

Question 1:[10 marks]

(a) Simplify (i)  $2\sqrt{125} - 4\sqrt{80}$  [1]

(ii)  $(3\sqrt{2} - 1)^2$  [1]

(b) Show that  $\frac{1}{3-\sqrt{2}} + \frac{1}{3+\sqrt{2}}$  is rational. [2]

(c) Factorise fully and simplify where possible (i)  $x^6 - 64$  [2]

(ii)  $\frac{2x^2 - 7x + 3}{x^2 - 9}$  [2]

(d) Find  $0.\dot{0}\dot{2}\dot{7}$  as a simple fraction [2]

$$\begin{array}{l} 2x^2 + 7x + 15 \\ \hline x^2 - 9 \end{array}$$

Question 2:[10 marks]

(a) Expand  $(2a+b)^3$   $a^3 + 3a^2b + 3ab^2 + b^3$  [2]

(b) Solve

(i)  $\frac{x+2}{3} + \frac{x}{4} = 7$  [2]

(ii)  $|2x-3| = |3x-7|$  [3]

(iii)  $4x^3 + 7x^2 - 2x = 0$  (hint: factorise first) [3]

**Question 3:****[10 marks]**

Find the values of  $x$  which satisfy the following inequalities:

(i)  $-3(x - 5) \leq 3$  [2]

(ii)  $x^2 - 7x + 12 < 0$  [2]

(iii)  $|5 + 2x| < 3x - 1$  [3]

(iv)  $\frac{3x - 2}{x + 4} < 1$  [3]

**Question 4:****[10 marks]**

(a) What is the domain and range of the function  $f(x) = \frac{3}{\sqrt{x-1}}$  [2]

(b) Is the function  $f(x) = \frac{x^3}{x^2 - 1}$  odd, even or neither? Support your answer. [2]

(c) Sketch the graph of  $|x| + |y| = 1$  (hint: do it quadrant by quadrant) [3]

(d) Solve  $\sqrt{x} + \sqrt{3x+1} = 3$  [3]

Q1

a) i)  $2\sqrt{5}\sqrt{11} - 4\sqrt{16 \times 5}$

$$= 10\sqrt{5} - 16\sqrt{5}$$

$$= -6\sqrt{5}$$

9  
10

ii)  $18 - 6\sqrt{2} + 1$

$$= 19 - 6\sqrt{2}$$

b)

$$\frac{3+\sqrt{2} + 3-\sqrt{2}}{9-2} = \frac{6}{7} \text{ -- a fraction } \therefore \text{ rational}$$

c) i) let  $x^2 = a$ ,  $4 = b$

$$(a^3 - b^3) = (a-b)(a^2 + ab + b^2)$$

$$= (x^2 - 4)(x^4 + 4x^2 + 16) \quad \text{let } x^2 = a$$

$$= (x^2 - 2)(x^2 + 2)(x^4 + 4x^2 + 16) \quad \text{difference of 2 squares}$$

$$\text{or difference of 2 squares } \therefore (x-2)(x+2)(x^2-2x+4)(x^2+2x+4)$$

$$\text{ii) } \frac{2x^2 - 6x - x + 3}{(x+3)(x-3)} = \frac{2x(x-3) - (x-3)}{(x+3)(x-3)} = \frac{(2x-1)(x-3)}{(x+3)(x-3)}$$

$$= \frac{2x-1}{x+3} \quad \checkmark$$

d) Let  $0.\overline{027} = x$

$$1000x = 27.\overline{027}$$

$$10x = 0.\overline{027}$$

$$990x = 27$$

$$x = \frac{27^3}{990} = \frac{3}{110} \quad \checkmark$$

## Q 2

a)  $\frac{8}{10} \quad (a+b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$

$(2a+b)^3 = 8a^3 + 3 \times 4a^2 \times b + 3 \times 2a \times b^2 + b^3$   
 $= 8a^3 + 12a^2b + 6ab^2 + b^3$

b) i)  $\frac{x+2}{3} + \frac{2}{4} = 7$

$4(x+2) + 3x = 84$

~~$4x+8 + 3x = 84$~~

$7x = 76$

$x = \frac{76}{7}$

ii) Either  $2x - 3 = 3x - 7$

$4 = x$

or

$2x - 3 = -(3x - 7)$

$2x - 3 = -3x + 7$

$5x = 10$

$x = 2$

check answers.

iii)  $x(4x^2 + 7x - 2) = 0$

$x(4x^2 + 8x - x - 2) = 0$

$x(4x(x+2) - (x+2)) = 0$

$x(4x-1)(x+2) = 0$

$x = 0, \frac{1}{4} \text{ or } -2$

///

$\frac{2}{2}$

$\frac{10}{10}$

Fail

(except ...)

$\frac{2}{2}$

$\frac{3}{3}$

$\frac{3}{3}$

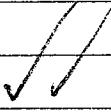
Q3

i)  $-3x + 15 \leq 3$

$$-x + 5 \leftarrow$$

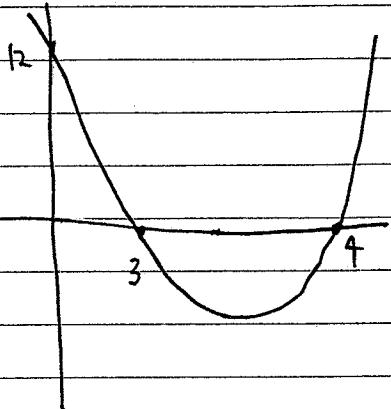
$$-x + 5 \leq 1$$

$$4 \leq x$$



ii)  $(x-4)(x-3) < 0$

9  
10



2  
2  $3 < x < 4$

iii) Either  $5+2x < 3x-1$

$$6 < x$$



72

or  $-(5+2x) < 3x-1$

$$-5-2x < 3x-1$$

$$-4 < 5x$$

$$\frac{-4}{5} < x$$

check solns \*



2  
3

~~1/2~~ ~~3/2~~ ~~2/2~~

Q3

$$\text{iv) } \frac{3x-2-(x+4)}{x+9} < 0$$

$$\frac{3x-2-x-4}{x+9} < 0$$

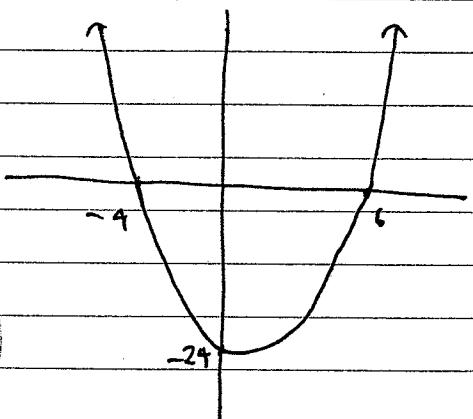
$$\frac{2x-6}{x+9} < 0$$

$$(2x-6)(x+4) < 0$$

$$2(x-3)(x+4) < 0$$

$$(x-3)$$

(CAB) oops.



$$-4 < x < 6 / 3$$

Q4

a) Domain:  $x-1 > 0$   
 $x > 1$  ✓

10  
10

(2)  
Range:  $f(x) \neq 0$   
 $f(x) > 0$  ✓

b) If ~~odd~~, even,  $f(x) = f(-x)$

Fab!

?  $\frac{x^3}{x^2-1} = \frac{(-x)^3}{(-x)^2-1}$

$\frac{x^3}{x^2-1} = \frac{-x^3}{x^2-1}$  ✗ False

So  $f(x)$  is not even

If odd,  $f(-x) = -f(x)$

$f(-x) = -\frac{x^3}{x^2-1}$

$-f(x) = -1 \times \frac{x^3}{x^2-1}$

$= \frac{-x^3}{x^2-1}$

you only need  
to look at

(2)  
 $-f(x) = f(-x) = \frac{-x^3}{x^2-1}$

$f(a)$

$f(-a)$  to see ...

∴  $f(x)$  is odd

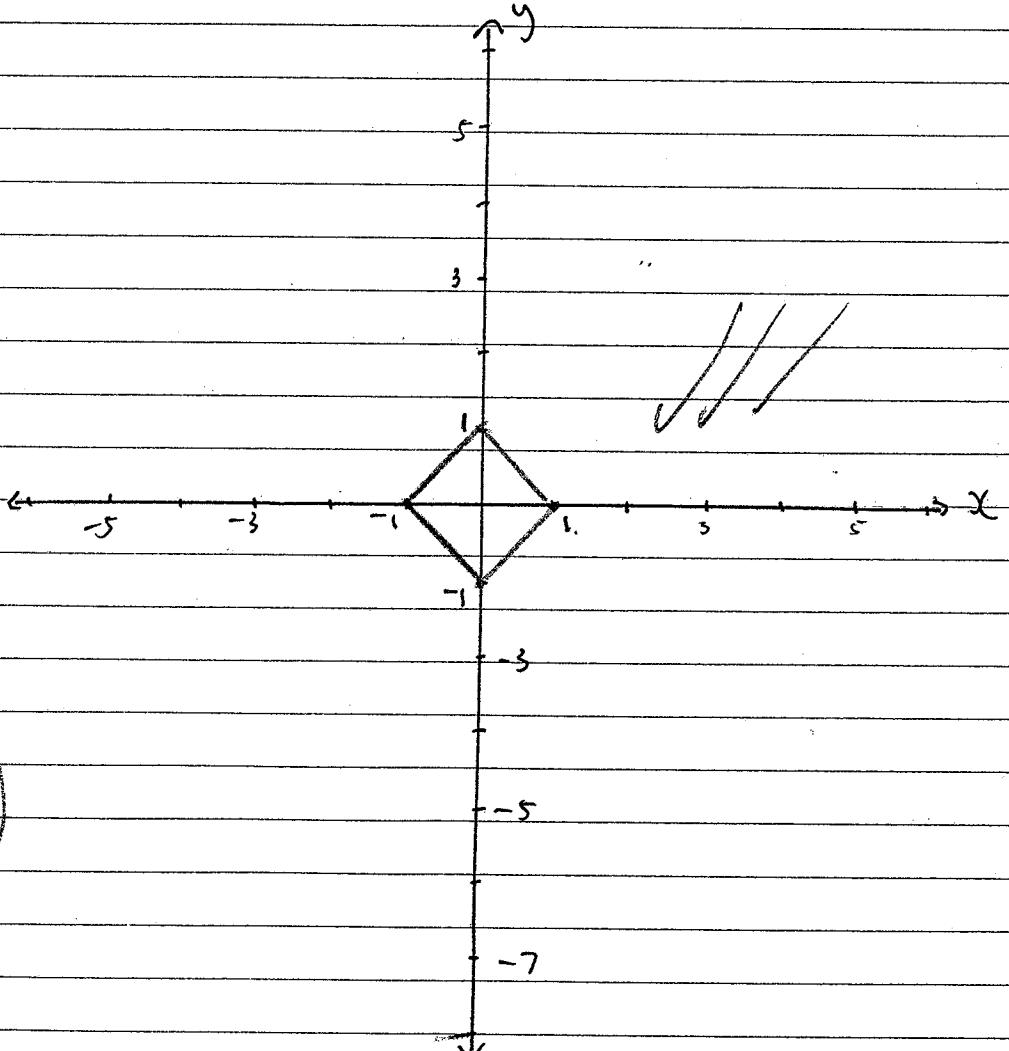
Q 4

c) If  $x \geq 0, y \geq 0$   
 $x+y=1 \rightarrow y=1-x$

If  $x < 0, y \geq 0$   
 $-x+y=1, y=1+x$

If  $x \geq 0, y < 0$   
 $x-y=1, x-1=y$

If  $x < 0, y < 0$   
 $-x-y=1$   
 $x+y=-1$   
 $y = -x-1$



Q 4

d)  $\sqrt{x} + \sqrt{3x+1} = 3$

$$\sqrt{3x+1} = 3 - \sqrt{x}$$

$$3x+1 = 9 - 6\sqrt{x} + x$$

$$2x < 8 - 6\sqrt{x}$$

$$2x - 8 + 6\sqrt{x} = 0$$

let  $\sqrt{x} = u$

$$2u^2 + 6u - 8 = 0$$

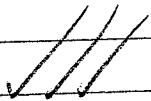
$$2(u^2 + 3u - 4) = 0$$

$$2(u+4)(u-1) = 0$$

$$u = -4 \text{ or } 1$$

$$\sqrt{x} = \cancel{-4} \text{ or } 1$$

$$x = 1$$



(3)  
3

stic

1.