Name:	Class:
	·

St George Girls High School

Year 9

Yearly Examination

2005



Mathematics

Time Allowed: 75 minutes

Instructions

- Set out work clearly
- Show all working where necessary
- Calculators may be used
- Diagrams are not to scale
- Section A answers only
- Section B show all necessary working

Section A	/15
Section B	
Question 1	/12
Question 2	/12
Question 3	/12
Question 4	/12
Question 5	
Question 6	/ 8
Total	183

Section A

(15 marks)

Write your answers to each question in the ANSWER column. You may do your working in the QUESTION column.

	Question	Answer
1.	Simplify $3a^2 \times -2a^3 + a^4$	•
/2/	Express $2\frac{3}{4}\%$ as a simplified fraction.	,
3.	Evaluate $\left(\frac{9}{16}\right)^{\frac{-1}{2}}$ without the use of a calculator.	•
4,	Give a simplified expression for the area of this trapezium.	
5.	What is the solution to this equation? $\frac{y-1}{5} = -3$	
6.	What is the value of y ?	

	Question	Answer
7.	What is the angle sum of a decagon? (ie. a 10-sided polygon)	
8.	What is the value of $\tan \theta$?	
9.,	What is the equation of the line passing through $(0, 2)$, and parallel to $y = -3x - 1$?	
10.	A dress has a marked price of \$125. It is offered for sale during a "15% off" discount sale. What is the new selling price?	
11.	Give the abbreviation for the congruence test used to prove these triangles congruent.	?
12.	Stephanie's normal hourly rate is \$10.50. How much does she earn, working 5½ hours overtime, at time and a half? (round off to nearest cent)	

Question		Answer
13. Give an inequality, describing number line:	g this section of the	
-1 0 1 2 3	4	
14. What is the perimeter of this answer in terms of π)	shape? (giving your	
15. Expand and simplify: $(2w-3y)$)2	

Section B

Show all necessary working (unless stated otherwise)

<u>Question 1</u> – Algebra and Rational Numbers – (12 marks)

Marks

- a) If $F(x) = 3 2x^2$, find:
 - (i) F(-5)

(ii) F(3p)

1 1

b). Expand and simplify: -3x(2x-5)-(x-2)(5x+4)

2

- c) Factorise fully:
 - (i) $28p^2q 14p^2q^3 + 7pq^2$
- (ii) $9y(2-y)-(2-y)^2$

1

Marl

1

d) Convert 110km/h into m/s

e) Round 0.0002053 off to 2 significant figures (write your answer in scientific notation).

f) Simplify $9 \times 10^{-7} \times 6 \times 10^4 \times 2 \times 10^{-3}$ (again, writing your answer in scientific notation)

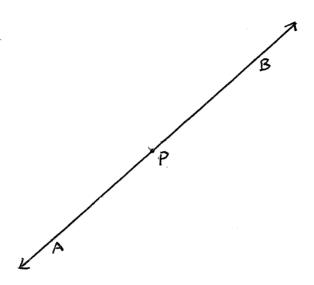
g) If a leaking pipe spills water at the rate of 12.6L/min, how much water is lost in 24 hours?

Question 2 – Measurement and Geometry – (12 marks)

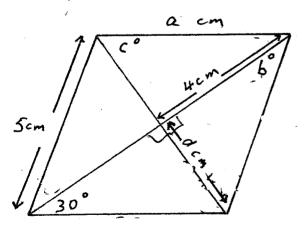
Mark

a) Construct a perpendicular to line AB from the point P. Leave all construction lines.

2



b) This figure is a rhombus. Find the values of the pronumerals.



$$a =$$

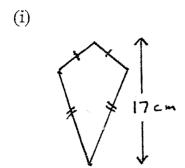
$$c \doteq$$

$$d =$$

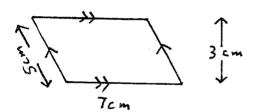
Marks

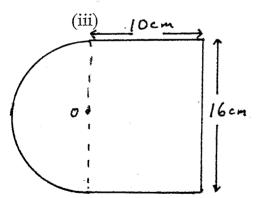
2

c) Find the areas of these figures:

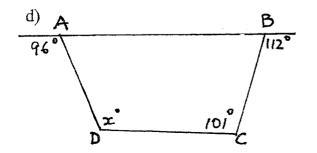


(ii)





(give answer to (iii) to 2 decimal places)



Find the value of x (giving full reasons):

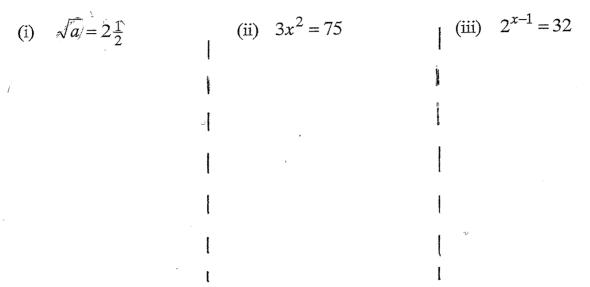
2

2

<u>Question 3</u> – Equations and Consumer Arithmetic – (12 marks)

Mark

a) Solve these equations:



b) If
$$s = ut + \frac{1}{2}at^2$$
, find u given that $s = 10$, $t = 2$, and $a = -5$

c) A filing cabinet depreciates at a rate of 10% p.a. It is originally worth \$250. How much is it worth after 3 years?

2

Mark

- d) Suzy earns \$146 000 p.a. (gross). She has allowable tax deductions of \$73, 500. She has paid \$23 700 in tax instalments throughout the financial year. Find:
 - (i) her taxable income.

(ii) her tax payable, using the tax table shown below:

Taxable income	Tax on this income	
0–6000	Nil	
6001–20 000	17¢ for each \$1 over \$6000	
20 001–50 000	\$2380 plus 30¢ for each \$1 over \$20000	
50 001–60 000	\$11 380 plus 42¢ for each \$1 over \$50 000	
60 000-	\$15 580 plus 47¢ for each \$1 over \$60 000	

∴ Tax payable =

(iii) How much refund does she receive from the tax office? (Ignore the Medicare levy)

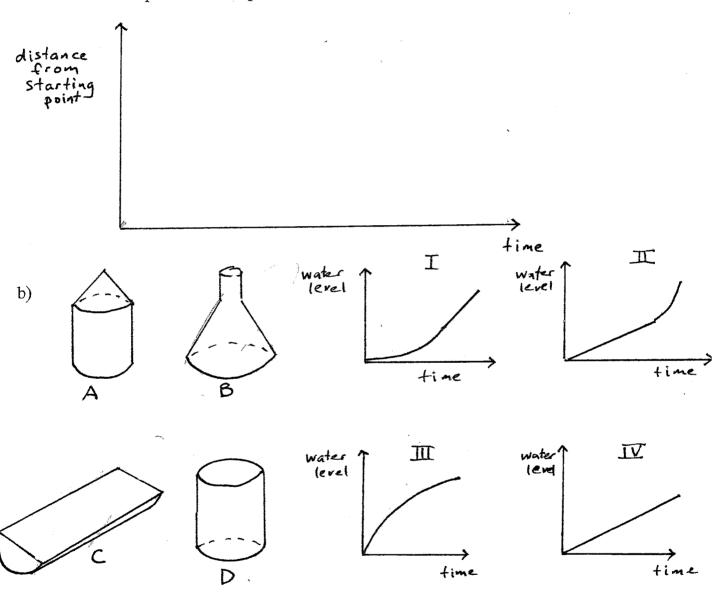
Question 4 – Graphs and Coordinate Geometry – (12 marks)

Mark

a) A girl walks up a hill at a constant rate. She rests for a few minutes, then runs back down the hill at a different constant rate to her starting point. Draw in a graph which could correspond to this trip.

2

2 :

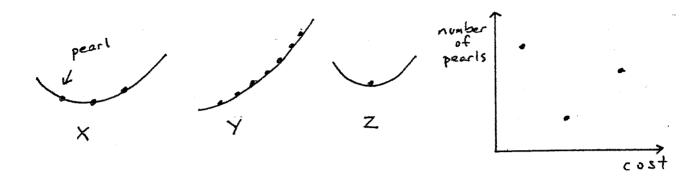


Each of the four containers pictured is filled with water at a steady rate. When the level of water in each container was plotted, the graphs I to IV were obtained. Match each container to its graph.

A B . C ____ D ___

Mark

c) By using the scatter diagram on the right, determine which necklace costs the most.



X, Y, Z are three different pearl necklaces.

A <		
Answer	2.5	

1

d) What is the equation of the x-axis?

1

e) (i) By completing this table of values, graph the line x-2y=3 on the number plane provided.

	7 6	1	1 2
\boldsymbol{x}	U		<u> </u>
v	-		

2

(ii) What is the gradient of this line?

Mark

3

- f) Given the two points A(-2, 3) and B(1, -4) find:
 - (i) the distance AB (exact value).

(ii) the gradient of the interval AB.

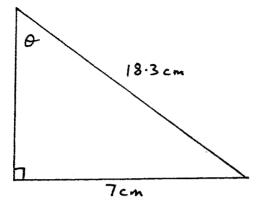
(iii) the mid-point of the interval AB.

<u>Question 5</u> – Trigonometry and Congruence – (12 marks)

Marl

a)

b)



Find the size of the angle marked θ (to nearest degree)

A lady flies her plane 180km from Sydney airport at a bearing of 153° from true north.

(i) Draw a diagram representing this.

1

(ii) How far east of Sydney is she?

2

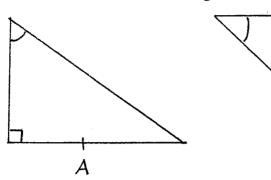
c) Write the direction NNW in terms of true bearings.

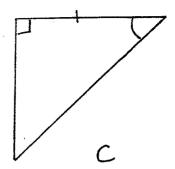
Mark

2

d) Pick out which of these triangles are congruent, and give the congruence test used.

B

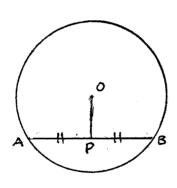




Answer: _____,

Test: ____

e)



A line is drawn from the centre, O, of a circle, so that it bisects a chord AB. By drawing in two construction lines, and proving two triangles congruent, prove that OP is perpendicular to AB.

Give full reasons at each step.

Question 6 – Spreadsheets – (8 marks)

1. In the spreadsheet below what name is given to the cell with ** in it?

	A	В
1		
2		-
3		**
4		

2. Consider the spreadsheet below.

	A	В	C	D
1	6	8	14	48
2	7	6		42
3	8	7		56 ·
4	9	3		27

a) The number in cell C1 is the sum of the numbers in cells A1 and B1. Write two different formulae which could appear in cell C1 to achieve this.

or

- b) Cell C1 was then highlighted and the cursor was dragged down to cell C4 and the command FILL DOWN was used. Write the number which would then appear in cell C4.
- c) Carefully study columns A, B and D. Write the formula which would appear in cell D3.

3. Consider the spreadsheet below.

	A	В
1	2	
2	4	
3	9	

Column B is to list the squares of the number in Column A. Write a formula which could appear in cell B3.

4. Consider the spreadsheet below.

	A	В	C
1	6		
2	7		
3	8		
4		1	9.3
5		2	

a) The formula =\$A\$1*B4 was entered in cell C4. Write the number which would then appear in cell C4.

b) If cell C4 was then highlighted, the cursor dragged down to cell C5 and the command FILL DOWN used, write the number which would appear in cell C5.

Class: Ms alusan

St George Girls High School

Year 9

Yearly Examination

2005



100%.

Mathematics

Time Allowed: 75 minutes

Instructions

- Set out work clearly
- Show all working where necessary
- Calculators may be used
- Diagrams are not to scale
- Section A answers only
- Section B show all necessary working

Section A	15 /15
Section B	
Question 1	12 /12
Question 2	13/12
Question 3	12 /12
Question 4	12/12
Question 5	12 /12
Question 6	% / 8
Total	84 183

100%

Section A

(15 marks) Write your answers to each question in the ANSWER column. You may do your working in the QUESTION column.

Question	Answer
1. Simplify $(3a^2 \times -2a^3) + a^4$ $-6a^5 + a^4$	-6a5+a4
Express $2\frac{3}{4}\%$ as a simplified fraction. $\frac{1}{4} + 100 = \frac{4}{4} \times \frac{1}{100}$	400
3. Evaluate $\left(\frac{9}{16}\right)^{\frac{-1}{2}}$ without the use of a calculator.	4 3
Give a simplified expression for the area of this trapezium. A= $\frac{1}{2}$ N (a+b) = $\frac{1}{2}$ N (a+b) = $\frac{1}{2}$ 2b (3a+b+7a-3b) = b (10 a -2b) = 10 M-2b ²	10ab -250 ²
5. What is the solution to this equation? $\frac{y-1}{5} = -3$ $y = -15$	y=-14 /
6. What is the value of y? $100^{\circ} - 39^{\circ}$ $100^{\circ} + 90^{\circ} + 5u^{\circ} = 360^{\circ}$	y=34°
100+90+5y=360 A=1/2h(a+b)	

	Question	Answer
	7. What is the angle sum of a decagon? (ie. a 10-sided polygon) (%%(W))	14400/
	8. What is the value of $\tan \theta$? 17 17 17	tan 4 - 8/5 odso as decimal (0.53)
6=y-r =2-	What is the equation of the line passing through $(0, 2)$, and parallel to $y = -3x - 1$? $(0, 2)$ by $(0, 2)$ by $(0, 2)$ $(0,$	y=-3x+2
=2	10. A dress has a marked price of \$125. It is offered for sale during a "15% off" discount sale. What is the new selling price?	\$106.25
	11. Give the abbreviation for the congruence test used to prove these triangles congruent.	5AS
	12. Stephanie's normal hourly rate is \$10.50. How much does she earn, working 5½ hours overtime, at time and a half? (round off to nearest cent)	\$86.63

Question	Answer
13. Give an inequality, describing this section of the number line:	
-101234	1 4x <u>4</u> 3
-16843	253 27-1 WRO19G
14. What is the perimeter of this shape? (giving your answer in terms of π) 2 TV $\times 120$ $+6$ $\times 120$ 360 2 TV $\times 120$ 360	(2T+6) cm
15. Expand and simplify: $(2w-3y)^2$ $4w^2-12wy+9y^2$	4w2-12wy79y2

Mar

Section B

Show all necessary working (unless stated otherwise)

Question 1 - Algebra and Rational Numbers - (12 marks)

Marks

a) If $F(x) = 3 - 2x^2$, find:

(i)
$$F(-5)$$

 $F(-5) = 3 - [2(-5)^{2}]$
 $= 3 - 2(25)$
 $= 3 - 50$
 $= -47$
 $= 3 - [(2 \times 25)]$
 $= 3 - 50 = -47$

(ii)
$$F(3p)$$

$$F(3p) = 3 - [2(3p)^{2}]$$

$$= 3 - [2(qp^{2})]$$

$$= 3 - [(2(3p)^{2})]$$

$$= 3 - [(2(3p)^{2})]$$

$$= 3 - [(2(3p)^{2})]$$

$$= 3 - [(2(3p)^{2})]$$

Expand and simplify: -3x(2x-5)-(x-2)(5x+4)-6x2 /15x - [5x2/4x-10x /8] 2+150c - (502+42-10x-8) 2+150c - (502+42-100c+8) 2+210c+8

Factorise fully:

Section B - continued

30 56 m/s 110 × 1000 +60 +60 m/s Convert 110km/h into m/s 30.555 ... = 30.56 m/s (c2dp)

Round 0.0002053 off to 2 significant figures (write your answer in scientific notation).

Simplify $9 \times 10^{-7} \times 6 \times 10^4 \times 2 \times 10^{-3}$

(again, writing your answer in scientific notation)

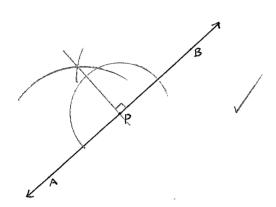
If a leaking pipe spills water at the rate of 12.6L/min, how much water is lost in 24 hours?

1. Mar 18 144 L'Utres is tost is 24 nour

Question 2 - Measurement and Geometry - (12 marks)

Marks

Construct a perpendicular to line AB from the point P. Leave all construction lines. 2



This figure is a rhombus. Find the values of the pronumerals.

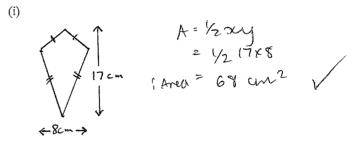
a cm

impossible

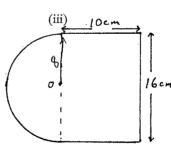
22× 53°7'48 = 106 15 136

Section B - continued

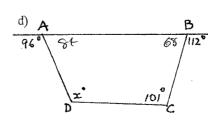
c) Find the areas of these figures:



(ii) 7cm



(give answer to (iii) to 2 decimal places)



Find the value of x (giving full reasons): 2c = 360 - (0 ÅB + ABC +101) (Lsuint quad is 86

DÂB= 180-96 (str L=1800) = 89-0 ABC = 140-112 (sar L=1800) = 680

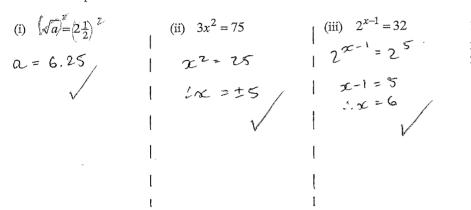
: x = 360 - (84+68+101) (all as stud

Mar

Question 3 – Equations and Consumer Arithmetic – (12 marks)

Marks

a) Solve these equations:



b) If $s = ut + \frac{1}{2}at^2$, find u given that s = 10, t = 2, and a = -5

$$10 = 2u + (\frac{1}{2} \times -5 \times 2^{2})$$

$$10 = 2u + (\frac{1}{2} \times -5 \times 4^{2})$$

$$10 = 2u + (\frac{1}{2} \times -5 \times 4^{2})$$

$$10 = 2u + -10$$

$$10 = 2u + -10$$

$$20 = 2u$$

$$10 = 2u + -10$$

c) A filing cabinet depreciates at a rate of 10% p.a. It is originally worth \$250. How much is if worth after 3 years?

$$A = P(1-R)^{n}$$

$$= 250 (1-0.1)^{3}$$

$$= 250 \times 183h 0.729$$

$$= $8i $182.25$$



1 After 3 years the cabinet is worth \$18225

Section B – continued Mar

f) Suzy earns \$146 000 p.a. (gross). She has allowable tax deductions of \$73, 500. She has paid \$23 700 in tax instalments throughout the financial year. Find:

(i) her taxable income.

(ii) her tax payable, using the tax table shown below:

Taxable income	Tax on this income	
0-6000	Nil	
6001-20 000	17¢ for each \$1 over \$6000	
20 001-50 000	\$2380 plus 30¢ for each \$1 over \$20 000	
50 001–60 000	\$11 380 plus 42¢ for each \$1 over \$50 000	
60 000-	\$15 580 plus 47¢ for each \$1 over \$60 000	

∴ Tax payable = \$21 4-55

(iii) How much refund does she receive from the tax office? (Ignore the Medicare levy)



I she will receive \$ 2 245 as a refund from the

M

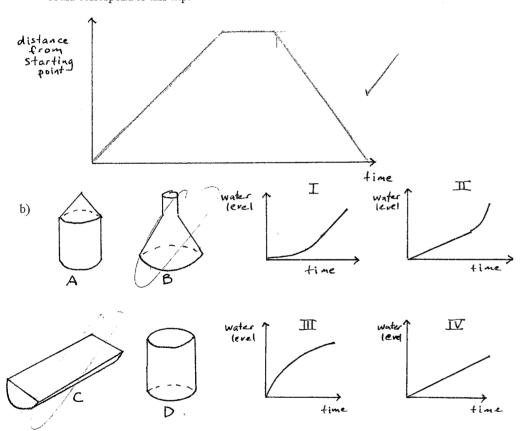
Section B - continued

Question 4 - Graphs and Coordinate Geometry - (12 marks)

Marks

a) A girl walks up a hill at a constant rate. She rests for a few minutes, then runs back down the hill(at a different constant rate) to her starting point. Draw in a graph which could correspond to this trip.

2



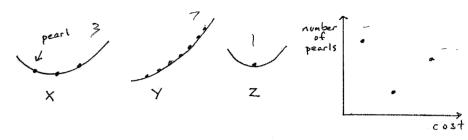
Each of the four containers pictured is filled with water at a steady rate. When the level of water in each container was plotted, the graphs I to IV were obtained. Match each container to its graph.



D = W

Section B - continued

By using the scatter diagram on the right, determine which necklace costs the most.



X, Y, Z are three different pearl necklaces.

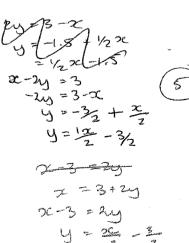
Answer Y cost W. Wort

What is the equation of the x-axis?

By completing this table of values, graph the line x-2y=3 on the number plane provided. - none provided

х	0	1	2	
у	-1-5	-1	-0.5	
		179		
		3.1		
			ine my	
	4+5 1-5	77.70	rice > ×	
	ن مان الله الم	N James Marie	۱- د د	$\sqrt{}$
	95.2			
	JK -9	- 4		
		186		

(ii) What is the gradient of this line?



a 25 HA W

Marks

Given the two points A(-2) 3) and B(1) -4) find: (-2) - (

3

the distance AB (exact value).

$$d = \sqrt{(-2-1)^2 + (3-(-4))^2}$$

$$= \sqrt{(-3)^2 + (7)^2}$$

$$= \sqrt{q+4q}$$

(1) - (-2)

$$= \sqrt{\frac{q+4q}{58}}$$

the gradient of the interval AB.

gradient =
$$\frac{32-9}{2-2}$$
,
$$= \frac{-4-3}{1-2}$$

$$= \frac{-7}{3}$$

(iii) the mid-point of the interval AB.

miapaint =
$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

= $\left(\frac{-2 + 1}{2}, \frac{3 - 4}{2}\right)$
= $\left(\frac{-1}{2}, \frac{-1}{2}\right)$ (3)

Section B - continued

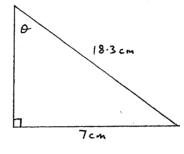
St George Girls High School

Ouestion 5 – Trigonometry and Congruence – (12 marks)

Marl

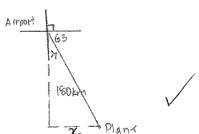
2

a)



Find the size of the angle marked θ (to nearest degree)

- A lady flies her plane 180km from Sydney airport at a bearing of 153° from true north.
 - Draw a diagram representing this.



How far east of Sydney is she?

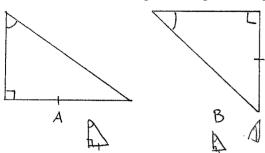
L. She is \$1-72 km 'East' of Sydney. Write the direction NNW in terms of true bearings.

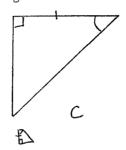
- E NAWA 337°30' T WAR

Marks

2

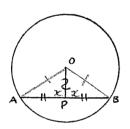
Pick out which of these triangles are congruent, and give the congruence test used.





Answer: A A

e)



A line is drawn from the centre, O, of a circle, so that it bisects a chord AB. By drawing in two construction lines, and proving two triangles congruent, prove that OP is perpendicular to AB.

Give full reasons at each step.

SIS AOP and BOP

1. AO=BO (unal radii of aids)

2. AP=BP (given it. programme PO bisets AB)

3. OP (common)

1. A ADP=ABOP (SSS)

: APO = BPO (comes L's, cong D'S)

Let APO be oc LBPO DO

(2x=180° (str L is 180°) / (x=90° :.0P is perpensional to AB)

St George Girls High School Year 9 Mathematics Yearly Examination - 2005

Section B - continued

Ouestion 6 - Spreadsheets - (8 marks)

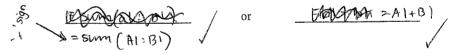
1. In the spreadsheet below what name is given to the cell with ** in it?

	A	В
1		
2		
3		**
4		

Consider the spreadsheet below.

	A	В	C	D
1	6	8	14	48
2	7	6		42
3	8	7		56 =
4	9	3		27

The number in cell C1 is the sum of the numbers in cells A1 and B1. Write two different formulae which could appear in cell C1 to achieve this.



Cell C1 was then highlighted and the cursor was dragged down to cell C4 and the command FILL DOWN was used. Write the number which would then appear in cell C4. 12

Carefully study columns A, B and D. Write the formula which would appear in cell D3. = A3* B3

3. Consider the spreadsheet below.

	A	В
_ 1	2	
2	4	
3	9	

Column B is to list the squares of the number in Column A. Write a formula which could appear in cell B3. $= A3^2 2 \qquad \text{ov} = A3^3 A3$

4. Consider the spreadsheet below.

	A	B	C
1	6		
_ 2	7		
3	8		
4		1	:
5		2	

- a) The formula =\$A\$1*B4 was entered in cell C4. Write the number which would then appear in cell C4.
- b) If cell C4 was then highlighted, the cursor dragged down to cell C5 and the command FILL DOWN used, write the number which would appear in cell C5.

