

A novel grating lobes suppression method of sparse arrays for acoustic source localization

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Outline

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- Approach
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 - 2) Beamforming Method
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 - 4) Comprehensive Processing
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Problems to be solved

Problem:

Existing algorithms: **ULA**, $d \leq \lambda / 2$;

Adding sensors to obtain **high resolution, high costs**;

Optical fiber sensor: **d=0.1m**, $f_0 = 7.5\text{kHz}$;

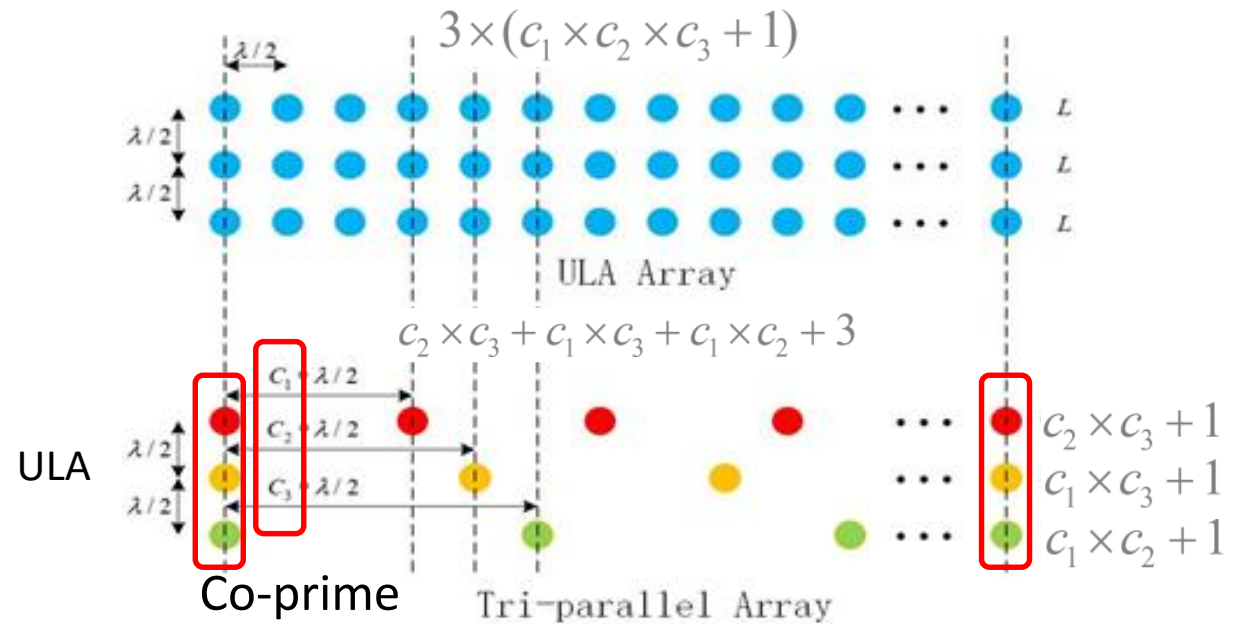
Sparse array is developed, but suffers from azimuth ambiguity caused by the **grating lobes**.

To deal :

A new array structure is designed ;

Comprehensive processing eliminates the azimuth ambiguity caused by grating lobes.

Approach - Array Structure



The array structure of optical fiber sensor array

Approach - Beamforming Method

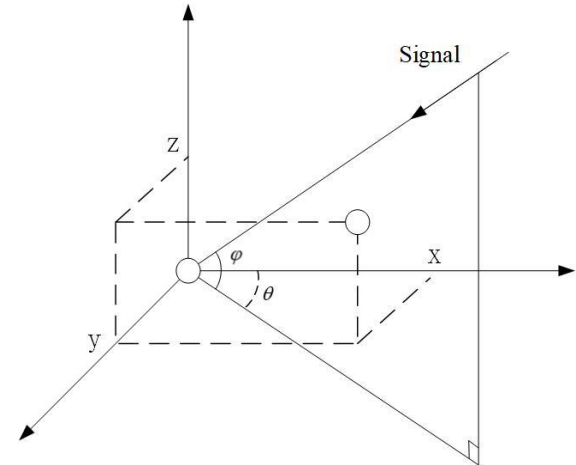
For each sub array, the beamforming is carried out utilizing conventional beamforming (CBF).

The received signal column vector can be expressed as a vector:

$$\mathbf{X}_i(t) = \mathbf{A}_i \mathbf{S}(t) + \mathbf{N}_i(t), i = 1, 2, 3$$

$$\mathbf{A}_i = [\mathbf{a}_{i1}(\omega_0) \quad \mathbf{a}_{i2}(\omega_0) \quad \cdots \quad \mathbf{a}_{iN}(\omega_0)], i = 1, 2, 3$$

$$\mathbf{a}_i(\omega_0) = \begin{bmatrix} \exp(-j\omega_0\tau_{i1k}) \\ \exp(-j\omega_0\tau_{i2k}) \\ \vdots \\ \exp(-j\omega_0\tau_{iM,k}) \end{bmatrix}, i = 1, 2, 3, k = 1, 2, \dots, N$$



Approach - Beamforming Method

The basic orientation information obtained from the three sub-arrays respectively.

Spatial Spectrum: $P_i(\theta, \varphi) = \mathbf{a}_i^H(\theta, \varphi) \mathbf{R}_{ix} \mathbf{a}_i(\theta, \varphi), i = 1, 2, 3$

$$\mathbf{R}_{ix} = \frac{1}{p} \sum_{n=1}^p [\mathbf{X}_i(n) \mathbf{X}_i^H(n)]$$

Output: $y_i(\theta, \varphi) = \mathbf{w}_i^H(\theta, \varphi) \mathbf{X}_i$

Due to the spatial under-sampling, the spatial spectrum obtained by the conventional beamforming scanning of each sub-array is affected by grating lobes, which seriously affect the quality of signal azimuth estimation.

Approach – Product & Min Processing

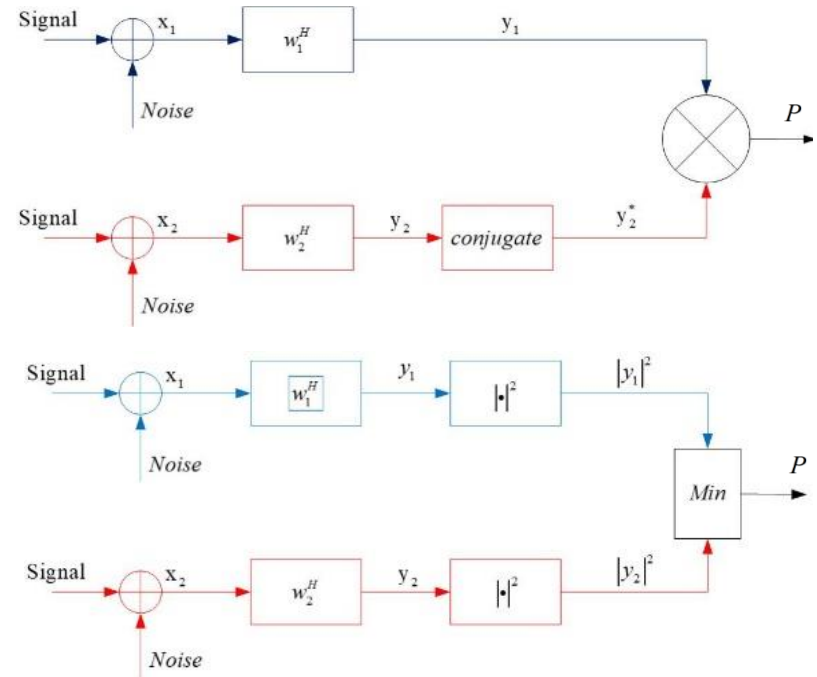
Product Processor:

$$P_{i,j}(\theta, \varphi) = y_i(\theta, \varphi) * \text{conj}(y_j^T(\theta, \varphi)),$$

$$i \neq j \in [1,2]$$

Min Processor:

$$P_{\min 1,2} = \min(P_1(\theta, \varphi), P_2(\theta, \varphi))$$



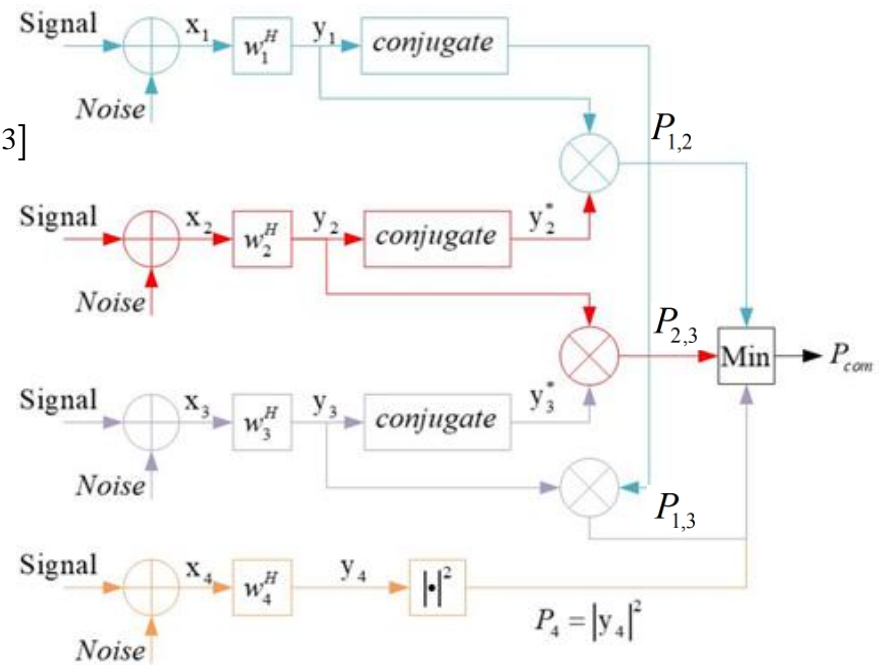
[1] Gaussian Source Detection and Spatial Spectral Estimation Using a Coprime Sensor Array With the Min Processor

Approach - Comprehensive Processing

$$P_{i,j}(\theta, \varphi) = y_i(\theta, \varphi) * \text{conj}(y_j^T(\theta, \varphi)), i \neq j \in [1, 2, 3]$$

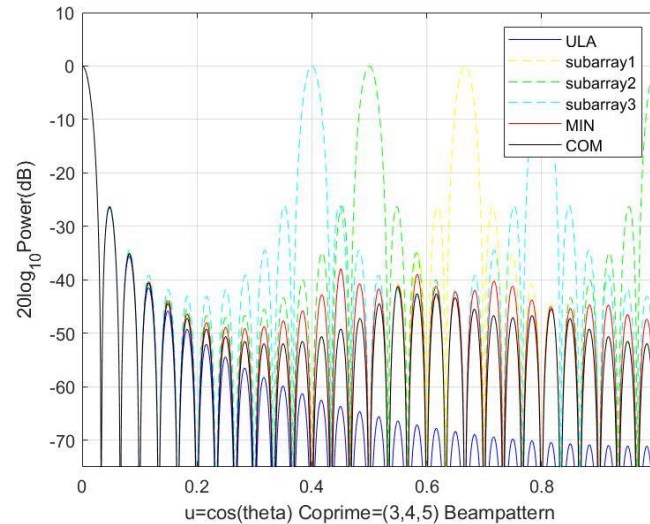
$$P_{\min 1,2,3} = \min(P_{1,2}(\theta, \varphi), P_{2,3}(\theta, \varphi), P_{3,1}(\theta, \varphi))$$

$$P_{Com} = \min(P_{\min 1,2,3}, P_{ula})$$



Results and Discussion

Assume that $c_1=3$, $c_2=4$, $c_3=5$, so sub-array 1,2,3 has 21,16,13 sensors separately. The compared ULA has 3 lines, each line has 60 sensors.



Beam Patterns

Results and Discussion

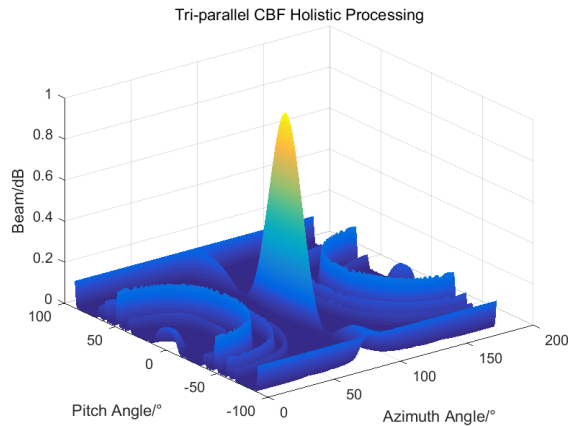


Fig.1

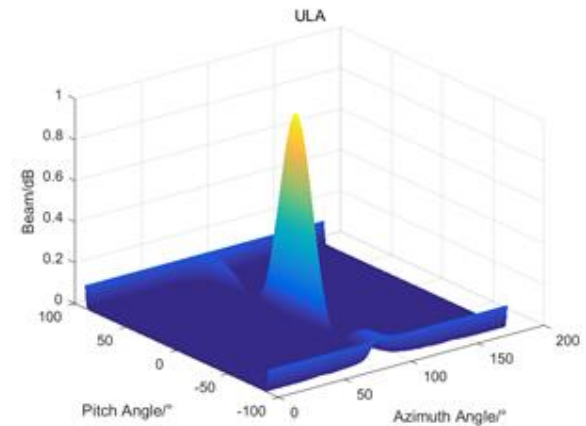


Fig.2

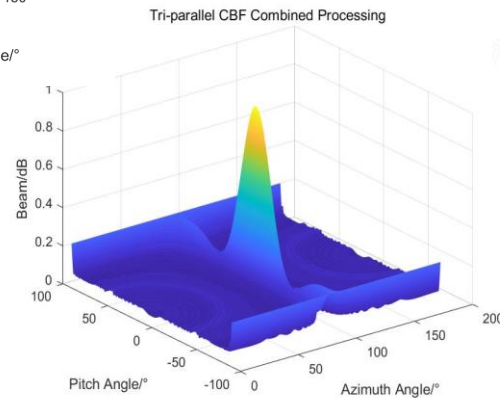


Fig.3

Conclusions

- Improve the resolution;
- Reduce the complexity of calculation and cost;
- Achieve large aperture using a novel coprime sparse sensor arrays;
- Suppress grating lobes;
- Lower side lobes than Min Processor.

The end

THANK YOU !