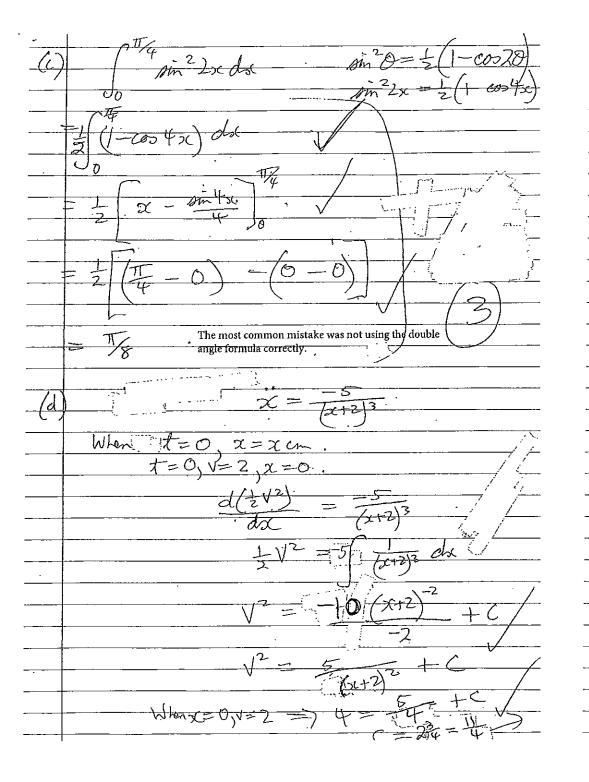
3 unit Trial 2015 Sydney Boys. (a) let y = sm (Inox, generally west out some students Joseph the 3: Others thought (Inse) = 2/nos or hox2 (b) generally well above but some students left off the 3 (C) (sin (A+B) + sin (A-B) SINA OSB + COSA/SINB + SINA COSB - COSA SINB (1) this part, very well answered by 95% 9 students. 2 sinfocus B sin 3x cos x dx 2 sin 3x cosx dis 2 [1: [sin4x + sin2x] da $= -\frac{1}{24} \left[\frac{4\sin 4x}{4\sin 4x} \right] \frac{dx}{4\cos 2x} = -\frac{1}{8} \cos 4x \right]_{0}^{2} = -\frac{1}{8} \cos 4x \right]_{0}^{2}$

(ii) (b) (ii) $\frac{M\chi_2 + n\chi_1}{m+n}$ My2+ny1 1x0+12p ,= Mapy students found A but could not find louis equation. 2 = 16y is the locus (ii) H = 180 All answered Using the method shown When E=0, T=10 Some boys wanted to integrale the oft and got into a lot of 10 = 180+Be 10 - 180 = BB=-170 T=180-170e 7=50

So
$$50 = 180 - 170e$$
 $-130 = -170e$
 $(\frac{13}{17}) = e^{-30k}$
 $\ln(\frac{13}{17}) = \ln e$
 $\lim_{n \to \infty} \frac{1}{17} = 1 \ln e$
 $\lim_{n \to \infty$



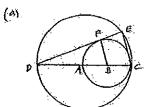




	(d) (ant)
	(4)
	V2= 1/x+2/2 + 4
	. (2)
	"V>O since v can nover be O
	Also when $t=0, V=2$ and $d^2x = 0 \Rightarrow do reasing$
	del 10 = decreasing
	at speed
	11/- 5-11:
	(x+2)2 4
_	
	The most common error was to differentiate the given function in
	terms of t.
	Half a mark was deducted if no statement about sign of v was
	included.
	·
	•

Solutions Q13 X1 THSC 2015

Average mark: 11.31/15



FB L DF (radius L tangent at point of contract)

DB2 = FBA+ DF2 (Pythygonis Theoren) 1. 92 = 37 +DF3

\$ DE = 74 2, DF = (12)

BELDE (DC is a dinnete 1. Loep=900, apple in a semicircle)

L. A DEF III & DEE (agricangular) AS CO IS COMMON Z DEB = Z bec = 90° (as linkedled above)

1. DE = DC (correspondos) rides in similar tonorples)

= 812

There repred to be a relictmen to give reasons for geometrical concusions

0	0.5	1	1.5	2	2.5	3	3.5	4	Mean
7	6	11	14	25	8	20	22	49	2.70

(i) KI+KXKI = K! (1+K) = (K#I) }

> Done well although some Stopped at K! (1+K)

(1)

0	0.5	1	Mean
6	18	138	0.91

(11) 5(h) = 1x11+2x21+ ...+1xn1=(0+1)(-1 Show S(1) is time (2 1x) = 2 -1 LH5 =1 RHSFLET 1/2 5(1) 15 HEREL Assume SCR) IT-true le 1x11+2x21+-++++(=(++))-) Show SCKTO Is the TE 18/14-24214-44 WKK 4 (KH) x (KH) = (((+2)) LHS = (RH) ! -] + (KH) x (KH) ! = (84)) (FARE) -4 = (146) (1442) =1 =(K+2)1 -1 = RIFS If ster is true, state) is true say is true, and, of say who school is true 1. By the process of Mediaratel Eduction, S(n) is time As all integral " >1. (3)

an understanding of the process of Matiendreal Industrian; However, wany statements were stoppy, For example, "Assime hek" tother than " Assume he statement prima if n= K" or having defined the statement of SIN) as above, "Assume that stry is frue! Many concluding statement were also sloppy.

ļ	0	. 0.5	1	1.5	2	2.5	3	Mean
1	2	8	2	3	0	4	143	2.77

(6) i) If x=3+351nB+, die a 3 cos & and sin 0 = 3 = 3 √x (6+x) dx = J (3+8 sind) (6-3-35ind) Bear Odl = [3] (1-8n20) 3 w/o dos # 9 Just 20 110

HOTEL DINGINAL INTERNAL IS POSITIVE

= 9 5 cor20 +1 do-

Most students demonstrated

= = [(x-3) (3(6-20) + 95/m = 3) + C
Many students found that integration challenging . Some lift the integral at the form
9 [sindeno +p]+0 or returning equivalent rather than returning to an exprastron interms of a

0 0.5 1 1.5 2 2.5 3 3.5 4 Mean

3 | 5 | 11 | 4 | 20 | 15 | 25 | 24 | 55

= = 1 [sin20 + 2] +c

= = [sin & cor8 + 0] + c

= 9 [2-3 /1-80] +511-1×3 +C

文皇[2] [W-12 +5] 214C

(II)	V= To (Vx	
	$= \pi \int_{0}^{C} \sqrt{x/\epsilon}$	(x) dx
	三 电水量 [12-3	(x16-x)+954 (3)
	= 美間かり	[]-[9 six (c)]}
	= 罢 { 4. 芒	4
	= 92	(3)

Nort who progressed through found the appropriate (i) (i) volume.

	0	0.5	1	1.5	2	2.5	3	Mean
i	15	10	21	4	24	23	65	2.05

when h=4

COMMENT not particularly well down.

many students treated has a

Contact in the differentiation

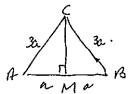
$$0 = \tan^{2} \frac{2\sqrt{5}}{3}$$

COMMBNT

Common earl was

$$VM = 2a \sin 60^{\circ}$$

= $2a \sqrt{3}$
 $VM = a\sqrt{3}$.



$$CVOO = CM^{2} + VM^{2} - VC^{2}$$

$$= 8a^{2} + 3a^{2} - 5a^{2}$$

$$= 2 \times a\sqrt{3} \times 2\sqrt{2}a$$

$$= \frac{6a^{2}}{4\sqrt{6}a^{2}}$$

$$\therefore \left| cOOO = \sqrt{6} \right|$$

COMMENT. Unite well done.

(")
$$Vo = VM \text{ sin } 0.$$
 $line = 1 - \frac{6}{16}$
= $a\sqrt{3} = \frac{\sqrt{10}}{4}$ = $a\sqrt{30}$ $i. A = \frac{\sqrt{10}}{4}$

COMMENT.

many students unable to find ano.

(III)
$$\cos \sqrt{\beta} c = (2a)^2 + (3a)^2 - (\sqrt{5}a)^2$$

$$= 4a^2 + 9a^2 - 5a^2$$

$$= \frac{4}{3}$$

commint very few students were able to obtain this answer.

Theremon eres was to assure

DCOP III D CMB. Lence finding an expension for or then using By chagrons to stain VP? (this was not given marks)

$$\frac{1}{2} = \frac{2\sqrt{30}}{4}$$

$$\frac{1}{2} + \frac{3\sqrt{2} - 8\sqrt{3}}{2}$$

$$\frac{90}{4\sqrt{12} + \frac{3\sqrt{2} - 8\sqrt{3}}{2}}$$

$$\frac{\sqrt{45}}{\sqrt{8(12 + \frac{3\sqrt{2} - 8\sqrt{3}}{2})}}$$

COMMENT-

most attained a mark, allewing for previous error in vo. (V). Best done by necognizing

that sin of is maximized by 3-12-8-1+12 being a minim this occurs when 65-8=0

ii. ein \$ = \ \ \frac{45}{8(3r^2-8142)} refer = \(\frac{45 \times 9}{8 \times 60} \) :1/4 = mi 3/6

COMMENT. able to obtain a mark to two.

many maximied in & log Colonlus. Lew son the easier approach.