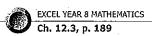
CHAPTER 9

Statistics and probability



Frequency distribution table

QUESTION 1 Draw up a frequency distribution table for each set of data below.

b	5	4	2	4	7.	6	4	4
	3	5	7	8	7	4	3	4
	/.	7.	Ω	7				

Score (x)	Tally	Frequency (f)	
	-		
	. <u>.</u> .		

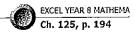
Score (x)	Tally	Frequency (f)		
	•			
-				
	•			

QUESTION 2 Draw up a frequency distribution table for each set of data below.

b	3	4	6	7	2	0	5 2	4
	5	6	4	5	3	4	6	7
	4	5	4	3	1	0	2	6
	3							

Score (x)	Tally	Frequency (f)		
	-			
ļ				

Score (x)	Tally	Frequency (f)
	,	
-		



Frequency histogram and frequency polygon

QUESTION **1** For the set of scores given:

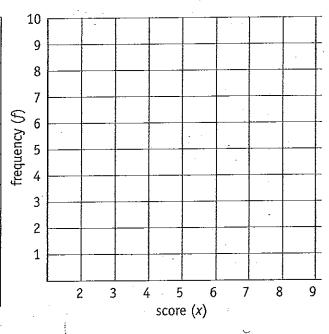
- a complete the frequency distribution table
- b draw a frequency histogram

c draw a frequency polygon

 3
 8
 6
 3
 2
 5
 5
 8
 5
 3
 7
 4
 5
 7
 8
 2
 5
 8
 6
 4

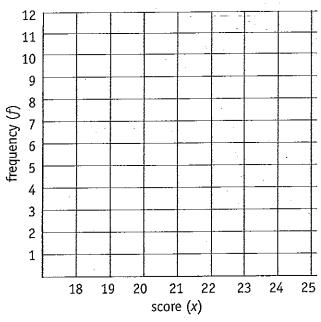
 9
 7
 7
 6
 7
 8
 9
 7
 7
 6
 7
 7
 6

Score (x)	Tally	Frequency (f)
;		
-	•	
	•	



QUESTION 2 From the following distribution table, draw a frequency histogram and frequency polygon.

Score	18	19	20	21	22	23	24	25
Frequency	3	5	4	8	12	9	6	3



EXCEL YEAR 8 MATHEMATICS Ch. 12.6, 12.7, p. 195, 196

Mean

QUESTION 1 Find the mean of the following set of scores.

a 7, 8, 9

b 8, 9, 10, 14

c 10, 11, 12, 13

- d 15, 17, 19, 23
- e 3, 5, 8, 10

f 9, 10, 13, 14, 16, 22

QUESTION 2 Find the mean of the following set of scores.

- 3, 3, 5, 5, 5, 5, 7, 7, 7, 7 b 8, 8, 9, 9, 9, 8, 8, 8, 8 c 3, 3, 6, 6, 6, 7, 7, 7, 7
- d 3, 3, 3, 3, 4, 4, 5, 5, 6 e 4, 5, 6, 7, 6, 5, 4, 3 f 8, 7, 9, 6, 5, 6, 8, 7

QUESTION 3 Find the mean of the following set of scores.

3, 3, 3, 6, 6, 8, 8, 8, 8

b 2, 2, 4, 4, 4, 5, 6, 8

c 6, 6, 6, 8, 8, 8, 8, 8, 9, 9, 9, 9

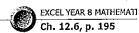
d 5, 5, 5, 6, 6, 6, 7, 7, 7, 7, 8, 8, 8

Complete each table and calculate the mean. QUESTION 4

X	f	fx
2	1	·
3	2 ,	,
4	2	
5	3	
6	2	
7	2	

f	fx
2	
2	
2	
1	
3	
3	
	2 2 2 1 3

х	f	fx
4	3	
5	1	
6	2	
- 7	1	
8	1 .	
9	1	



Mode

QUESTION 1 What is the mode of the following sets of scores?

a · 2, 2, 3, 8, 9, 3, 2, 5, 2, 3 ·

b 6, 7, 5, 6, 8, 6, 3, 4, 6, 5, 6

c 2, 3, 4, 3, 3, 2, 2, 3, 3, 3, 1

d 5, 3, 4, 3, 5, 5, 6, 5, 7, 5

e 6, 7, 8, 9, 9, 9, 10, 5, 9, 6

f 2, 5, 3, 5, 3, 5, 2, 1, 5, 5, 6

g 2, 3, 5, 2, 1, 2, 3, 2

h 5, 2, 4, 4, 4, 5, 4, 4, 6, 3

QUESTION **2** Find the mode from each set of scores.

a 6, 5, 7, 5, 8, 6, 5, 7, 5

b 6, 5, 6, 7, 4, 3, 6, 6, 2, 6

c 5, 6, 4, 7, 7, 5, 7, 7, 5, 4, 7, 7, 8

d 5, 6, 8, 6, 5, 6, 5, 6, 6, 6, 7, 6, 6

e 16, 15, 16, 19, 16, 17, 16, 16

f 7, 8, 7, 6, 7, 5, 7, 7, 5, 7, 7

g 42, 37, 38, 42, 43, 42, 42, 44, 42

h 6, 1, 2, 6, 4, 6, 4, 6, 3, 2, 6, 6, 1, 6

QUESTION 3 Select the mode from each set of scores.

a 5, 6, 6, 5, 7, 5, 8, 5, 5, 7

b 3, 4, 5, 5, 3, 3, 3, 4, 3, 7

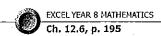
c 2, 3, 4, 3, 2, 1, 3, 3, 4, 3

- d 4, 3, 6, 6, 3, 6, 5, 6, 7, 6, 6
- e 2, 3, 4, 4, 5, 4, 5, 4, 6, 5, 4, 4, 4, 3, 4
- f 7, 8, 9, 7, 10, 7, 8, 7, 9, 7, 9, 7, 5, 7

QUESTION **4** Find the mode for each set of scores.

a 7, 8, 7, 7, 9, 7, 8, 7, 7, 7

- **b** 6, 7, 8, 7, 6, 5, 6, 6, 7, 6
- c 9, 8, 11, 11, 8, 11, 10, 11, 12, 11, 11
- d 5, 6, 7, 7, 8, 7, 8, 7, 9, 8, 7, 7, 7, 6, 7
- e 10, 11, 12, 10, 13, 10, 11, 10, 11, 10, 12, 10, 8, 10 f 8, 9, 8, 8, 10, 8, 9, 8, 8, 8



Median

QUESTION 1 Find the median of the following sets of scores.

a 8, 9, 10, 12, 10

b 11, 14, 18, 13, 11

c 5, 8, 9, 8, 9, 10, 9

d 12, 16, 18, 14, 13

e 6, 4, 7, 5, 8

f 21, 23, 20, 18, 18

QUESTION 2 What is the median of each set of scores?

a 4, 5, 6, 8, 6

b 13, 16, 20, 15, 13, 14, 13

c 3, 6, 7, 6, 7, 8, 7

d 9, 13, 15, 11, 10

e 8, 6, 9, 7, 10

f 16, 18, 15, 13, 13

QUESTION **3** Find the median of the following sets of scores.

a 8, 9, 10, 11, 12

b 42, 52, 32, 22, 52, 72, 62

c 13, 15, 8, 12, 9, 14, 10, 11, 15

d 7, 10, 5, 2, 1, 2, 7, 6, 4, 3, 10

e 9, 1, 6, 3, 2, 5, 7, 8, 4, 7, 9

f 2, 7,1, 5, 8, 5, 3, 6, 7, 8, 8

QUESTION 4 Find the median of the following sets of scores.

a 30, 33, 25, 26, 29, 30, 33

b 8, 7, 6, 8, 5, 13, 9, 9, 3

c 5, 8, 13, 10, 9, 10, 13, 8, 5, 4, 5

d 5, 11, 4, 8, 11, 8, 6, 9, 10, 11, 11

e 5, 9, 11, 7, 6, 7, 6, 5, 9

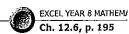
f 14, 10, 16, 13, 11, 12, 11

g 3, 6, 4, 9, 22, 3, 6

h 8, 12, 15, 13, 12

i 5, 7, 9, 10, 11, 2

j 7, 6, 5, 7, 4, 12, 10, 10, 4



Range

QUESTION **1** Find the range of the following sets of scores.

a 8, 2, 1, 4, 5, 7, 0

b 3, 8, 11, 5, 9, 1, 3, 8, 15

c 5, 3, 4, 2, 8, 13

d 14, 11, 7, 6, 13, 11, 12

e 6, 8, 8, 5, 10, 12, 14

f 7, 4, 5, 12, 17, 4, 3

g 10, 7, 12, 22, 1, 23

h 19, 21, 27, 19, 17, 3

QUESTION **2** Find the range of each set of scores.

a 3, 5, 2, 1, 7, 20, 3, 6

b 0, 1, 2, 3, 5, 8, 18, 1, 0, 9

c 6, 11, 9, 14, 69, 10, 11, 12

d 6, 13, 17, 31, 12, 39

è 7, 10, 5, 3, 14, 13, 18, 21

f 10, 12, 14, 17, 18, 24, 9

g 8, 10, 22, 38, 65, 1

h 5, 10, 15, 20, 30, 35, 40

QUESTION **3** Find the range of the following sets of scores.

a 6, 8, 9, 3, 5, 1, 17

b 1, 5, 0, 3, 8, 12, 31, 54

c 1, 7, 8, 3, 16, 7, 8, 33

d 4, 5, 3, 1, 9, 15, 28, 34

e 52, 39, 52, 16, 16, 50

f 6, 20, 28, 27, 34, 32, 34

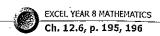
QUESTION **4** Find the range of each set of scores.

a 9, 14, 12, 34, 28

b 5, 9, 10, 3, 15, 29, 61

c 2, 5, 1, 8, 36, 72, 18

- d 10, 12, 14, 17, 24, 9, 15, 16, 18
- e 15, 3, 8, 5, 7, 3, 2, 25, 39
 - f 6, 4, 11, 20, 11, 67, 34



Miscellaneous questions

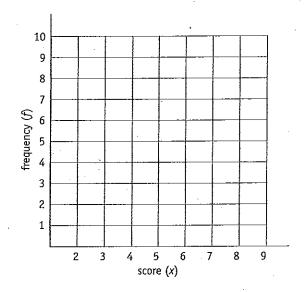
QUESTION 1 The following survey involves the test results obtained by a class of 30 students.

4 8 6 4 5 6 6 5 6 7 5 5 7 8 9 5 6 7 5 4 3 2 5 6 8 7 8 6 8

- a Draw a frequency distribution table.
- c Draw a frequency polygon.
- e Find the mode.
- **g** Find the range.

Score (x)	Tally	Frequency (f)
		1
	· 	
		,

- b Draw a frequency histogram.
- d Calculate the mean.
- f Find the median.

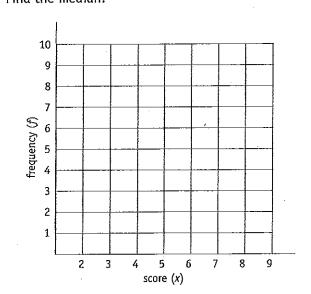


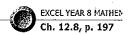
QUESTION 2 Twenty-five families were surveyed as to how many children were in the family. The following data was obtained.

- a Draw a frequency distribution table.
- c Draw a frequency polygon.
- e Find the mode.
- g Find the range.

Score (x)	Tally	Frequency (f)
		-

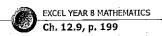
- **b** Draw a frequency histogram.
- d Calculate the mean.
- f Find the median.





Basic probability

Q	UESTION 1	A die is thrown once.	Fin	d the probability of showing:		
a .	a three		b	a prime number	C	an even number
d	a seven		е	any number from 1 to 6	f	a two or six
	·	·	:	. <u> </u>		<u>. Partie v</u>
Qı	JESTION 2	From the letters of the probability that the le		ord PROBABILITY, one letter is is:	select	ed at random. What is the
3	P?		b	A or B?	. c	a vowel?
Qı	JESTION 3	A card is drawn at ran	dom	ı from a pack of 52 playing caı	ds. Fin	d the probability that the
a	a club		b	a black card	C	a jack
d	a red card		e	not a spade	f	a king or queen
	JESTION 4	A bag contains 8 gree probability that it is:		2 yellow and 5 white balls. If		
1	green	·	b	yellow	· . · C.;	white :
ł	not green		е	not white	f	pink
					•	
Qυ	ESTION 5	A 3-digit number is to number is:	be	formed from the digits 5, 4 an	d 6. WI	hat is the probability that
	greater than	600?		b even?		
					5?	
Qυ	ESTION 6	The numbers from 1 to the probability that th		are written on separate cards. Imber is:	One ca	ard is chosen at random. F
l.	even			b odd		· · · · · · · · · · · · · · · · · · ·
				The second secon		
	•					
		but greater than 8				
	tess than 12	but greater than o		j a muttiple of	·	



Probability and tree diagrams

QUESTIC	What is the probability that the number will:
a sta	t with the digit 1?
b be	even?
c be	greater than 700?
Questio	Three coins are tossed together. What is the probability of throwing
a thre	ee heads?
b two	heads and a tail?
c thre	ee tails?
d two	tails and a head?
e atl	east two tails?
QUESTIC	A coin is drawn at random. What is the probability that it is:
	vo dollar coin?
	ne dollar coin?
	venty cent coin?
d ā g	old-coloured coin?
	Three cards with the names Michael, Michelle and Melony are put in One card is draw at random from the box. What is the probability that the name is: helle?
	oy's name?
	irl's name?
i, ay	its name.
QUESTIC	A die is thrown once. What is the probability of throwing:
a afi	ve?
b an	odd number?
c a n	umber less than 7?
d a ze	ero?



•	^	•
Α	A letter is chosen at random from the word MAT	THEMATICS. Find the probability that it will be:
a	a aTorM	
b	b a vowel	
C		
d		
Á	A die is thrown once. Find the probability that i	it is a number:
a	a greater than 3	
b	b a number greater than 6	
c	•	
	The numbers 1 to 7 are written on separate card that the number is:	ds. One card is chosen at random. What is the prob
a	a odd?	
b		
С		
	*	
d	d divisible by 3?	the state of the s
_		
d		
d e A	a prime number? A bag contains 6 red, 5 yellow and 4 white balls	s. If a ball is drawn at random, find the probability
d e A is:	a prime number? A bag contains 6 red, 5 yellow and 4 white balls s:	s. If a ball is drawn at random, find the probability
d e A is:	a prime number? A bag contains 6 red, 5 yellow and 4 white balls s: a red	s. If a ball is drawn at random, find the probability
d e A is: a b	e a prime number? A bag contains 6 red, 5 yellow and 4 white balls s: a red white	s. If a ball is drawn at random, find the probability
d e A is: a	a prime number? A bag contains 6 red, 5 yellow and 4 white balls s: red white blue	s. If a ball is drawn at random, find the probability
d e	A bag contains 6 red, 5 yellow and 4 white balls s: a red b white blue yellow yellow	s. If a ball is drawn at random, find the probability

PART A TOPIC TEST

- **Instructions** This part consists of 15 multiple choice questions
 - Fill in only ONE CIRCLE for each question
 - Each question is worth 1 mark
 - Calculators may be used

Time allowed: 15 min	nutes
----------------------	-------

Total marks = 15

From the set of scores 3, 1, 4, 6, 5, 5, 7, 3, 4, 5, 4, 5, 7, the mode is

- (A) 6
- **(B)** 4.538

1

Marks

Find the range of the scores 4, 3, 5, 1, 2, 8, 7, 10, 6, 9.

- (A) 7

1

What is the difference between the mean and the mode of the scores 20, 40, 50, 20, 60?

- (A) 2
- (B) 12
- \bigcirc 20

1

The mean of the scores 3, 5, 3, 3, 7, 3, 6, 5, 4, 3 equals

- (A) 4.1
- (\mathbf{B}) 4.2

1

The median of the scores 1, 2, 3, 5, 3, 2, 1, 6, 3, 1, 2, 8, 9 is

- (A) 1
- **(B)** 2
- (D) 5

A letter is chosen at random from the word AUSTRALIA. Find the probability that it is a vowel.

1

A bag contains 3 red, 4 blue and 5 yellow balls. Find the probability of choosing at random:

a red ball

1

either a blue or yellow ball

1

a ball that is not blue

1

10 a white ball

(A) 0

 \bigcirc $\frac{1}{4}$

 \mathbb{C} $\frac{1}{2}$

D 1

1

Marl

A card is chosen at random from a pack of 52 playing cards. Find the probability that the card is:

11 an ace

(A) $\frac{1}{13}$

(B) $\frac{7}{13}$

 $\bigcirc \frac{1}{26}$

1

12 a red king

(A) $\frac{1}{13}$

B $\frac{7}{13}$

 \bigcirc $\frac{1}{26}$

1

13 a diamond

(A) $\frac{1}{13}$

B $\frac{7}{13}$

 \bigcirc $\frac{1}{26}$

 $\bigoplus_{n \in \mathbb{N}} \frac{1}{4}$

1

14 black or a king

(A) $\frac{1}{13}$

(B) $\frac{7}{13}$

 \bigcirc $\frac{1}{26}$

① $\frac{1}{4}$

1

15 either a five, a six or a seven

 $\bigcirc \frac{1}{13}$

 $\mathbb{C}^{-\frac{3}{13}}$

① $\frac{4}{13}$

1

Total marks achieved for PART A

PART B TOPIC TEST

- **Instructions** This part consists of 15 questions
 - Each question is worth 1 mark
 - Write answers in the 'Answers only' column

	Time allowed: 15 minutes Questions						Anc	wers only	Marks
		Ų	uestions		•		Alls	Weis offing	Patrice
For	the scores 3, 5, 7 ,	3, 4, 3, 2, 3	3, 3, find:						
1	the mean							· .	_ 1
2	the mode		•	•				· 	_ 1
3	the median					5			_ 1
4	the range								_ 1
For	the set of scores g	iven, find:				, s			
5	the mode	Score	Frequency	7					_ 1
6	the median	1	3		٠			·	_ 1
7	the mean	2 3	5 9						_ 1
8	the range	4	8	j					1
A d	ie is thrown. Find t	he probabili	ty of throwin	ng:					
	a three	•			,				_ 1
10	a seven				•	į			_ 1
11	a number greater	than 2							1
12	a prime number	,							_ 1
13	an even number		,	•					1
	numbers from 1 to								
14	an odd number?								_ 1
15	a square number?								_ 1

Total marks achieved for PART B



TOPIC TEST

PART

Mar

5

5

5

- **Instructions** This part consists of 4 questions
 - Each question is worth 5 marks
 - Show all necessary working

T	ime	allov	ved:	20	minutes
---	-----	-------	------	----	---------

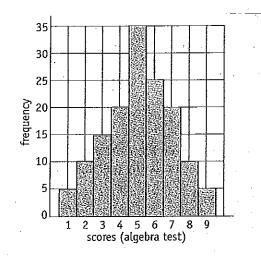
Total marks = 20

7	Fo	r the set of scores 8, 11, 3, 5, 2, 2, 12,	6:					
	a	find the mode	b	find the mean	·	1	· .	
	C	arrange the scores in ascending order						-

d find the median _____ e find the range _____

- **2** A die is rolled and the following results obtained; 6, 1, 2, 6, 6, 6, 3
 - a How many times was the die thrown? ______
 - b How many times was the result 6?

 - c What fraction of the throws are 6s? _____
 - d What fraction of the throws were odd numbers?
 - e What fraction of the throws were even numbers?
- A four-digit number is to be formed from the digits 2, 3, 6 and 7. What is the probability that the number will:
 - a start with a 7? ______ b be an odd number? _____
 - e be less than 3000?_____
- be an even number? _____ d be greater than 6000? _____
- a What is the mode of the distribution?
 - b How many students scored 6 marks?
 - c. How many students scored more than 8 marks?
 - How many students scored less than 4 marks?
 - What is the range of the distribution?



Total marks achieved for PART C

Answers

PAGE 103

1 8

		·
Score (x)	Tally	Frequency (f)
. 7	1	1
8	1	1
9	İll	3
10	1#1	6
11	1##	. 6
12	III	3
13	1111	4

	4
	_

Score (x)	Tally	Frequency (f)
2	l	1
3	11	2
4	## III	8
5	11	2
6	Ι΄ ΄	1
7 -		4
8	11	2

2 8

Score (x)	Tally	Frequency (f)
8	1111	4
10	₩.	5
12	13H III	8
14	##	5
16	III	3

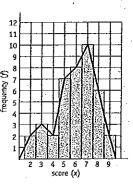
Ł

Score (x)	Tally	Frequency (f)
0	R	2
1	1	1
2]][3
3	OII	4
4	₩ I	6
5	111	3
6	1111	4
7	11	2

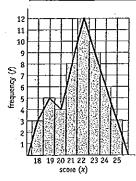
PAGE 104 1 a

_			
	Score (x)	Tally	Frequency (f)
ſ	2	11	2
	3	111	3
ſ	4	11	2
ſ	5	## II	7
	6	## III	8
	7	###	10
	8	₩I	6
	9	il	2

b



2



PAGE 105 1 a 8 b 10.25 c 11.5 d 18.5 e 6.5 f 14 2 a 5.4 b 8.3 c 5.7 d 3.9 e 5 f 7 3 a 5.8 b 4.375 c 7.83 d 6.54 4 a 2,6,8,15,12,14;4.75 b 2,4,6,4,15,18;3.77 c 12,5,12,7,8,9;5.8 PAGE 106 1 a 2 b 6 c 3 d 5 e 9 f 5 g 2 h 4 2 a 5 b 6 c 7 d 6 e 16 f 7 g 42 h 6 3 a 5

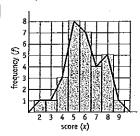
PAGE 106 1 a 2 b 6 c 3 d 5 e 9 f 5 g 2 h 4 2 a 5 b 6 c 7 d 6 e 16 f 7 g 42 h 6 3 a 5 b 3 c 3 d 6 e 4 f 7 4 a 7 b 6 c 11 d 7 e 10 f 8

PAGE 107 1 a 10 b 13 c 9 d 14 e 6 f 20 2 a 6 b 14 c 7 d 11 e 8 f 15 3 a 10 b 52 c 12 d 5 e 6 f 6 4 a 30 b 8 c 8 d 9 e 7 f 12 g 6 h 12 i 8 j 7

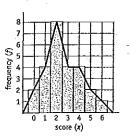
PAGE 108 1 a 8 b 14 c 11 d 8 e 9 f 14 g 22 h 24 2 a 19 b 18 c 63 d 33 e 18 f 15 g 64 h 35 3 a 16 b 54 c 32 d 33 e 36 f 28 4 a 25 b 58 c 71 d 15 e 37 f 63

PAGE 109 1 a, b, c see below d 5.86 e 5 f 6 g 7 2 a, b, c see below d 2.56 e 2 f 2 g 6

Score (x)	Tally	Frequency (f)
2	1	1
3	J	1
4	(1)	3
5	## III	8
6	7HL 11	- 7
7	1111	4
8	#	5
9	1.	1



Score (x)	Tally	Frequency (f)
0	11	2
1	1101	4
2	## III	8
3	TIII	4
4	IIII	4
5		2
6	1	1



PAGE 110 1 a $\frac{1}{6}$ b $\frac{1}{2}$ c $\frac{1}{2}$ d 0 e 1 f $\frac{1}{3}$ 2 a $\frac{1}{11}$ b $\frac{3}{11}$ c $\frac{4}{11}$ 3 a $\frac{1}{4}$ b $\frac{1}{2}$ c $\frac{1}{13}$ d $\frac{1}{2}$ e $\frac{3}{4}$ f $\frac{2}{13}$ 4 a $\frac{8}{25}$ b $\frac{12}{25}$ c $\frac{1}{5}$ d $\frac{17}{25}$ e $\frac{4}{5}$ f 0 5 a $\frac{1}{3}$ b $\frac{2}{3}$ c $\frac{1}{3}$ d $\frac{1}{3}$ 6 a $\frac{7}{15}$ b $\frac{8}{15}$ c $\frac{1}{15}$ d $\frac{1}{3}$ e $\frac{3}{5}$ f $\frac{2}{5}$

$$g = \frac{1}{5} + h = \frac{1}{3} + i = \frac{1}{5} + j = \frac{2}{15}$$

PAGE 111 1 a $\frac{1}{3}$ b $\frac{2}{3}$ c $\frac{1}{3}$ 2 a $\frac{1}{8}$ b $\frac{3}{8}$ c $\frac{1}{8}$ d $\frac{3}{8}$ e $\frac{1}{2}$ 3 a $\frac{8}{15}$ b $\frac{7}{15}$ c 0 d 1 4 a $\frac{1}{3}$ b $\frac{1}{3}$ c $\frac{2}{3}$

5 a
$$\frac{1}{6}$$
 b $\frac{1}{2}$ c 1 d 0

PAGE 112 1 $\frac{1}{4}$ 2 a $\frac{4}{11}$ b $\frac{4}{11}$ c $\frac{7}{11}$ d $\frac{3}{11}$ 3 a $\frac{1}{2}$ b 0 c $\frac{1}{3}$ 4 a $\frac{4}{7}$ b $\frac{3}{7}$ c $\frac{1}{7}$ d $\frac{2}{7}$ e $\frac{4}{7}$ 5 a $\frac{2}{5}$ b $\frac{4}{15}$ c 0 d $\frac{1}{3}$ e 1 f $\frac{3}{5}$

PAGES 113 & 114 1 C 2 C 3 C 4 B 5 C 6 D 7 B 8 D 9 D 10 A 11 A 12 C 13 D 14 D 15 C

PAGE 115 1 3.6 2 3 3 3 4 5 5 3 6 3 7 2.88 8 3 9 $\frac{1}{6}$ 10 0 11 $\frac{2}{3}$ 12 $\frac{1}{2}$ 13 $\frac{1}{2}$ 14 $\frac{1}{2}$ 15 $\frac{1}{5}$

PAGE 116 1 a 2 b 6.125 c 2, 2, 3, 5, 6, 8, 11, 12 d 5.5 e 10 2 a 7 b 4 c $\frac{4}{7}$ d $\frac{2}{7}$ e $\frac{5}{7}$ 3 a $\frac{1}{4}$ b $\frac{1}{2}$

 $c \frac{1}{2} d \frac{1}{2} e \frac{1}{4} 4 a 5 b 25 c 5 d 30 e 8$

PAGE 117 1 ΔABC and ΔPML; ΔGHI and ΔΑΥΖ; ΔMNO and ΔJKL; ΔVWX and ΔPRO; ΔDEF and ΔSUT 2 a i ∠A and ∠C; ∠ADB and ∠CDB; ∠ABD and ∠DBC ii AD = DC; AB = BC; BD = BD b i ∠E = ∠G, ∠EHF = ∠GFH, ∠EFH = ∠GHF ii EH = FG, EF = HG, HF = HF c i ∠I = ∠K, ∠ILJ = ∠JLK, ∠IJL = ∠KJL ii IJ = LK, IL = JK, LJ = LJ d i ∠P = ∠N, ∠PMO = ∠NOM, ∠POM = ∠NMO ii MN = PO, MP = NO, MO = MO e i ∠QTS = ∠QTR, ∠S = ∠R, ∠SQT = ∠RQT ii QS = QR, QT = QT, ST = RT f i ∠U = ∠X, ∠UWV = ∠XVW, ∠UVW = ∠XWV ii UV = XW, VW = VW, UW = XV 3 a ΔAOD = ΔBOC; ΔAOB = ΔCOD; ΔADC = ΔABC; ΔABD = ΔCBD b ΔABC = ΔAED and ΔABD = ΔAEC

PAGE 118 1 a = b three sides c two angles and a side d two sides and the included angle e the hypotenuse and one side 2 a RHS b SAS c AAS d SSS 3 a OC b OA = OB c yes d RHS

PAGE 119 1 a SSS b AAS c AAS 2 a SSS b SAS c RHS d AAS e SSS f SSS

PAGE 120 1 a AAS; $x = 30^{\circ}$, $y = 60^{\circ}$ b SAS; x = 11 cm, $y = 115^{\circ}$ 2 a SSS or SAS or RHS b RHS

PAGE 121 1 a || b two angles c same ratio d one angle; the same ratio e congruent 2 a equiangular b equiangular 3 a Two

sides in the same ratio and included angle is equal to included angle. **b** $\angle A = \angle D$; $\angle B = \angle E$; $\angle C = \angle F$ **c** $\frac{AB}{DE} = \frac{AC}{DF} = \frac{BC}{EF}$

PAGE 122 1 a true b false c false d false e false f false g false h true 2 a $\frac{3}{12} = \frac{5}{20}$ and $\angle ACB = \angle ECD$ b $\frac{AO}{OC} = \frac{BO}{OD}$ and $\angle AOB = \angle DOC$ 3 $\triangle QSP$, $\triangle PSR$, $\triangle QPR$

PAGE 123 1 a equiangular; x = 5 b equiangular; y = 4 c equiangular; m = 20 d two sides and the included angle; a = 80, a = 60 equiangular; a = 60 b equiangular; a = 60 c equiangular; a = 60 d equiangular

PAGE 124 1 a equiangular b $\frac{x}{3} = \frac{6}{4}$ c $x = 4\frac{1}{2}$ 2 a equiangular b m = 115 3 a equiangular b y = 45 4 a BD

b $\angle A = \angle C$; $\angle ADB = \angle CBD$ c yes d AAS 5 a AO = CO = BO = DO = 12 cm b $\angle BOC$ c SAS

PAGES 125 & 126 1 B 2 A 3 C 4 A 5 B 6 C 7 D 8 C 9 A 10 C 11 C 12 B 13 B 14 A 15 B

PAGE 127 1 PQ = QS, QR = QR 2 ∠PQR = ∠SQR 3 ΔPQR = ΔSQR 4 SAS 5 OL = ON; OM = OM 6 ∠OML = ∠OMN;

∠OLM = ∠ONM; ∠LOM = ∠NOM 7 ΔOML = ΔOMN 8 RHS 9 ∠ACB = ∠DCE; ∠CAB = ∠CED; ∠ABC = ∠CDE

10 $\frac{5}{25}$, $\frac{3}{15}$, $\frac{4}{20}$ 11 yes 12 yes 13 The sides are in the same ratio, $\frac{AB}{DE} = \frac{AC}{CE} = \frac{BC}{CD} = \frac{1}{5}$ 14 equiangular 15 x = 25

PAGE 128 1 \angle AMB = \angle AMC, CM = BM, AM = AM; SAS 2 a \angle D = \angle B, AD = CB, AC = AC; SAS b \angle BAC = \angle DCA, AB \parallel DC (alternate angles equal) 3 a \angle BAP = \angle FEP, \angle BPA = \angle FPA, BP = FP; AAS; \therefore AP = PE b parallelogram; diagonals bisect 4 a \angle ADE = \angle ABC,

 $\angle A = \angle A$, $\angle AED = \angle ACB$ **b** equiangular **c** $\frac{AD}{AB} = \frac{AE}{AC} = \frac{DE}{BC}$

PAGES 129 & 130 1 D 2 C 3 A 4 B 5 A 6 D 7 C 8 D 9 C 10 A 11 A 12 C 13 D 14 D 15 B

Page 131 1 202.80 2 15.625 3 $1\frac{8}{25}$ 4 \$117.36 5 49 6 5:8 7 $125a^9$ 8 $\frac{4m}{5}$ 9 -a-2b 10 a 11 y+3

12 $\frac{1}{4}$ 13 $\frac{1}{9}$ 14 x^{12} 15 143.11

PAGE 132 1 a 19a b 21axy + 30xy c $\frac{10n}{3}$ d $243x^{15}y^{10}$ e $2x^3y^2z$ 2 a \$718.76 b \$1080 c \$120 d 80% e \$19.20

3 a 2m + 2n; mn b x + 2y + 3z; xy c P = S - C 4 a $\frac{4x}{5}$ b 0 c $\frac{a^2}{10}$ d $\frac{8m^2}{35}$ e $\frac{4}{3}x^5y^2$