

Further Practice: Algebraic Skills and Techniques

Remember: all questions match the numbered examples on pages 223–232.

- 1 If $x = 2$, evaluate $3x - 5$.
- 2 If $a = 3$, $b = 2$ and $c = 6$, find the value of $5ab - 4c$.
- 3 If $m = 4$, evaluate $m^2 - m$.
- 4 If $p = 10$, $3p^2 = ?$
- 5 If $t = -3$, find the value of $10 - t$.
- 6 If $a = -2$, find the value of $6a^2$.
- 7 Find the value of $x^3 - 4x^2 + 8x - 5$ if $x = -1$.
- 8 Evaluate $\sqrt{x^2 + y^2}$ if $x = 9$ and $y = 40$.
- 9 Evaluate $\frac{b^2 + c^2 - a^2}{2bc}$ when $a = 700$,
 $b = 800$ and $c = 500$.
- 10 Find the value, correct to two decimal places,
of $4\pi r^2$ when $r = 9$.
- 11 If $r = \sqrt{\frac{A}{\pi}}$ find the value of r , to one decimal place,
if $A = 415.5$
- 12 If $r = 0.05$, $n = 6$ and $M = 2000$, find the value of N to
two decimal places if $N = M \left\{ \frac{(1+r)^n - 1}{r(1+r)^n} \right\}$.
- 13 Find $9k + 3k - 7k$
- 14 Simplify $5a + 4b - 3c$, if possible.
- 15 Simplify $7a + 3a + 4b$
- 16 Simplify $8p - 3q - 6p + 5q$
- 17 Simplify $x^2 + 6x - 5 + 3x - 4x^2 - 2$
- 18 Simplify $-5a + 4b + 3a - 7b$
- 19 Simplify $7pq + 3p - 4q - 6qp - 3q + 1$
- 20 Simplify $7 \times a \times b$
- 21 Find $4p \times 5q$
- 22 Find $2a \times 3b \times 5c \times 6d$
- 23 Simplify $4x \times 3x$
- 24 Simplify $3p \times 5p \times 2q$
- 25 Simplify $x^4 \times x^6$
- 26 Find $a^3b^2 \times ab^5$
- 27 Simplify $m^3 \times n^4$
- 28 Find $2a^5 \times 4a^4$
- 29 Simplify $7x^3y^2 \times 5xy^3$
- 30 Simplify $6a^2b^3c^2 \times 3abc \times 2a^3b^2c^2$
- 31 Find $6x \div 2$
- 32 Find $7m \div m$
- 33 Find $15xyz \div 5y$
- 34 Simplify $\frac{9ab}{3b}$
- 35 Simplify $\frac{15pq}{3r}$

36 Simplify $\frac{18x^2}{12x}$

37 Find $p^6 \div p^2$

38 Simplify $a^5b^6 \div a^2b^3$

39 Find $x^8 \div a^2$

40 Find $36x^{36} \div 9x^9$

41 Find $12a^7b^5c^2 \div 3a^6bc^2$

42 Simplify $\frac{24a^7b}{8a^6b^2}$

43 Expand $3(x + 5)$

44 Expand $4(2a - 3b)$

45 Expand $a(a + 6)$

46 Expand $5t(4t + 3u - 1)$

47 Expand $-7(2a + 5b)$

48 Expand $-(p - q)$

49 Simplify $7x^2 + 4x \times 2x$

50 Simplify $10n^{10} \div 2n^2 - 4n \times 3n^7$

51 Expand and simplify $2(8h + 7) + 3(5h - 9)$

52 Expand and simplify $5(2x + 3) - 2(4x + 9)$

53 Expand and simplify $x(x - 8) - 4(x - 1)$

54 Solve $7k + 4 = 25$

55 Solve the equation $6x + 7 = 23 - 2x$

56 Solve $\frac{8a - 5}{3} = 2a + 1$

57 Solve $5x^2 = 1805$ ($x > 0$)

58 Solve $\sqrt{7x + 2} = 3$

59 Change the subject of the equation $v = u + at$ to a .

60 Change the subject of the equation $S = V_0 - Dn$ to n .

61 Make h the subject of the formula $A = \frac{1}{2}bh$.

62 Change the subject of the formula $P = 2l + 2b$ to l .

63 Change the subject of the formula $C = \frac{5}{9}(F - 32)$ to F .

64 Change the subject of the equation $x = kt^2$ to t .

65 Change the subject of the formula $A = \pi r^2$ to r ($r > 0$).

66 Find the value of x if $y = mx + b$ and, when $y = 7$, $m = 2$ and $b = -1$.

67 If $C = \frac{k}{x^2}$ find the value of k for which $C = 50$ and $x = 3.4$

68 Evaluate x ($x > 0$), when $y = ax^2$ given $a = 5$ and $y = 320$.

69 Find the value of r , correct to one decimal place, if $V = \frac{1}{3}\pi r^2h$ and $V = 5750$ when $h = 19$ ($r > 0$).

70 a Change the subject of the formula $V = \frac{4}{3}\pi r^3$ to r .
b If $V = 1988$ find r .

71 a Change the subject of the formula $A = \pi(R^2 - r^2)$ to R ($R > 0$).
b Find R , correct to one decimal place, if $r = 13$ and $A = 356$.

72 Use the estimation and refinement technique to find the value of x for which $6^x = 10\,077\,696$.

73 Find the value of t , to the nearest whole number, for which $2.3^t = 116\,000$.

74 Find, to two decimal places, the value of x for which $3^x = 21$.

75 If $N = 12\,200$, $M = 800$ and $r = 0.04$, use the estimation and refinement technique and your calculator to find the value of n , to the nearest whole

number, for which
$$N = M \left[\frac{(1+r)^n - 1}{r(1+r)^n} \right].$$

76 Express 28 000 in scientific notation.

77 Express in scientific notation:

- a 600 000
- b 9 417
- c 7 290 000 000

78 Write 7×10^5 as a normal number.

79 Write as normal numbers:

- a 4×10^6
- b 3.5×10^4
- c 1.234×10^8

80 Express in scientific notation:

- a 0.0007
- b 0.0312
- c 0.000 45

81 Write as decimals:

- a 5×10^{-4}
- b 8.7×10^{-6}
- c 4.61×10^{-5}

82 Find the product of 4.6×10^4 and 3.1×10^{-6} .

83 Find $400\,000 \div 0.000\,05$, expressing the answer in scientific notation.

84 The population of Western Australia is 2×10^6 and its area is 2.5×10^6 square kilometres. Find the population density in people per square kilometre.

85 a The planet Mercury is 57.5 million kilometres from the sun. Express this distance in metres, in scientific notation.
b If the speed of light is 3×10^8 m/s, find the time for light from the sun to reach Mercury.

Go to p 292 for **Quick Answers**
or to pp 353–5 for **Worked Solutions**

Challenge: Algebraic Skills and Techniques

1 Simplify $3x^2 + 5x \times 2x - 8x^3 \div 4x$. *Hint 1*

2 If $a = 3$, $b = 4$ and $c = 6$, evaluate $\frac{7a + 4b - 3c}{a^2 + b^2}$. *Hint 2*

3 Simplify $3xy + 5x - 2y + 4yx$. *Hint 3*

4 Expand and simplify:
 $5x(x^2 + 3x - 2) - 2(3x^2 + 1)$. *Hint 4*

5 Solve $\frac{4x}{9} + \frac{x+1}{3} = 5$. *Hint 5*

6 Change the subject of the formula $V = \frac{2\pi r^3}{3}$ to r . *Hint 6*

7 Consider the formula $R = \frac{a^2 + b^2 - c^2}{2ab}$:

- Change the subject of the formula to c (given that $c > 0$).
- If $R = 0.5$, $a = 8$ and $b = 5$ find the value of c .
Hint 7

8 Use the estimation and refinement technique to find the value of x , to two decimal places, for which $10^x = 5370$. *Hint 8*

9 Find the value of $\frac{5.9 \times 10^6 + 1.5 \times 10^5}{4.4 \times 10^8 \times 2.5 \times 10^{-3}}$. *Hint 9*

10 Simplify $8x - 5a + 3a$. *Hint 10*

11 If $p = 3$ and $q = 5$, evaluate pq^2 . *Hint 11*

12 Simplify $\frac{2ab^2}{8a^3b^2}$. *Hint 12*

13 Arrange in ascending order:
 3.1×10^{-2} , 5.834×10^{-4} , 9×10^{-3} . *Hint 13*

14 If $y = 2x^2 + b$ and x is a positive number, find x when $y = 19$ and $b = 1$. *Hint 14*

15 Francesca tried to solve the equation $7x + 19 = 2x - 4$. Her solution appears below.

$$\begin{array}{ll} 7x + 19 = 2x - 4 & \text{line I} \\ 7x = 2x - 15 & \text{line II} \\ 5x = 15 & \text{line III} \\ x = 3 & \text{line III} \end{array}$$

- Is $x = 3$ the correct solution to the equation?
Hint 15
- Where did Francesca make a mistake? *Hint 16*

Go to p 292 for **Quick Answers**
or to pp 355–6 for **Worked Solutions**

Hint 1: Remember the correct order of operations.

Hint 2: Make sure you divide by the whole denominator.

Hint 3: Only add or subtract like terms. xy and yx are the same term.

Hint 4: All of the second bracket must be subtracted. Be careful with the signs.

Hint 5: Multiply every term by the common denominator. Take care when there is more than one term in part of a fraction.

Hint 6: First divide by $\frac{2\pi}{3}$.

Hint 7: Substitute into the rearranged formula from part a.

Hint 8: You should know that $10^3 = 1000$ and $10^4 = 10\,000$. Between what two whole numbers must x lie?

Hint 9: Divide the whole numerator by the whole denominator. Use brackets or the calculator's memory.

Hint 10: Remember that the sign in front of the term belongs to the term. Be careful with the signs.

Hint 11: Only q is squared.

Hint 12: The answer is a fraction.

Hint 13: Ascending order means from lowest to highest. Write each number as a decimal for easy comparison.

Hint 14: Substitute, then solve an equation.

Hint 15: Substitute $x = 3$ into the original equation to see if it satisfies it (makes it true).

Hint 16: Check each line of the solution. There may be more than one mistake.

Solutions

UNIT 5: ALGEBRAIC MODELLING

Ch 12: Algebraic Skills and Techniques

Further Practice p233

1 If $x = 2$,

$$3x - 5 = 3 \times 2 - 5 = 1$$

2 If $a = 3$, $b = 2$ and $c = 6$,

$$5ab - 4c = 5 \times 3 \times 2 - 4 \times 6 = 30 - 24 = 6$$

3 If $m = 4$,

$$m^2 - m = 4^2 - 4 = 12$$

4 If $p = 10$,

$$3p^2 = 3 \times 10^2 = 300$$

5 If $t = -3$,

$$10 - t = 10 - (-3) = 13$$

6 If $a = -2$,

$$6a^2 = 6 \times (-2)^2 = 6 \times 4 = 24$$

7 If $x = -1$,

$$x^3 - 4x^2 + 8x - 5 = (-1)^3 - 4 \times (-1)^2 + 8 \times -1 - 5 = -1 - 4 - 8 - 5 = -18$$

8 If $x = 9$ and $y = 40$,

$$\sqrt{x^2 + y^2} = \sqrt{9^2 + 40^2} = \sqrt{1681} = 41$$

9 If $a = 700$, $b = 800$ and $c = 500$,

$$\frac{b^2 + c^2 - a^2}{2bc} = \frac{800^2 + 500^2 - 700^2}{2 \times 800 \times 500} = \frac{400\,000}{800\,000} = 0.5$$

10 When $r = 9$,

$$4\pi r^2 = 4 \times \pi \times 9^2 = 1017.876\,02 \dots = 1017.88 \quad (2 \text{ d.p.})$$

11 If $A = 415.5$,

$$r = \sqrt{\frac{A}{\pi}} = \sqrt{\frac{415.5}{\pi}} = 11.500\,337\,29 \dots = 11.5 \quad (1 \text{ d.p.})$$

12 If $r = 0.05$, $n = 6$ and $M = 2000$,

$$N = M \left[\frac{(1+r)^n - 1}{r(1+r)^n} \right] = 2000 \times \left[\frac{(1+0.05)^6 - 1}{0.05(1+0.05)^6} \right] = 10\,151.384\,13 \dots = 10\,151.38 \quad (2 \text{ d.p.})$$

13 $9k + 3k - 7k = 5k$

14 $5a + 4b - 3c = 5a + 4b - 3c$

15 $7a + 3a + 4b = 10a + 4b$

16 $8p - 3q - 6p + 5q = 2p + 2q$

17 $x^2 + 6x - 5 + 3x - 4x^2 - 2 = -3x^2 + 9x - 7$

18 $-5a + 4b + 3a - 7b = -2a - 3b$

19 $7pq + 3p - 4q - 6qp - 3q + 1 = pq + 3p - 7q + 1$

20 $7 \times a \times b = 7ab$

21 $4p \times 5q = 20pq$

22 $2a \times 3b \times 5c \times 6d = 180abcd$

23 $4x \times 3x = 12x^2$

24 $3p \times 5p \times 2q = 30p^2q$

25 $x^4 \times x^6 = x^{10}$

26 $a^3b^2 \times ab^5 = a^4b^7$

27 $m^3 \times n^4 = m^3n^4$

28 $2a^5 \times 4a^4 = 8a^9$

29 $7x^3y^2 \times 5xy^3 = 35x^4y^5$

30 $6a^2b^3c^2 \times 3abc \times 2a^3b^2c^2 = 36a^6b^6c^5$

31 $6x \div 2 = 3x$

32 $7m \div m = 7$

33 $15xyz \div 5y = 3xz$

34 $\frac{9ab}{3b} = 3a$

35 $\frac{15pq}{3r} = \frac{5pq}{r}$

36 $\frac{18x^2}{12x} = \frac{3x}{2}$

37 $p^6 \div p^2 = p^4$

38 $a^5b^6 \div a^2b^3 = a^3b^3$

39 $x^8 \div a^2 = x^8 \div a^2 \quad \left[\text{or } \frac{x^8}{a^2} \right]$

$$40 \quad 36x^{36} \div 9x^9 = 4x^{27}$$

$$41 \quad 12a^7b^5c^2 \div 3a^6bc^2 = 4ab^4$$

$$42 \quad \frac{24a^7b}{8a^6b^2} = \frac{3a}{b}$$

$$43 \quad 3(x+5) = 3 \times x + 3 \times 5 \\ = 3x + 15$$

$$44 \quad 4(2a-3b) = 4 \times 2a - 4 \times 3b \\ = 8a - 12b$$

$$45 \quad a(a+6) = a \times a + a \times 6 \\ = a^2 + 6a$$

$$46 \quad 5t(4t+3u-1) = 20t^2 + 15tu - 5t$$

$$47 \quad -7(2a+5b) = -7 \times 2a - 7 \times 5b \\ = -14a - 35b$$

$$48 \quad -(p-q) = -p + q$$

$$49 \quad 7x^2 + 4x \times 2x = 7x^2 + 8x^2 \\ = 15x^2$$

$$50 \quad 10n^{10} \div 2n^2 - 4n \times 3n^7 = 5n^8 - 12n^8 \\ = -7n^8$$

$$51 \quad 2(8h+7) + 3(5h-9) \\ = 16h + 14 + 15h - 27 \\ = 31h - 13$$

$$52 \quad 5(2x+3) - 2(4x+9) \\ = 10x + 15 - 8x - 18 \\ = 2x - 3$$

$$53 \quad x(x-8) - 4(x-1) \\ = x^2 - 8x - 4x + 4 \\ = x^2 - 12x + 4$$

$$54 \quad 7k+4=25 \quad [\text{subtract } 4] \\ 7k=21 \quad [\text{divide by } 7] \\ k=3$$

$$55 \quad 6x+7=23-2x \quad [\text{add } 2x] \\ 8x+7=23 \quad [\text{subtract } 7] \\ 8x=16 \quad [\text{divide by } 8] \\ x=2$$

$$56 \quad \frac{8a-5}{3} = 2a+1 \quad [\text{multiply by } 3] \\ 8a-5=6a+3 \quad [\text{subtract } 6a] \\ 2a-5=3 \quad [\text{add } 5] \\ 2a=8 \quad [\text{divide by } 2] \\ a=4$$

$$57 \quad 5x^2 = 1805 \quad [\text{divide by } 5] \\ x^2 = 361 \quad [\text{take the square root}] \\ x = \sqrt{361} \quad (x > 0) \\ x = 19$$

$$58 \quad \sqrt{7x+2} = 3 \quad [\text{square both sides}] \\ 7x+2=9 \\ 7x=7 \\ x=1$$

$$59 \quad v = u + at \\ u + at = v \quad [\text{turn the equation around}] \\ at = v - u \quad [\text{subtract } u \text{ from both sides}] \\ a = \frac{v-u}{t} \quad [\text{divide both sides by } t]$$

$$60 \quad S = V_0 - Dn \\ S + Dn = V_0 \quad [\text{add } Dn \text{ to both sides}] \\ Dn = V_0 - S \quad [\text{subtract } S] \\ n = \frac{V_0 - S}{D} \quad [\text{divide by } D]$$

$$61 \quad A = \frac{1}{2}bh \\ 2A = bh \quad [\text{multiply by } 2] \\ \frac{2A}{b} = h \quad [\text{divide by } b] \\ h = \frac{2A}{b}$$

$$62 \quad P = 2l + 2b \\ 2l + 2b = P \\ 2l = P - 2b \quad [\text{subtracting } 2b] \\ l = \frac{P - 2b}{2} \quad [\text{dividing by } 2] \\ [\text{Or: } P = 2l + 2b \\ \frac{P}{2} = l + b \quad [\text{dividing by } 2] \\ l = \frac{P}{2} - b \quad [\text{subtracting } b]]$$

$$63 \quad C = \frac{5}{9}(F - 32) \\ \frac{9C}{5} = F - 32 \\ F = \frac{9C}{5} + 32$$

$$64 \quad x = kt^2 \\ kt^2 = x \\ t^2 = \frac{x}{k} \\ t = \pm \sqrt{\frac{x}{k}}$$

$$65 \quad A = \pi r^2 \\ \pi r^2 = A \\ r^2 = \frac{A}{\pi} \\ r = \sqrt{\frac{A}{\pi}} \quad (r > 0)$$

$$66 \quad y = mx + b \\ m = 2, b = -1, y = 7 \\ 7 = 2x + (-1) \\ 2x - 1 = 7 \\ 2x = 8 \\ x = 4$$

$$67 \quad C = \frac{k}{x^2} \\ C = 50, x = 3.4 \\ 50 = \frac{k}{3.4^2} \\ k = 50 \times 3.4^2 \\ = 578$$

$$68 \quad y = ax^2 \\ y = 320, a = 5 \\ 320 = 5x^2 \\ x^2 = 64 \\ x = \sqrt{64} \quad (x > 0) \\ x = 8$$

$$69 \quad V = \frac{1}{3}\pi r^2 h \\ V = 5750, h = 19 \\ 5750 = \frac{1}{3}\pi r^2 \times 19 \\ 5750 = \frac{19\pi}{3} r^2 \\ r^2 = 5750 \div \left(\frac{19\pi}{3}\right) \\ = 288.9918704 \dots \\ r = \sqrt{288.9918704 \dots} \quad (r > 0) \\ = 16.999\ 760\ 89 \dots \\ = 17.0 \quad (1 \text{ d.p.})$$

$$70 \text{ a } V = \frac{4}{3}\pi r^3 \\ 3V = 4\pi r^3 \\ r^3 = \frac{3V}{4\pi} \\ r = \sqrt[3]{\frac{3V}{4\pi}}$$

$$\text{b } V = 1988, \\ r = \sqrt[3]{\frac{3V}{4\pi}} \\ = \sqrt[3]{\frac{3 \times 1988}{4\pi}} \\ = 7.800\ 263\ 197 \dots \\ = 7.8 \quad (1 \text{ d.p.})$$

$$71 \text{ a } A = \pi(R^2 - r^2) \\ \frac{A}{\pi} = R^2 - r^2 \\ R^2 = \frac{A}{\pi} + r^2 \\ R = \sqrt{\frac{A}{\pi} + r^2} \quad (R > 0)$$

$$\text{b } A = 356, r = 13 \\ R = \sqrt{\frac{A}{\pi} + r^2} \quad (R > 0) \\ = \sqrt{\frac{356}{\pi} + 13^2} \\ = 16.802\ 330\ 78 \dots \\ = 16.8 \quad (1 \text{ d.p.})$$

- 72** $6^x = 10\ 077\ 696$
 Guess $x = 7$,
 [Any value of x could be used.]
 $6^7 = 279\ 936$ [Too low]
 Guess $x = 10$,
 $6^{10} = 60\ 466\ 176$ [Too high]
 Guess $x = 9$,
 $6^9 = 10\ 077\ 696$ [Correct answer]
 The solution is $x = 9$.

- 73** $2.3^t = 116\ 000$
 Try $t = 12$,
 $2.3^{12} = 21\ 914.624\ 43 \dots$
 Try $t = 20$,
 $2.3^{20} = 17\ 161\ 558.31 \dots$
 Try $t = 15$,
 $2.3^{15} = 266\ 635.2355 \dots$
 Try $t = 14$,
 $2.3^{14} = 115\ 928.3632 \dots$
 \therefore the nearest whole number t
 for which $2.3^t \approx 116\ 000$ is $t = 14$.

- 74** $3^x = 21$
 $[3^2 = 9$ and $3^3 = 27$ so x is between
 2 and 3]
 Guess $x = 2.5$,
 $3^{2.5} = 15.588\ 457\ 27 \dots$
 Guess $x = 2.7$,
 $3^{2.7} = 19.419\ 023\ 52 \dots$
 Guess $x = 2.8$,
 $3^{2.8} = 21.674\ 022\ 17 \dots$
 Guess $x = 2.77$,
 $3^{2.77} = 20.97132523 \dots$
 Guess $x = 2.78$,
 $3^{2.78} = 21.202989 \dots$
 If $3^x = 21$, $x = 2.77$ to two decimal
 places.

75
$$N = M \left[\frac{(1+r)^n - 1}{r(1+r)^n} \right]$$

$$12\ 200 = 800 \left[\frac{(1.04)^n - 1}{0.04(1.04)^n} \right]$$

 $n = 24$ (by calculator to the
 nearest whole number)

76 $28\ 000 = 2.8 \times 10^4$ [$2.8 \times 10\ 000$]

- 77** a $600\ 000 = 6 \times 10^5$
 b $9417 = 9.417 \times 10^3$
 c $7\ 290\ 000\ 000 = 7.29 \times 10^9$

78 $7 \times 10^5 = 7 \times 100\ 000$
 $= 700\ 000$

- 79** a $4 \times 10^6 = 4 \times 1\ 000\ 000$
 $= 4\ 000\ 000$
 b $3.5 \times 10^4 = 35\ 000$
 c $1.234 \times 10^8 = 123\ 400\ 000$

- 80** a $0.0007 = 7 \times 10^{-4}$
 b $0.0312 = 3.12 \times 10^{-2}$
 c $0.000\ 45 = 4.5 \times 10^{-4}$

- 81** a $5 \times 10^{-4} = 0.0005$
 b $8.7 \times 10^{-6} = 0.000\ 0087$
 c $4.61 \times 10^{-5} = 0.000\ 0461$

82 $4.6 \times 10^4 \times 3.1 \times 10^{-6} = 0.1426$

83 $400\ 000 \div 0.000\ 05 = 8\ 000\ 000\ 000$
 $= 8 \times 10^9$

- 84** Population density
 $= (2 \times 10^6) \div (2.5 \times 10^6)$
 $= 0.8$
 There are 0.8 people/km².

85 a 57.5 million km
 $= 57\ 500\ 000$ km
 $= 5.75 \times 10^7$ km
 $= (5.75 \times 10^7) \times 1000$ m
 $= 5.75 \times 10^{10}$ m

- b Time = distance \div speed
 $= (5.75 \times 10^{10}) \div (3 \times 10^8)$
 $= 191.666\ 66 \dots$
 $= 192$ (nearest whole number)
 192 seconds = 3 minutes and
 12 seconds
 It takes approximately 3 minutes and
 12 seconds for light from the sun to
 reach Mercury.

Challenge p236

1 $3x^2 + 5x + 2x - 8x^3 \div 4x$
 $= 3x^2 + 10x^2 - 2x^2$
 $= 11x^2$

2 $a = 3, b = 4, c = 6$

$$\frac{7a + 4b - 3c}{a^2 + b^2} = \frac{7 \times 3 + 4 \times 4 - 3 \times 6}{3^2 + 4^2}$$

 $= \frac{19}{25}$
 $= 0.76$

3 $3xy + 5x - 2y + 4yx = 7xy + 5x - 2y$

4 $5x(x^2 + 3x - 2) - 2(3x^2 + 1)$
 $= 5x^3 + 15x^2 - 10x - 6x^2 - 2$
 $= 5x^3 + 9x^2 - 10x - 2$

5
$$\frac{4x}{9} + \frac{x+1}{3} = 5$$

 $9 \times \frac{4x}{9} + 9 \times \left(\frac{x+1}{3} \right) = 9 \times 5$
 $4x + 3(x+1) = 45$
 $4x + 3x + 3 = 45$
 $7x + 3 = 45$
 $7x = 42$
 $x = 6$

6
$$V = \frac{2\pi r^3}{3}$$

 $3V = 2\pi r^3$
 $\frac{3V}{2\pi} = r^3$
 $r = \sqrt[3]{\frac{3V}{2\pi}}$

7 a
$$R = \frac{a^2 + b^2 - c^2}{2ab}$$

 $2abR = a^2 + b^2 - c^2$
 $c^2 = a^2 + b^2 - 2abR$
 $c = \sqrt{a^2 + b^2 - 2abR}$ ($c > 0$)

b $R = 0.5, a = 8, b = 5$

$$c = \sqrt{a^2 + b^2 - 2abR}$$

 $= \sqrt{8^2 + 5^2 - 2 \times 8 \times 5 \times 0.5}$
 $= \sqrt{49}$
 $= 7$

- 8** $10^x = 5370$
 Try $x = 3.5$,
 $10^{3.5} = 3162.277\ 66 \dots$
 Try $x = 3.7$,
 $10^{3.7} = 5011.872\ 336 \dots$
 Try $x = 3.75$,
 $10^{3.75} = 5623.413\ 252 \dots$
 Try $x = 3.73$,
 $10^{3.73} = 5370.3179\ 64 \dots$
 $\therefore x = 3.73$ to two decimal places.

9
$$\frac{5.9 \times 10^6 + 1.5 \times 10^5}{4.4 \times 10^8 \times 2.5 \times 10^{-3}} = \frac{6.05 \times 10^6}{1.1 \times 10^6}$$

 $= 5.5$

10 $8x - 5a + 3a = 8x - 2a$

11 $p = 3, q = 5$
 $pq^2 = 3 \times 5^2$
 $= 3 \times 25$
 $= 75$

12 $\frac{2ab^2}{8a^3b^2} = \frac{1}{4a^2}$

13 $5.834 \times 10^{-4}, 9 \times 10^{-3}, 3.1 \times 10^{-2}$
 $[0.000\ 5834, 0.009\ 0000, 0.031\ 0000]$

14 $y = 2x^2 + b$
 When $y = 19$ and $b = 1$
 $19 = 2x^2 + 1$
 $18 = 2x^2$
 $9 = x^2$
 $x = 3$ ($x > 0$)

$$\begin{array}{l} 15 \quad 7x + 19 = 2x - 4 \\ \quad \quad 7x = 2x - 15 \quad \text{Line I} \\ \quad \quad 5x = 15 \quad \quad \text{Line II} \\ \quad \quad x = 3 \quad \quad \text{Line III} \end{array}$$

a When $x = 3$,

$$\begin{aligned} 7x + 19 &= 7 \times 3 + 19 \\ &= 40 \end{aligned}$$

$$\begin{aligned} 2x - 4 &= 2 \times 3 - 4 \\ &= 2 \end{aligned}$$

$x = 3$ is not the correct solution.

b There is a mistake in line I.

Subtracting 19 from both sides leaves

$$7x = 2x - 23.$$

There is a mistake in line II.

Subtracting $2x$ from both sides of line I leaves $5x = -23$.

The correct solution is:

$$7x + 19 = 2x - 4$$

$$7x = 2x - 23$$

$$5x = -23$$

$$x = -4.6$$