1. (i) On the same set of axes, sketch the graphs of y = x and  $y = -\frac{1}{x}$ .

- (ii) By addition of ordinates, sketch the graph of  $y = x \frac{1}{x}$ . (Sketch all graphs on the above set of axes).
- 2. Sketch the following by addition of ordinates:

(a) 
$$y = 2x + \frac{1}{x}$$

(b) 
$$y = \frac{3}{x} - 2x$$

(c) 
$$y = x^2 + \frac{1}{x}$$

(d) 
$$y = x^2 - \frac{1}{x}$$

3. (a) Prove that  $y = \sqrt{x+1} + \sqrt{1-x}$  is an even function.

(b) Find the domain of this function.

(c) Find the value of y when x = 0.

(d) Use the information gleaned in parts (a), (b) and (c), and the method of addition of ordinates to sketch this function, stating also its range.

- 4. Sketch the following graphs of reciprocal functions, stating the domain and range:
- (a)  $y = \csc x$ ,  $0 \le x \le 360^{\circ}$

(b)  $y = \cot x$ ,  $0 \le x \le 360^{\circ}$ 

(c)  $y = \frac{2}{x^2 + 1}$ 

(d)  $y = \frac{2}{x^2 - 1}$ 

(e) 
$$y = \frac{1}{x^3 - x}$$

(f) 
$$y = \frac{1}{x^2}$$

(g) 
$$y = \frac{1}{(x-2)^2}$$

(h) 
$$y = \frac{1}{\sqrt{4 - x^2}}$$



5. Sketch the following rational functions:

(a) 
$$y = \frac{1}{x+1}$$

(b) 
$$y = \frac{x}{x+1}$$

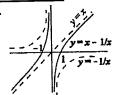
(c) 
$$y = \frac{2}{(x-3)(x+2)}$$

(d) 
$$y = \frac{1}{x^2 + x}$$

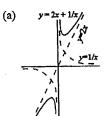
(e) 
$$y = \frac{x+1}{(x-1)(x+2)}$$

(f) 
$$y = \frac{x^2 - 4}{x^2 + 2x - 3}$$

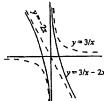
## **ANSWERS:**



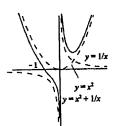
2.



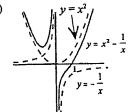
(b)



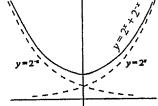
(c)



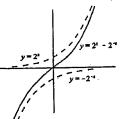
(d)



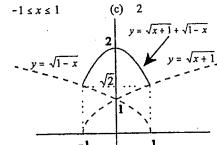
(e)



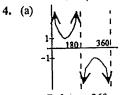
(f)



3. (b) (d)

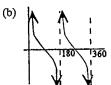


Range:  $\sqrt{2} \le y \le 2$ 

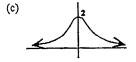


D:  $0 < x < 360, x \neq 180$ 

 $R: y \le -1, y \ge 1$ 



D:  $0 < x < 360, x \neq 180$ R: all real y

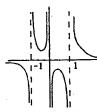


D: all real x

(d)

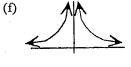
D:  $x \neq \pm 1$ R:  $y \le -2$ , y > 0

(e)

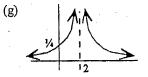


D:  $x \neq 0, \pm 1$ 

 $R: y \neq 0$ 

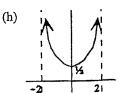


 $D: x \neq 0$ 



D:  $x \neq 2$ 

R: y > 0



D: -2 < x < 2

 $R: y \ge \frac{1}{2}$ 

