

A Number skills: Scientific notation

Skill 1.6

Express the following using scientific notation:

- | | | | |
|----------------|---------------|--------------------|---------------|
| 1 0.003 3 | 2 0.000 048 | 3 0.014 | 4 0.028 6 |
| 5 0.000 000 2 | 6 0.000 004 2 | 7 0.000 000 6 | 8 0.000 008 9 |
| 9 0.000 481 | 10 0.014 8 | 11 0.000 186 | 12 0.000 009 |
| 13 0.000 000 2 | 14 0.000 482 | 15 0.000 000 008 9 | |

Write the numbers for these expressions:

- | | | | |
|---------------------------|---------------------------|---------------------------|----------------------------|
| 16 8.043×10^{-6} | 17 6.093×10^{-4} | 18 8.104×10^{-3} | 19 1.076×10^{-11} |
| 20 8.21×10^{-4} | 21 3.09×10^{-5} | 22 3.023×10^6 | 23 5.012×10^3 |
| 24 6.09×10^5 | 25 1.568×10^9 | 26 2.314×10^{10} | 27 3.814×10^7 |

B Number applications: Sharing quantities in a given ratio

Skill 2.1

- Steve and Colin decide to share a potential lottery win in the ratio of their contributions to buy the ticket. If Steve puts in \$3.50 for a \$10.00 ticket then how much will each receive if they win \$1.1 million?
- A block of chocolate with 48 squares is to be shared in the ratio of 1:2:4. To the nearest square, how much will each receive?

C Algebra: Working with lateral equations

Skill 3.8

1 Make b the subject of these equations:

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|---------------------------|-----------------------------|----------------------|-----------------------------|
| (a) $A = Lb$ | (b) $V = Lbh$ | (c) $W = 4ab^2$ | (d) $A = \frac{1}{2}bh$ |
| (e) $Z = \frac{bh^2}{6}$ | (f) $A = \frac{1}{2}(a+b)h$ | (g) $W = aL + b$ | (h) $F = \frac{b}{r^2} + a$ |
| (i) $P = a + \frac{w}{b}$ | (j) $S = \frac{b}{2}(a+c)$ | (k) $P = b(a-d) + s$ | (l) $A = \pi b^2$ |

2 The formula connecting a particle's velocity (v m/s), acceleration (a m/s²) and distance travelled (s m) is $v^2 = 2a$. Make s the subject and so find the distance travelled for these values:

- | | |
|---|--|
| (a) $v = 9$ m/s, $a = 2$ m/s ² | (b) $v = 4$ m/s, $a = 3$ m/s ² |
| (c) $v = 10$ m/s, $a = 3$ m/s ² | (d) $v = 1.8$ m/s, $a = 0.3$ m/s ² |
| (e) $v = 3.9$ m/s, $a = 2.6$ m/s ² | (f) $v = 11.2$ m/s, $a = 6.3$ m/s ² |

D Algebra: Simultaneous equations

Skill 3.9

1 Solve these simultaneous equations using the substitution method:

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|------------------------------|-------------------------------|
| (a) $y = 3x, x + 2y = 14$ | (b) $y = -x, x + 2y = -4$ |
| (c) $y = x + 2, 2x + y = 11$ | (d) $x = 6 + y, 4x + 3y = 31$ |

2 Solve these simultaneous equations using the elimination method:

- | | | | |
|------------------|------------------|--------------------|--------------------|
| (a) $x + y = 16$ | (b) $3x + y = 4$ | (c) $2x + 3y = 12$ | (d) $5x - 2y = 10$ |
| $x - y = -2$ | $-2x - y = 6$ | $x + y = 3$ | $x + y = 2$ |

E Indices: Expanding brackets with indices

Skill 4.5

Simplify:

- | | | | |
|---|---|---|--|
| 1 $\left(\frac{2a^4}{b}\right)^3$ | 2 $\left(\frac{3^2 a}{b^4}\right)^2$ | 3 $\left(-6^2 a^4 b^5\right)^2$ | 4 $\left(-\frac{2a^2 b^4}{c}\right)^3$ |
| 5 $\left(\frac{5^2 ab^3}{c^4}\right)^2$ | 6 $\left(\frac{-3^3 a^2}{b^4}\right)^2$ | 7 $\left(\frac{a^2 b^3}{c^4}\right)^{10}$ | 8 $\left(\frac{2^3 a}{b^2}\right)^3$ |
| 9 $\left(\frac{-3^2 b^4}{c^4}\right)^3$ | 10 $\left(6^2 a^4 b^3\right)^2$ | 11 $\left(-4a^2 b^3 c^4\right)^3$ | 12 $\left(-3a^4 b^6 c^8\right)^2$ |

Worksheet 7

- A** 1 3.8×10^{-3} 2 4.8×10^{-5} 3 1.4×10^{-2}
 4 2.86×10^{-2} 5 2×10^{-7} 6 4.2×10^{-6}
 7 6×10^{-7} 8 8.9×10^{-6} 9 4.81×10^{-4}
 10 1.48×10^{-2} 11 1.86×10^{-4} 12 9×10^{-6}
 13 2×10^{-7} 14 4.82×10^{-4} 15 8.9×10^{-9}
 16 0.000 008 043 17 0.000 609 3
 18 0.008 104 19 0.000 000 000 010 76
 20 0.000 821 21 0.000 030 9
 22 3 023 000 23 5012
 24 609 000 25 1 568 000 000
 26 23 140 000 000 27 38 140 000

- B** 1 Steve \$385 000, Colin \$715 000
 2 7, 14, 27

- C** 1 (a) $b = \frac{A}{L}$ (b) $b = \frac{V}{Lh}$ (c) $b = \sqrt{\frac{W}{4a}}$
 (d) $b = \frac{2A}{h}$ (e) $b = \frac{6Z}{h^2}$ (f) $b = \frac{2A}{h} - a$
 (g) $b = W - aL$ (h) $b = r^2(F - a)$ (i) $b = \frac{w}{(P - a)}$
 (j) $b = \frac{2S}{(a + c)}$ (k) $b = \frac{P - s}{a - d}$ (l) $b = \sqrt{\frac{A}{\pi}}$

2 $s = \frac{v^2}{2a}$

- (a) 20.25 m (b) $2\frac{2}{3}$ m (c) $16\frac{2}{3}$ m
 (d) 5.4 m (e) 2.925 m (f) 9.96 m

- D** 1 (a) $x = 2, y = 6$ (b) $x = 4, y = -4$
 (c) $x = 3, y = 5$ (d) $x = 7, y = 1$
 2 (a) $x = 7, y = 9$ (b) $x = 10, y = -26$
 (c) $x = -3, y = 6$ (d) $x = 2, y = 0$

- E** 1 $\frac{8a^{12}}{b^3}$ 2 $\frac{81a^2}{b^8}$ 3 $1296a^8b^{10}$
 4 $\frac{-8a^6b^{12}}{c^3}$ 5 $\frac{625a^2b^6}{c^8}$ 6 $\frac{729a^4}{b^8}$
 7 $\frac{a^{20}b^{30}}{c^{40}}$ 8 $\frac{512a^3}{b^6}$ 9 $\frac{-729b^{12}}{c^{12}}$
 10 $1296a^8b^6$ 11 $-64a^6b^9c^{12}$ 12 $9a^8b^{12}c^{16}$