

# LEVEL 1 — ALGEBRA

Note: Only turn back to page number if you have difficulty

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- Q1.** (a) A car travels  $y$  km/h for  $x$  hours. How far does it travel?  
 (b) Two angles of a triangle are  $x^\circ$  and  $y^\circ$ . What is the size of the third angle?  
 (c) Three people have \$ $x$ , \$ $y$  and \$ $z$  respectively. What is their average wealth?

1

- Q2.** If  $p = 6$ ,  $q = 2$ ,  $r = 4$  and  $s = 3$ , find:

(a) $ps + qr$	(b) $pqrs$	(c) $\sqrt{2p+r}$
(d) $2(p+q) - r^2$	(e) $5r + 2q - 3s$	(f) $\frac{1}{2}pq + \frac{1}{3}rs$

2

- Q3.** Simplify:

(a) $5x + 3x^2 - 2x + 6x^2$	(b) $p^2 + 2p - 5 - 6p + 3p^2$
(c) $6xy - 5x + 4y - 3xy$	(d) $x^2 + 3y + 3xy - x^2 + 5xy$

3

- Q4.** Simplify:

(a) $5a \times b \times 3c$	(b) $6p \times 4q \times \frac{1}{2}p$	(c) $3xy \times -5x$
(d) $16mn \div 2n$	(e) $4x^2y \div 2x$	(f) $24abc \div 2ac$

4

- Q5.** Simplify:

(a) $\frac{m}{2} + \frac{m}{4}$	(b) $\frac{x}{3} - \frac{x}{4}$	(c) $\frac{2a}{5} + \frac{a}{2}$
(d) $\frac{a}{x} + \frac{b}{x}$	(e) $\frac{3x}{2} - \frac{2y}{3}$	(f) $\frac{m}{3} - \frac{2m}{7}$

5

- Q6.** Simplify:

(a) $\frac{x}{2} \times \frac{x}{4}$	(b) $\frac{5}{a} \times \frac{b}{10}$	(c) $\frac{4}{m} \times \frac{3}{2n}$
(d) $\frac{a}{3} \div \frac{a}{4}$	(e) $\frac{2x}{3} \div \frac{x}{6}$	(f) $\frac{4}{m} \div \frac{3n}{m}$

6, 7

- Q7.** Expand the following:

(a) $5(x + 2)$	(b) $3(2a - 1)$	(c) $2y(y + 3)$
(d) $4(3 - x)$	(e) $-2(m + n)$	(f) $b(2 - 3b)$

8, 9

- Q8.** Expand these binomial products:

(a) $(x + 2)(x + 1)$	(b) $(x - 1)(x - 3)$	(c) $(m + 3)(m - 4)$
(d) $(a + 3)(b - 2)$	(e) $(m - 9)(n + 2)$	(f) $(b - 2)(a + 2)$

10, 11

## LEVEL 2 — ALGEBRA

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**Q1.** Write the simplest algebraic expressions for each of the following:

1

- (a) The perimeter of a square with side  $x$  cm.
- (b) The perimeter of a rectangle with sides  $x + 3$  and  $x + 4$ .
- (c) The area of a square with side  $x - 1$ .
- (d) The area of a rectangle with sides  $x + 6$  and  $x - 3$ .

**Q2.** If  $x = 3$ ,  $y = -4$  and  $z = 6$ , find:

2

- (a)  $z^2 - (x^2 + y^2)$
- (b)  $(x + y)^2 + (y + z)^2$
- (c)  $2xy(x - y + z)$
- (d)  $\frac{xy}{z}$
- (e)  $\frac{x}{2} + \frac{yz}{3}$
- (f)  $\sqrt[3]{\frac{xy^2}{z}}$

**Q3.** Simplify:

3, 4

- (a)  $-2xy + 5y \times 3x + 6x - y$
- (b)  $-3mn \div 2m + 4n - m$
- (c)  $2a + 15a^2b \div 3ab - 2ab$
- (d)  $8x^2 \times (-3xy^2) \div (-6xy)$

**Q4.** Simplify:

5 – 7

- (a)  $\frac{4y}{3x} + \frac{3y}{4x} - \frac{y}{x}$
- (b)  $\frac{4n}{5m} + \frac{3n}{2m} - \frac{2n}{m}$
- (c)  $\left( \frac{3}{8y} + \frac{5}{6x} \right) \div \frac{5}{12xy}$
- (d)  $\frac{2a}{5b} \times \frac{3a}{5b} \div \frac{5a}{4b}$

**Q5.** Expand and simplify:

8, 9

- (a)  $3x(2x + 5) + 4x$
- (b)  $-x(2 - x) + x$
- (c)  $\frac{1}{2}(4x - 3) - 5x$
- (d)  $-\frac{3}{4}(3x + 2) - 2$
- (e)  $2x\left(\frac{2x + 1}{3}\right)$
- (f)  $-(6x - 5) - (2x - 3)$

**Q6.** Expand and simplify:

10, 11

- (a)  $(2x + 3)(x - 4)$
- (b)  $(3x - 2)(2x + 3)$
- (c)  $(4x - 5)(2x - 3)$
- (d)  $(4 - x)(3x + 2)$
- (e)  $2(2x + 1)(x - 2)$
- (f)  $\frac{1}{2}(2x + 6)(x - 4)$

**Q7.** Expand and simplify:

12, 13

- (a)  $(x + 4)^2$
- (b)  $(x - 1)(x + 1)$
- (c)  $(m + n)(n - m)$
- (d)  $(4x + 3)(4x - 3)$
- (e)  $(2x - 1)^2$
- (f)  $(3x + 2)^2$
- (g)  $(x^2 + 4)^2$
- (h)  $5x(6x + 1)^2$
- (i)  $\frac{1}{2}x(2x - 4)^2$

## LEVEL 3 — ALGEBRA

- Q1. (a) If  $x$  apples cost a total of \$ $y$ , what is the cost of  $z$  apples?  
 (b) The price of bricks increases from \$ $x$ /tonne to \$ $y$ /tonne. Before the price rise, the cost of bricks for an average house was \$ $H$ . What is the new cost of bricks for an average house?  
 (c) \$ $A$  is divided in the ratio  $x : y$ . What is the difference, in dollars, between the two amounts if  $x > y$ ?

Q2. If  $x = \frac{1}{2}$ ,  $y = \frac{2}{3}$  and  $z = \frac{3}{4}$ , evaluate:

(a)  $\frac{x}{y} + z$

(b)  $\sqrt{\frac{xy}{z}}$

(c)  $\frac{x^2}{z} \cdot \frac{2}{y}$

Q3. Simplify:

(a)  $x + \frac{1}{x}$

(b)  $\frac{5x}{7} - x$

(c)  $\frac{4}{x^2} + \frac{2}{x}$

(d)  $\left(\frac{1}{x} + \frac{1}{y}\right) \div (x + y)$

Q4. Expand and simplify:

(a)  $x(x + y) + y(x - y)$

(b)  $x(x + 1)(x + 2)$

(c)  $(2x - 3)^2 - (x - 3)^2$

(d)  $\frac{1}{2}(x + 3) + \frac{1}{3}(x + 2)$

(e)  $(2x - 3y)(2x + 3y)$

(f)  $-(2x - 1)^2$

Q5. Simplify:

(a)  $(3x + 2)(3x - 2) + (x - 1)^2 - (x + 1)^2$

(b)  $(5x - 3)^2 - (x + 3)^2 + (2x - 1)(2x + 1)$

(c)  $5x^2 - 4x(3x - 2) - (4x - 1)^2 + (2x + 1)^2$

(d)  $(x + 1)^2 - (x + 2)^2 + (x - 3)^2 + (x + 4)^2 - x^2$

Q6. Simplify:

(a)  $\frac{(x - 3)^2}{(x + 3)^2} - \frac{(x + 2)^2}{(x + 3)^2}$

(b)  $\frac{3(x - 1)}{x + 1} + \frac{2(x + 1)}{x - 1}$

## Level 1 — Algebra

- Q1. (a)  $xy \text{ km}$  (b)  $(180 - x - y)^\circ$  (c)  $\frac{\$(x + y + z)}{3}$   
 Q2. (a) 26 (b) 144 (c) 4 (d) 0 (e) 15 (f) 10  
 Q3. (a)  $3x + 9x^2$  (b)  $4p^2 - 4p - 5$  (c)  $3xy - 5x + 4y$  (d)  $3y + 8xy$   
 Q4. (a)  $15abc$  (b)  $12p^2q$  (c)  $-15x^2y$  (d)  $8m$  (e)  $2xy$  (f)  $12b$   
 Q5. (a)  $\frac{3m}{4}$  (b)  $\frac{x}{12}$  (c)  $\frac{9a}{10}$  (d)  $\frac{a+b}{x}$  (e)  $\frac{9x-4y}{6}$  (f)  $\frac{m}{21}$   
 Q6. (a)  $\frac{x^2}{8}$  (b)  $\frac{b}{2a}$  (c)  $\frac{6}{mn}$  (d)  $1\frac{1}{3}$  (e) 4 (f)  $\frac{4}{3n}$   
 Q7. (a)  $5x + 10$  (b)  $6a - 3$  (c)  $2y^2 + 6y$  (d)  $12 - 4x$  (e)  $-2m - 2n$  (f)  $2b - 3b^2$   
 Q8. (a)  $x^2 + 3x + 2$  (b)  $x^2 - 4x + 3$  (c)  $m^2 - m - 12$   
 (d)  $ab - 2a + 3b - 6$  (e)  $mn + 2m - 9n - 18$  (f)  $ab + 2b - 2a - 4$

## Level 2 — Algebra

- Q1. (a)  $4x \text{ cm}$  (b)  $(4x + 14) \text{ units}$  (c)  $(x^2 - 2x + 1) \text{ units}^2$  (d)  $(x^2 + 3x - 18) \text{ units}^2$   
 Q2. (a) 11 (b) 5 (c) -312 (d) -2 (e)  $-6\frac{1}{2}$  (f) 2  
 Q3. (a)  $13xy + 6x - y$  (b)  $\frac{5n}{2} - m$  (c)  $7a - 2ab$  (d)  $4x^2y$   
 Q4. (a)  $\frac{13y}{12x}$  (b)  $\frac{3n}{10m}$  (c)  $\frac{9x+20y}{10}$  (d)  $\frac{24a}{125b}$   
 Q5. (a)  $6x^2 + 19x$  (b)  $x^2 - x$  (c)  $-3x - \frac{3}{2}$  (d)  $-\frac{9x}{4} - \frac{7}{2}$  (e)  $\frac{4x^2}{3} + \frac{2x}{3}$  (f)  $8 - 8x$   
 Q6. (a)  $2x^2 - 5x - 12$  (b)  $6x^2 + 5x - 6$  (c)  $8x^2 - 22x + 15$   
 (d)  $-3x^2 + 10x + 8$  (e)  $4x^2 - 6x - 4$  (f)  $x^2 + 7x + 12$   
 Q7. (a)  $x^2 + 8x + 16$  (b)  $x^2 - 1$  (c)  $n^2 - m^2$   
 (d)  $16x^2 - 9$  (e)  $4x^2 - 4x + 1$  (f)  $9x^2 + 12x + 4$   
 (g)  $x^4 + 8x^2 + 16$  (h)  $180x^3 + 60x^2 + 5x$  (i)  $2x^3 - 8x^2 + 8x$

## Level 3 — Algebra

- Q1. (a)  $\$(\frac{zy}{x})$  (b)  $\$(\frac{Hy}{x})$  (c)  $\frac{A(x-y)}{x+y}$   
 Q2. (a)  $1\frac{1}{2}$  (b)  $\frac{2}{3}$  (c) 1  
 Q3. (a)  $\frac{x^2 + 1}{x}$  (b)  $-\frac{2x}{7}$  (c)  $\frac{4+2x}{x^2}$  (d)  $\frac{1}{xy}$   
 Q4. (a)  $x^2 + 2xy - y^2$  (b)  $x^3 + 3x^2 + 2x$  (c)  $3x^2 - 6x$  (d)  $\frac{5x+13}{6}$   
 (e)  $4x^2 - 9y^2$  (f)  $-4x^2 + 4x - 1$   
 Q5. (a)  $9x^2 - 4x - 4$  (b)  $28x^2 - 36x - 1$  (c)  $-19x^2 + 20x$  (d)  $x^2 + 22$   
 Q6. (a)  $\frac{5-10x}{(x+3)^2}$  (b)  $\frac{5x^2-2x+5}{x^2-1}$