

Exercise 8.1

1. Differentiate $\ln(x + \sqrt{x^2 + 1})$ with respect to x . Hence, find $\int \frac{1}{\sqrt{x^2 + 1}} dx$.
2. Given that $y = (x + 3)\sqrt{2x - 3}$, show that $\frac{dy}{dx} = \frac{3x}{\sqrt{2x - 3}}$. Hence, find $\int \frac{x}{\sqrt{2x - 3}} dx$.
3. Find $\frac{d}{dx}(x \cos x)$. Hence, evaluate $\int (\cos x - x \sin x) dx$.
4. Differentiate $\frac{x^2}{2x - 1}$ with respect to x and hence evaluate $\int \frac{x(x - 1)}{(2x - 1)^2} dx$.
5. Given that $y = \ln \cos x$, find $\frac{dy}{dx}$. Hence, find $\int \tan x dx$.

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1. $\frac{1}{\sqrt{x^2 + 1}}, \ln(x + \sqrt{x^2 + 1}) + c$
2. $3(x + 3)\sqrt{2x - 3} + c$
3. $\cos x - x \sin x; x \cos x + c$
4. $\frac{2x(x - 1)}{(2x - 1)^2}; \frac{1}{2} \left(\frac{x^2}{2x - 1} \right) + c$
5. $-\tan x, -\ln |\cos x| + c$